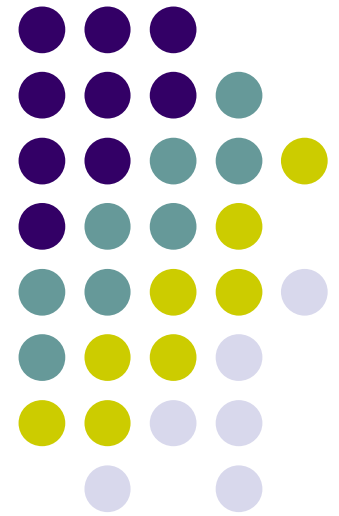


# Magneto-convection

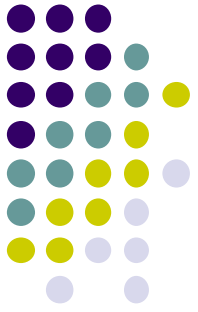
**Åke Nordlund**  
**Niels Bohr Institute**  
**University of Copenhagen**

with

Anders Lagerfjård, Fernando Moreno-Insertis  
Werner Schaffnerberger, Bob Stein, Göran Scharmer

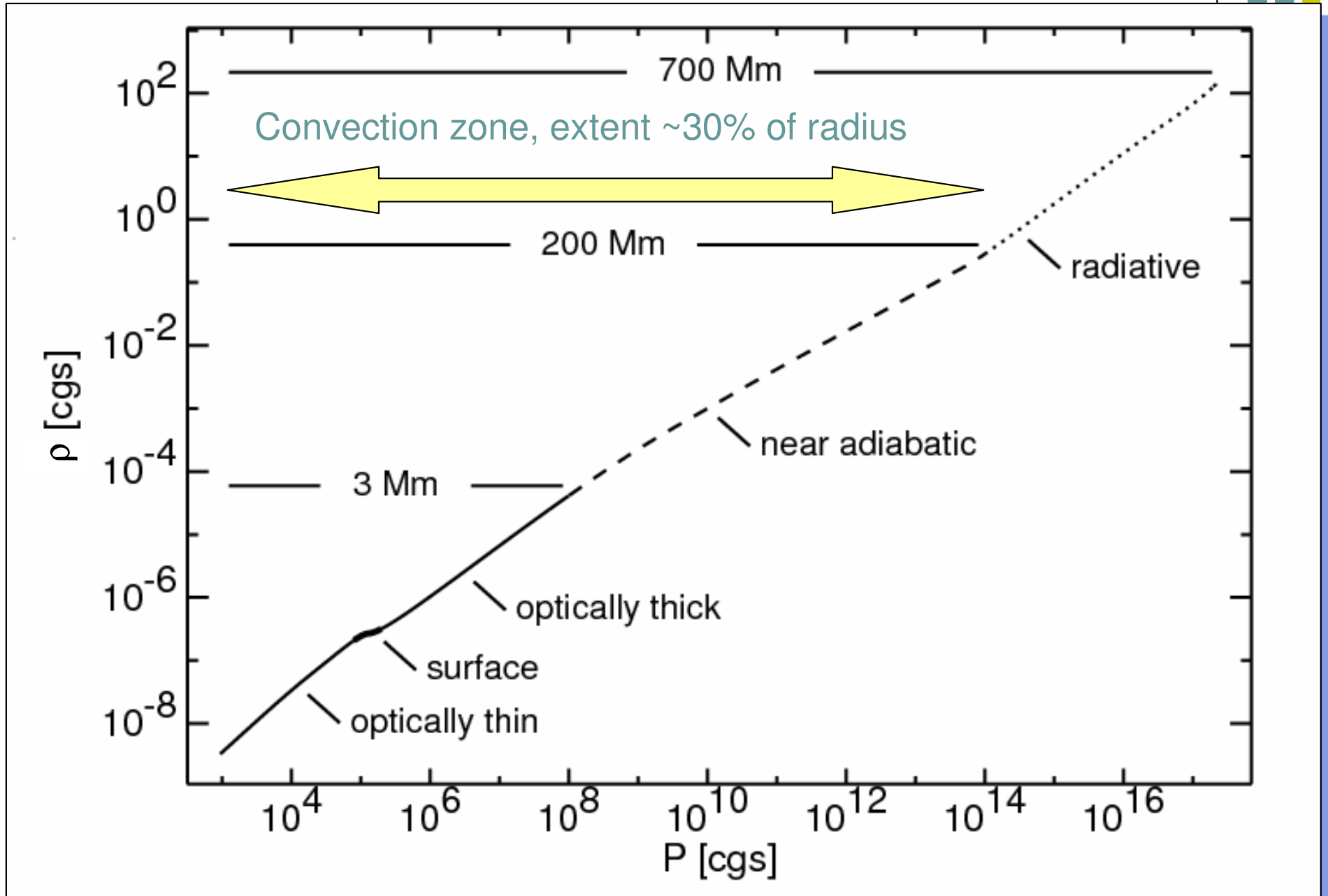


# Summary of main points

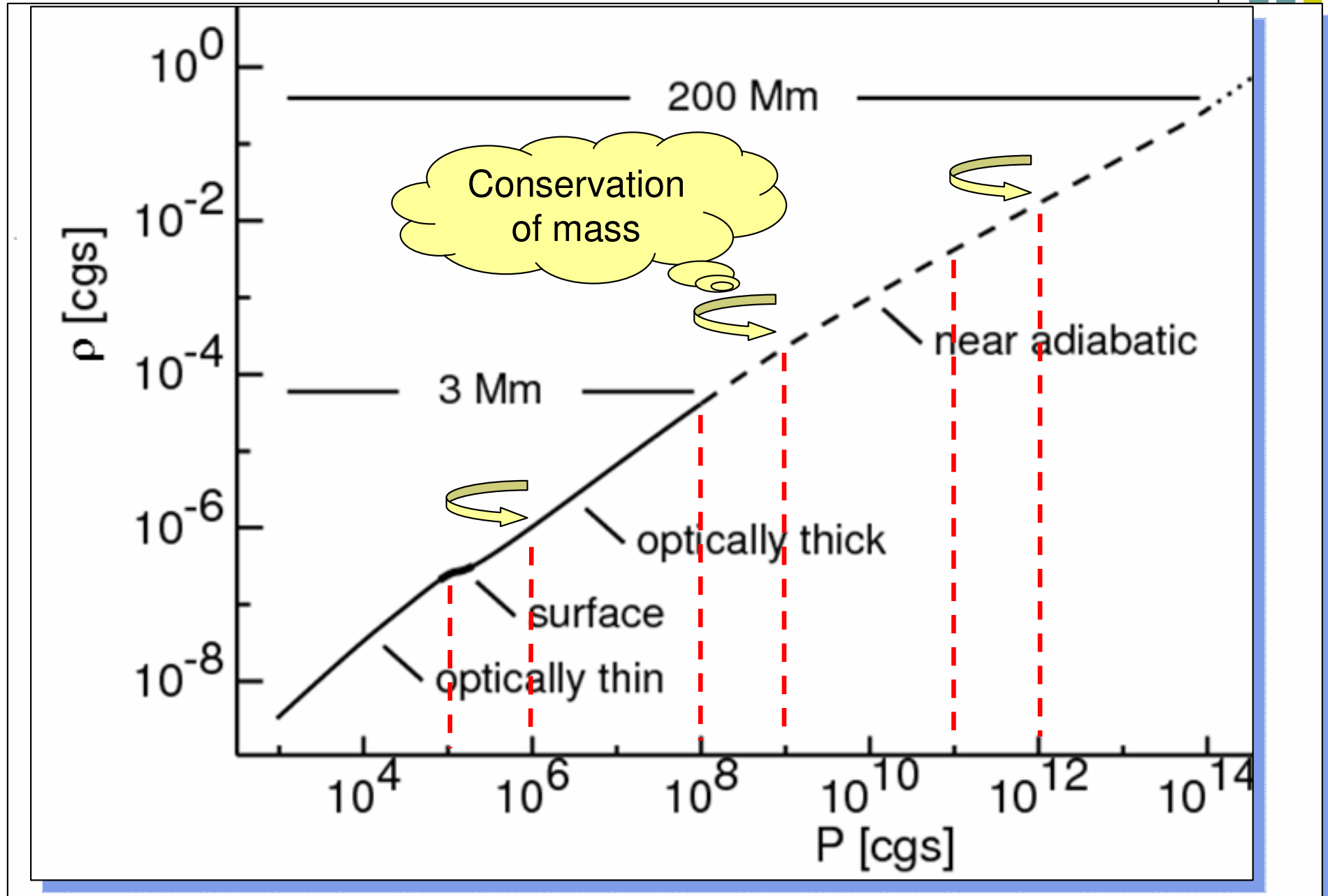


- Stellar magneto-convection is fundamentally *multi-scale*
- But also has *scale invariance* to some extent
- Two asymptotic regimes; **small and large**
  - The Sun + simulations prove that *turbulent dissipation converges* at relatively low Re
- Implications for sunspots and penumbrae
  - More on Thursday ...

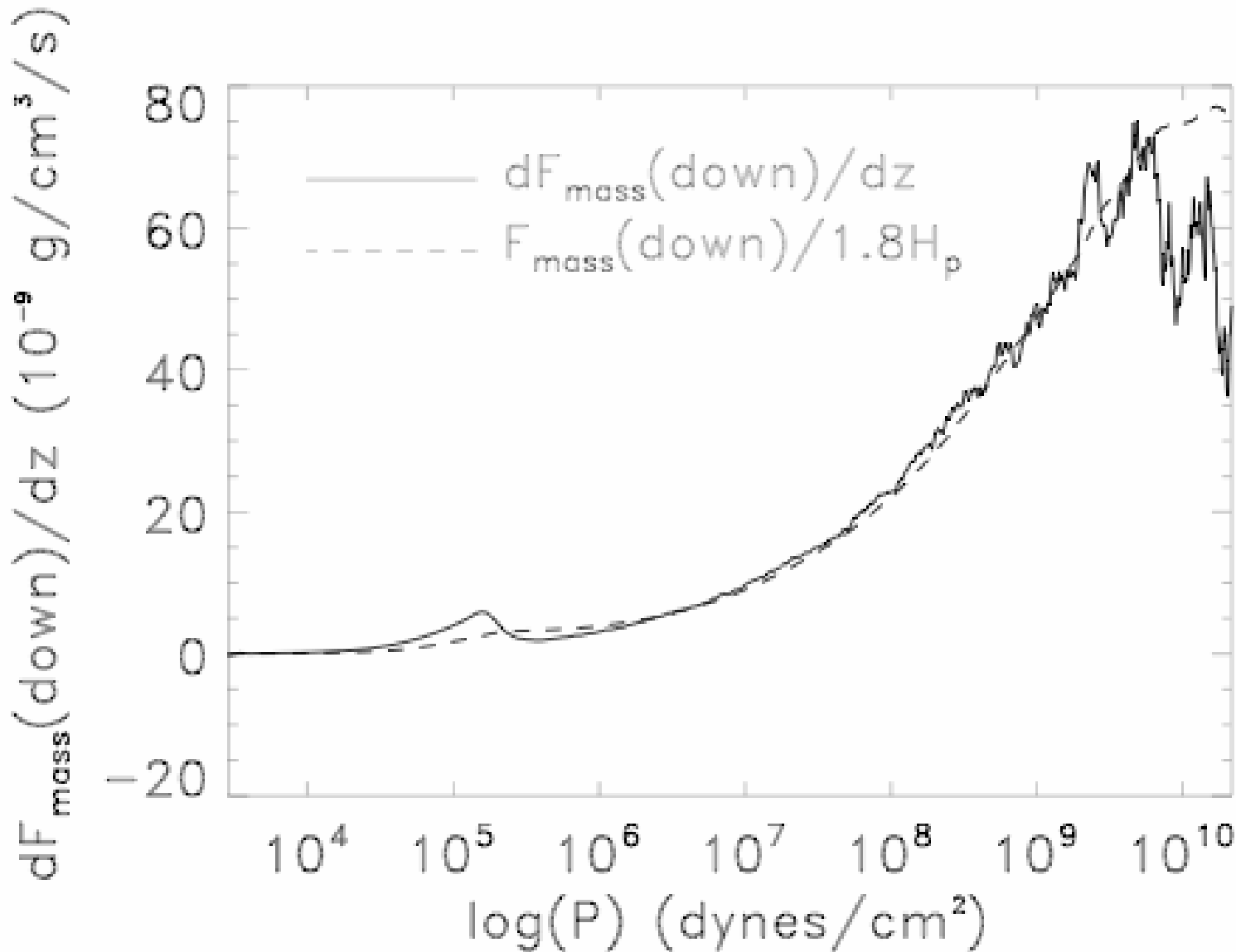
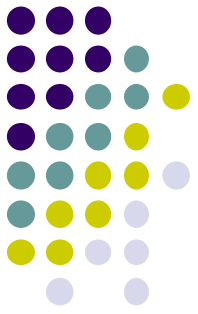
# Overall Solar Structure



# Convection Zone



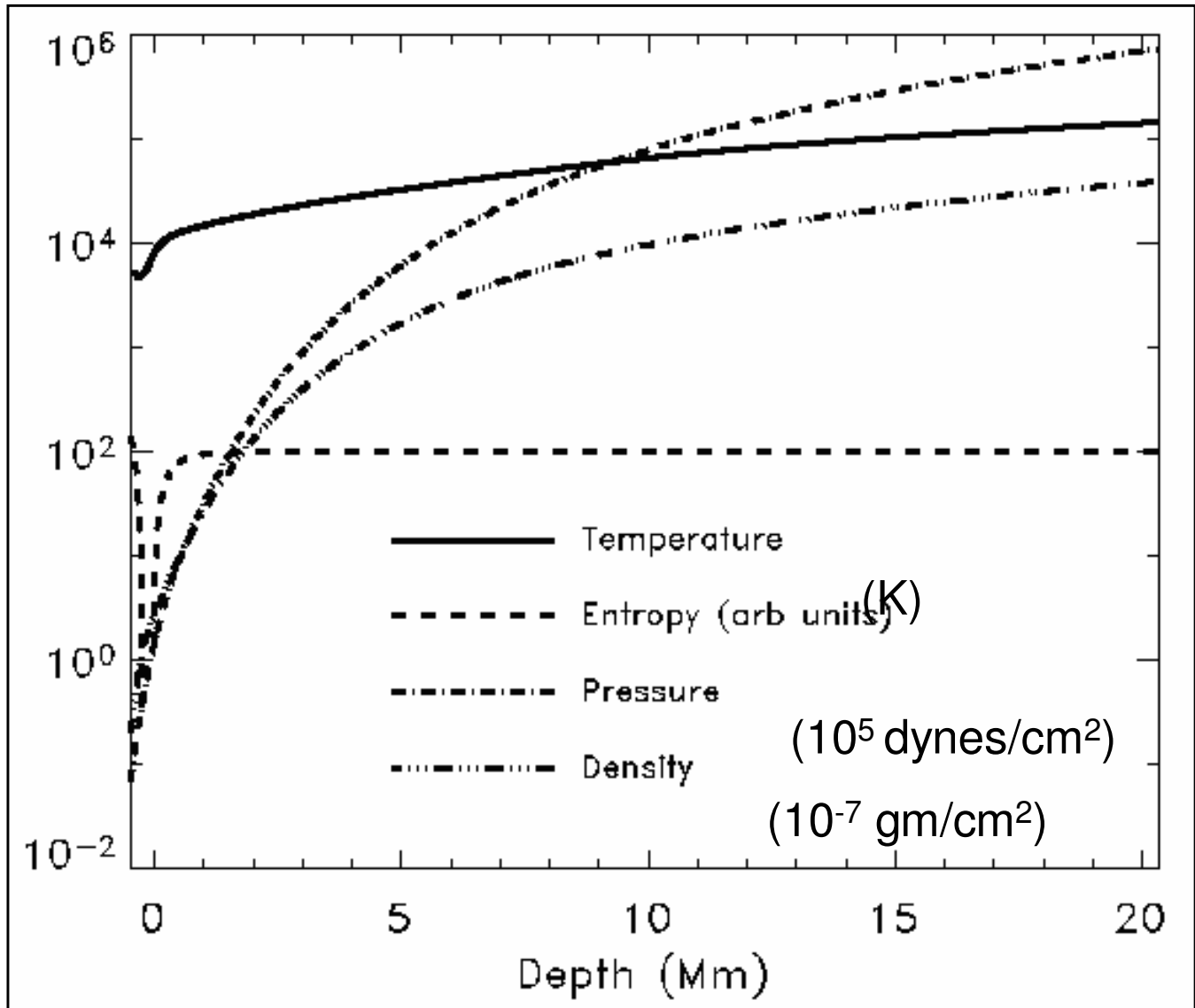
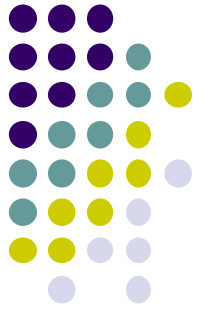
# Mass conservation



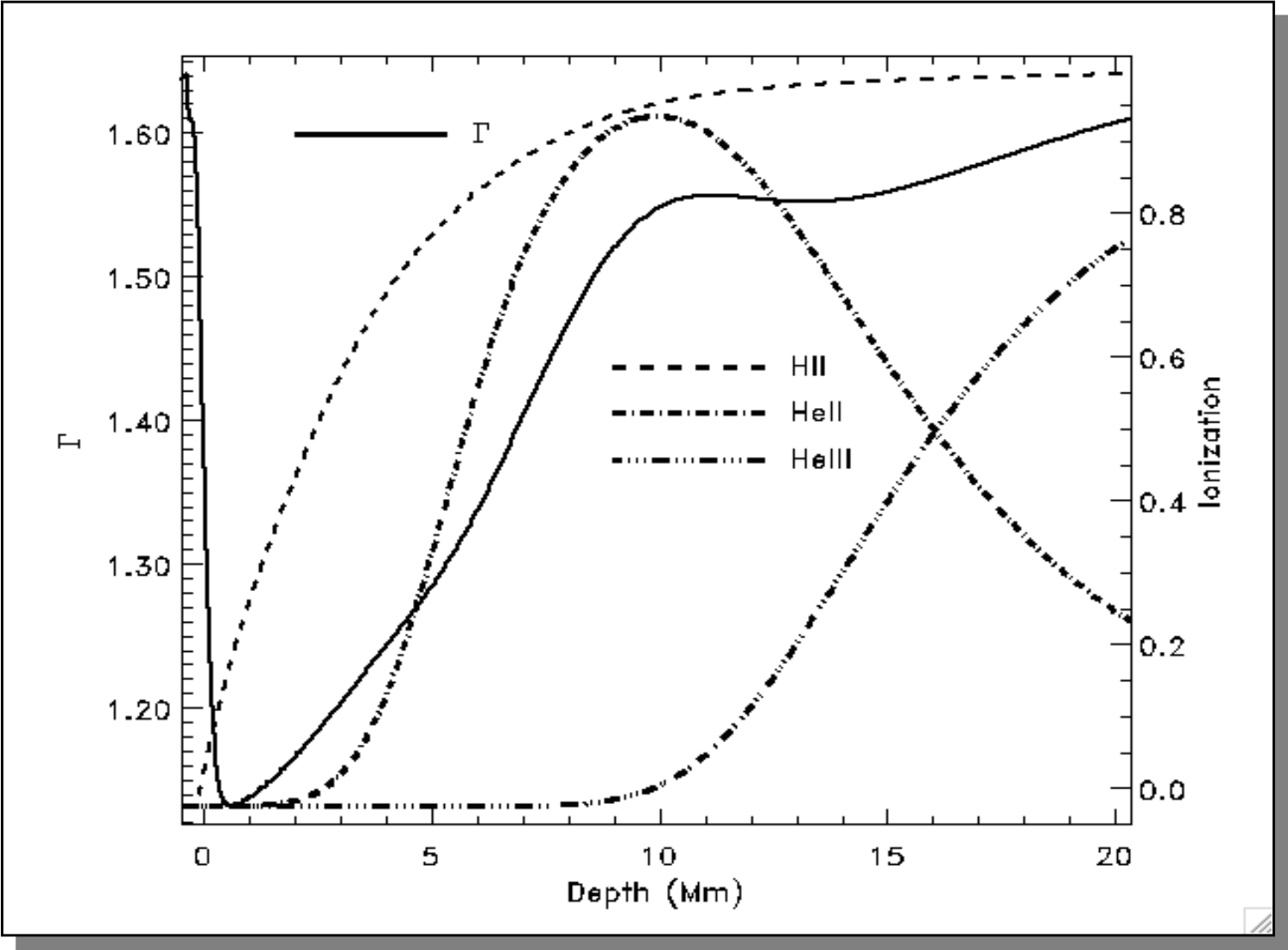
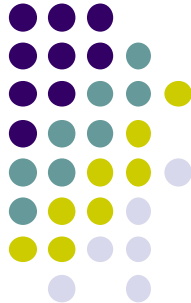
Rising fluid must turn over and descend within about a scale height to conserve mass.

The actual mixing (entrainment) length in simulations is  $1.8 H_p$ .

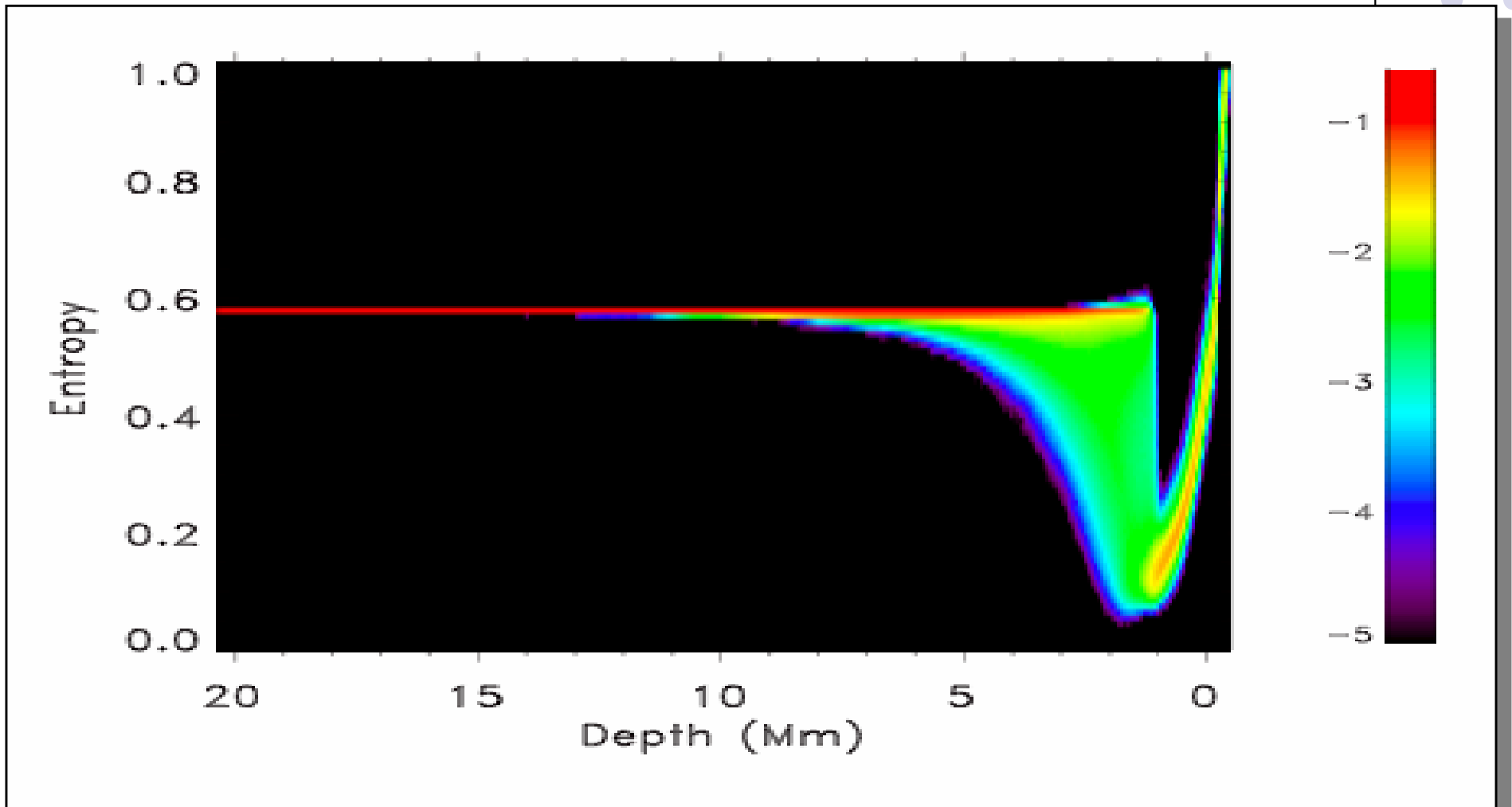
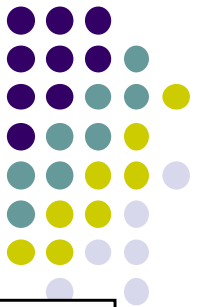
# Mean stratification



# Ionization of H and He

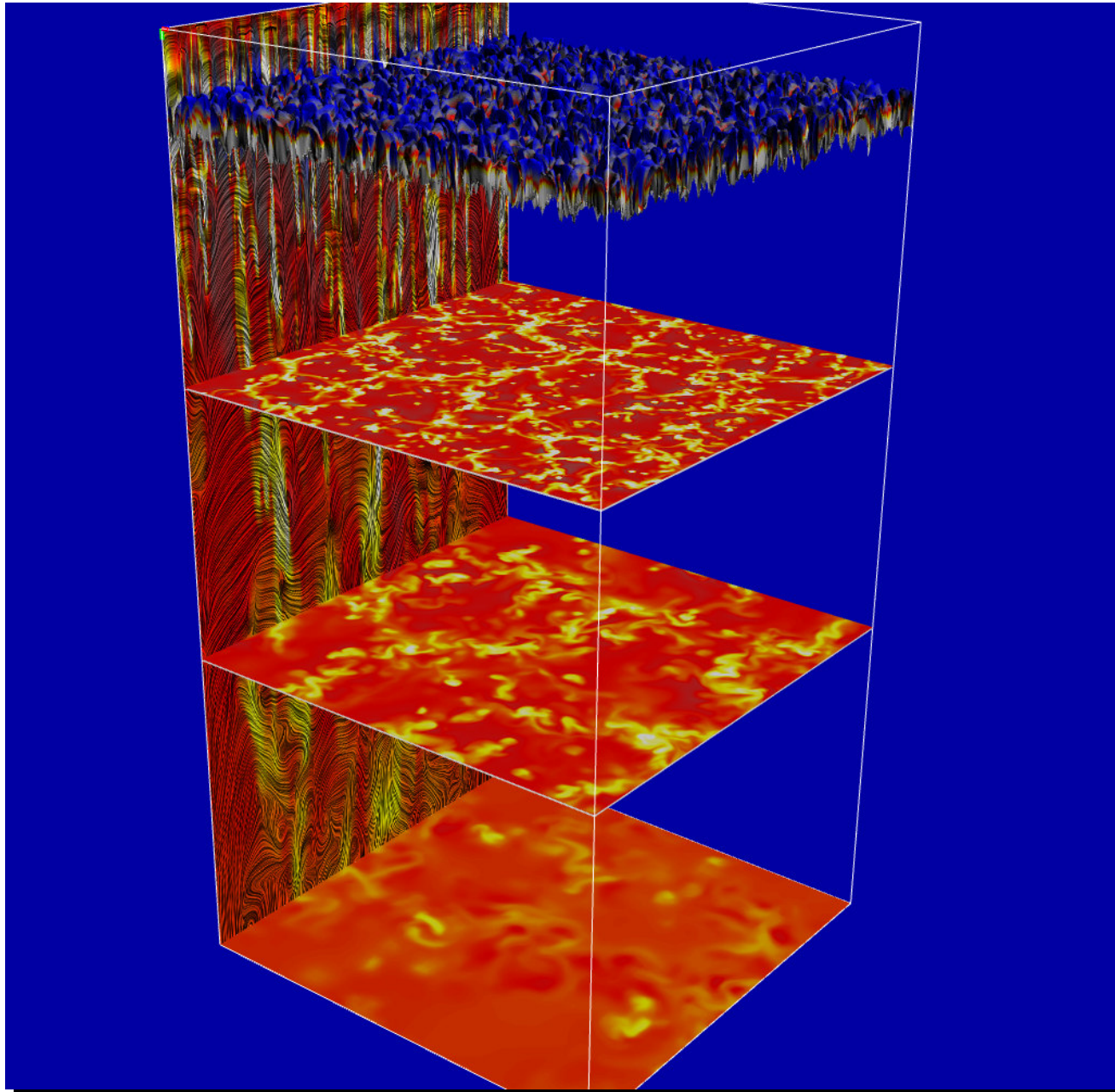
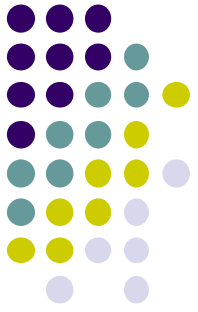


# Entropy Histogram



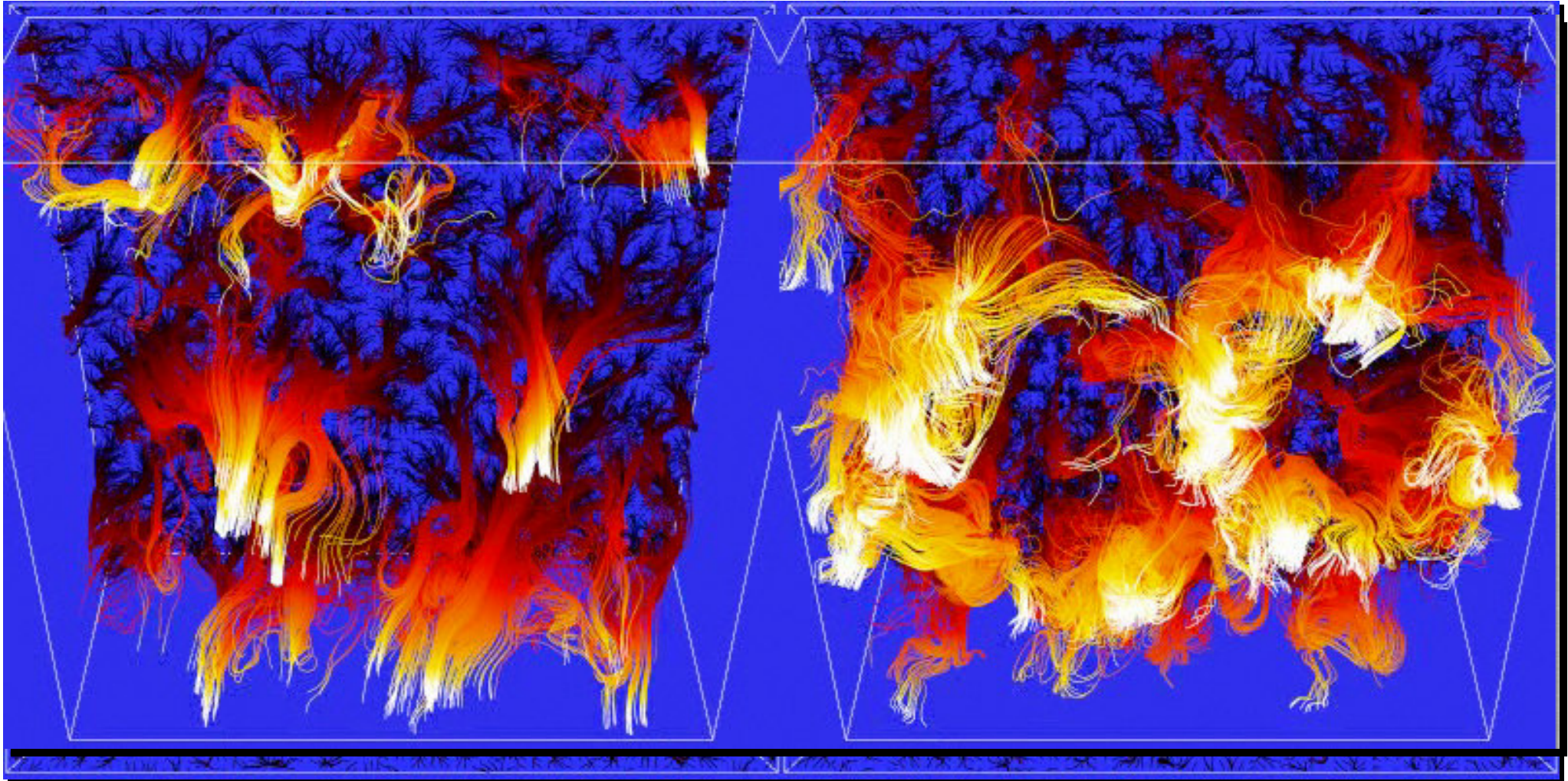
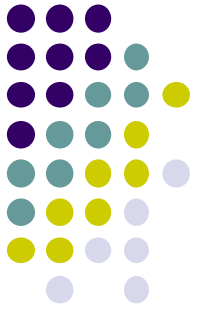


# Velocity patterns

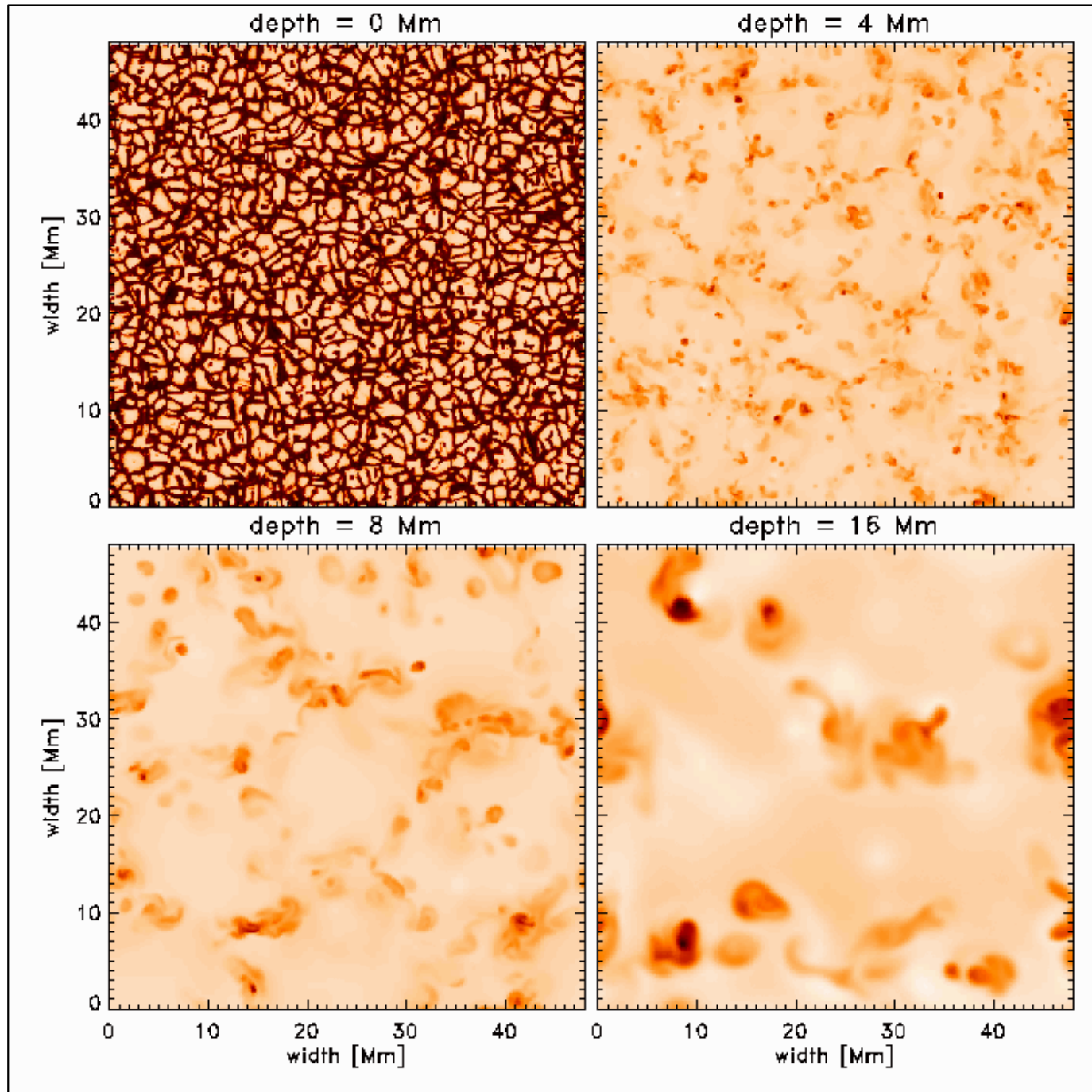
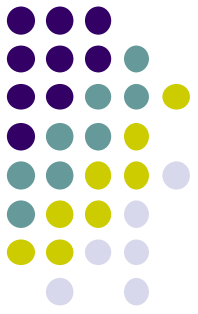


**Upflows at surface come from small area at bottom (left)**

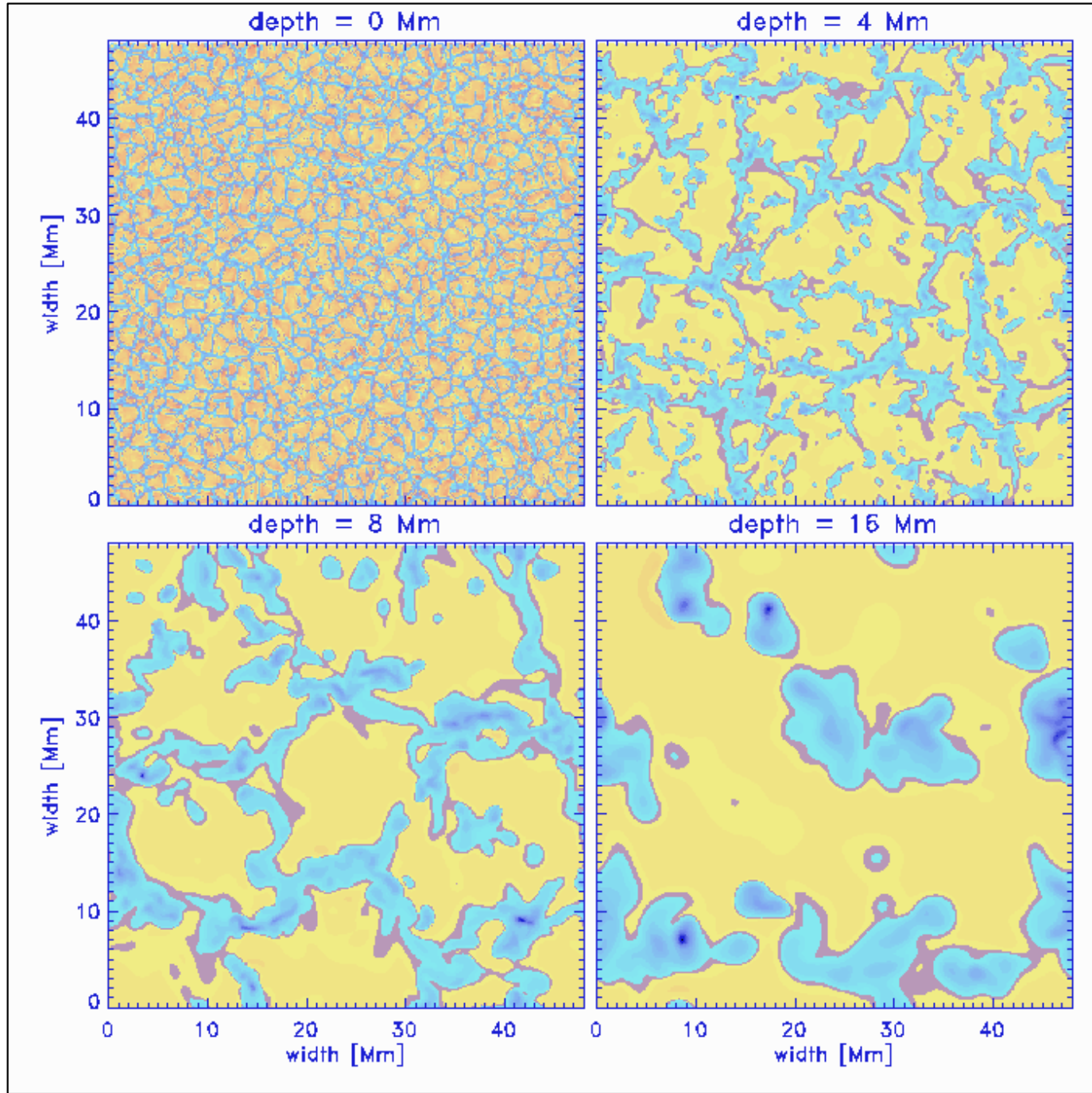
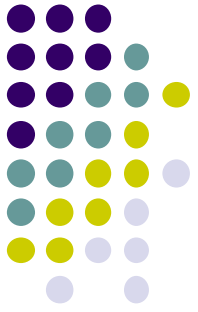
**Downflows at surface converge to supergranule boundaries (right)**



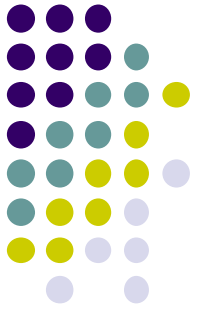
# Temperature patterns at four different depths



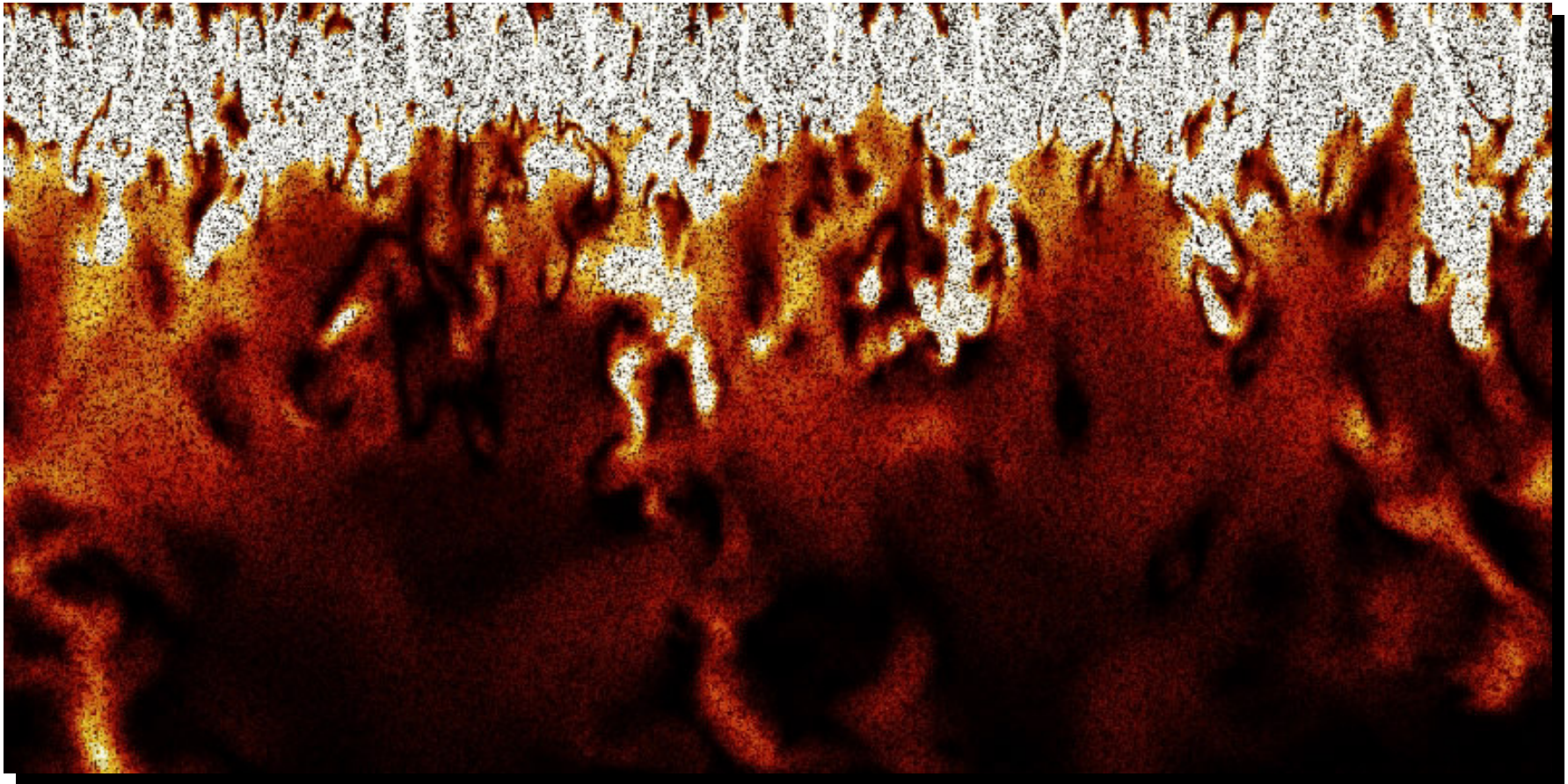
# Velocities at the same depths



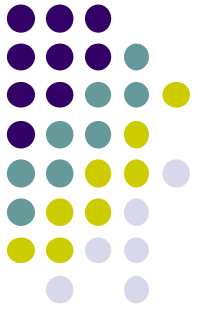
# Large scale solar convection (48x48x20 Mm) -- Stein & Nordlund 2008



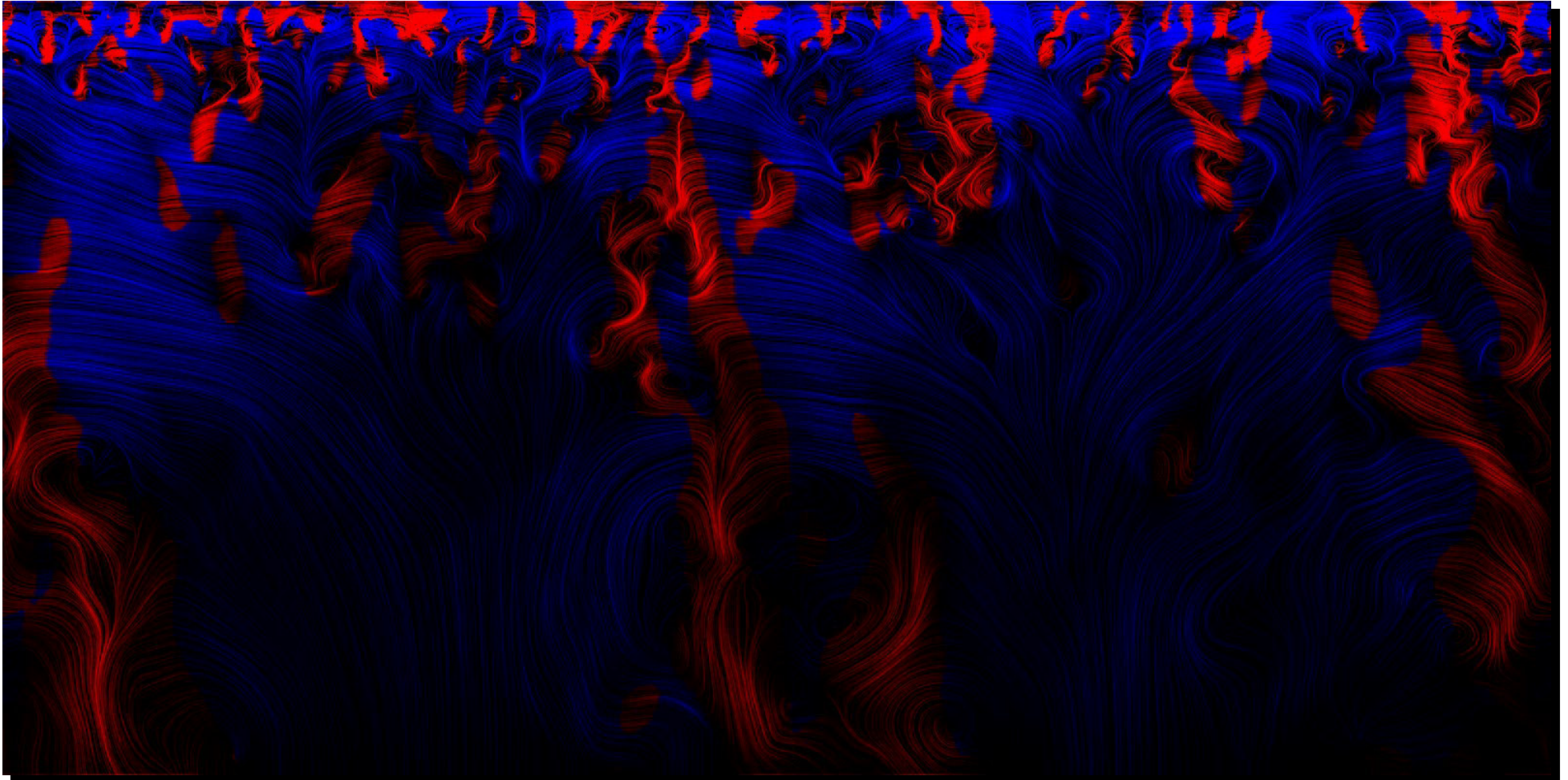
Finite lifetime corks, on top of color ~ velocity magnitude



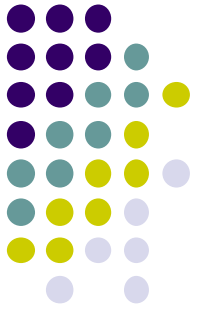
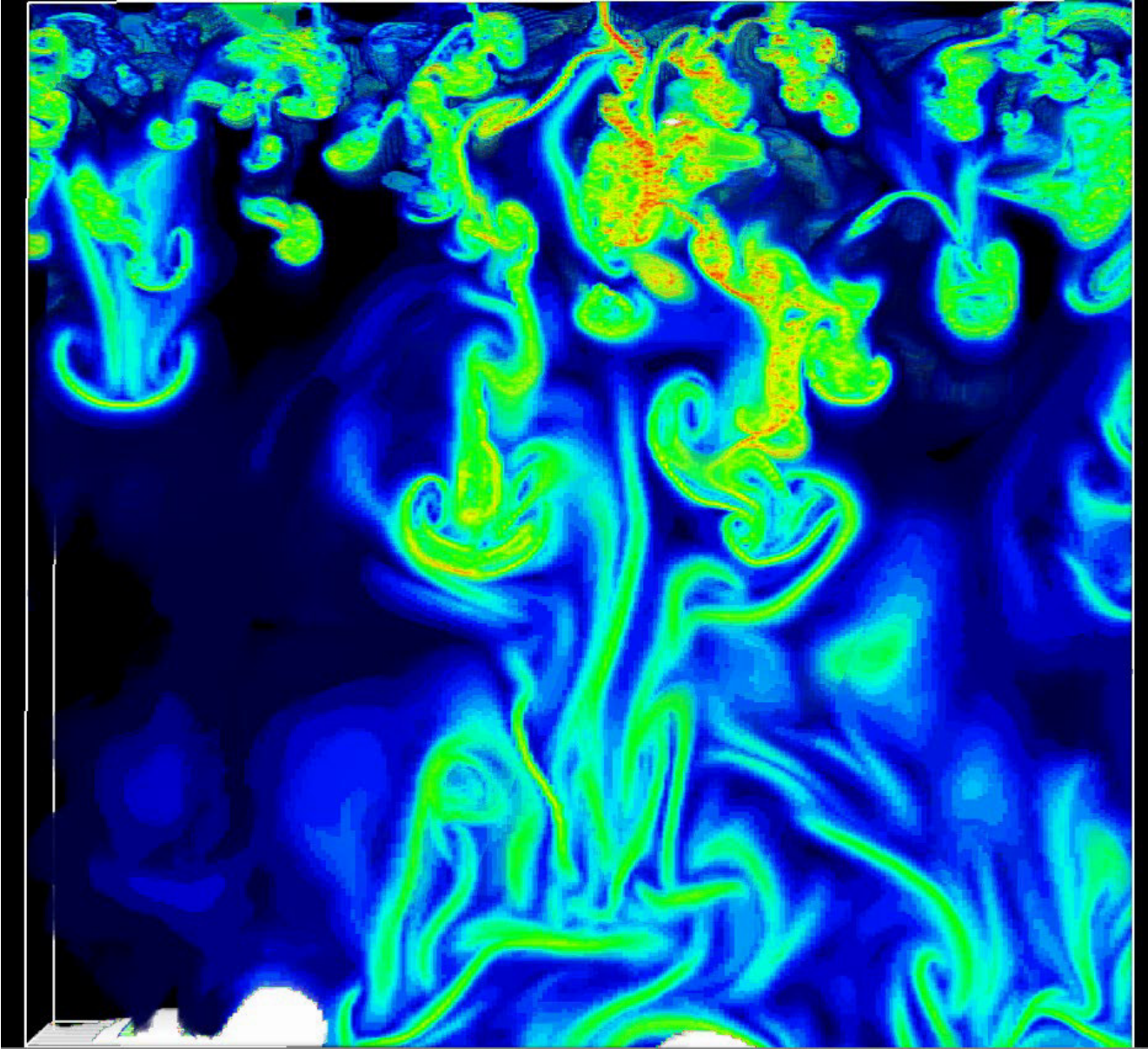
# Large scale solar convection (48x48x20 Mm) -- Stein & Nordlund 2008



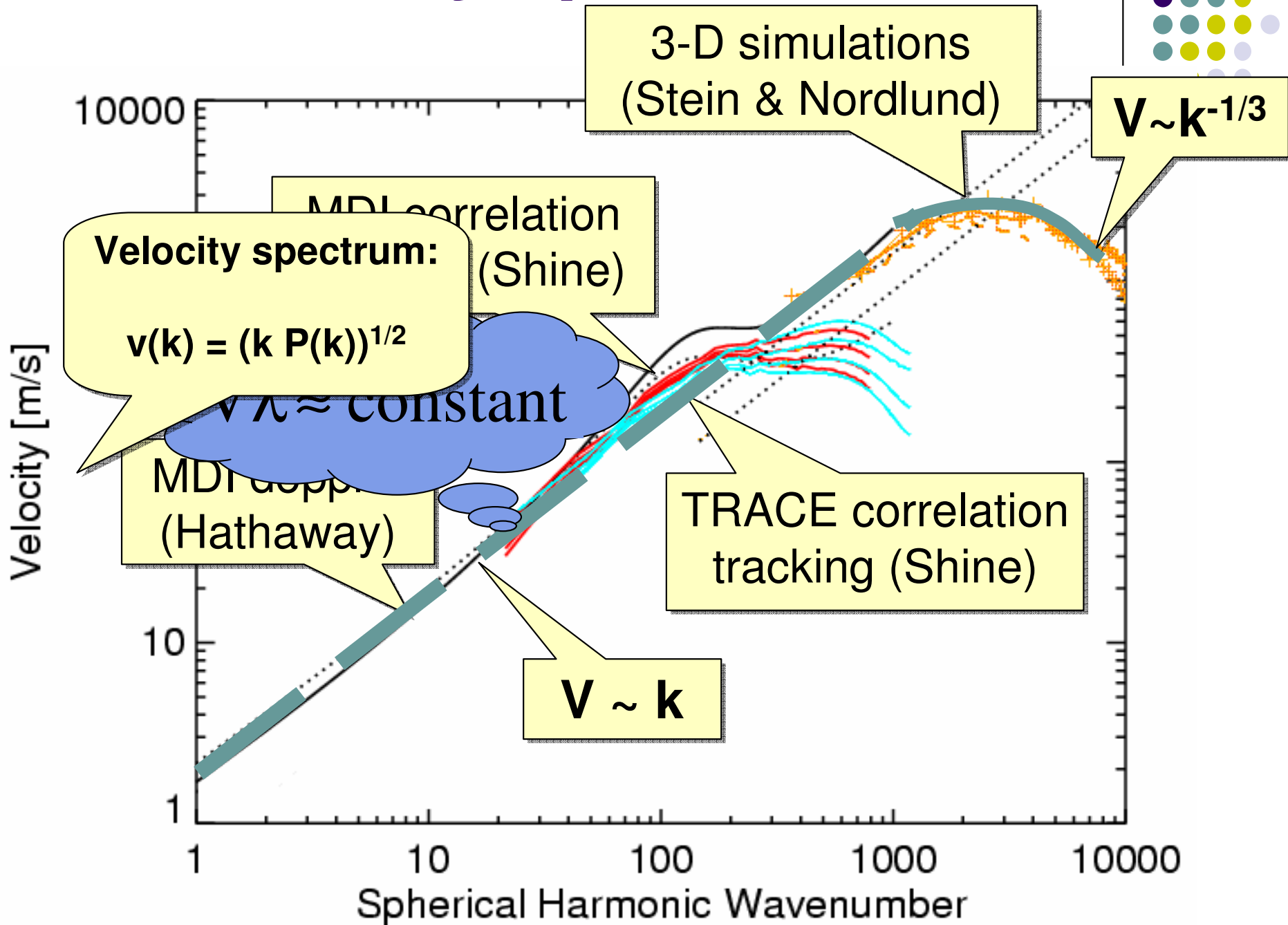
Blue and red show up and down velocity



# Vorticity

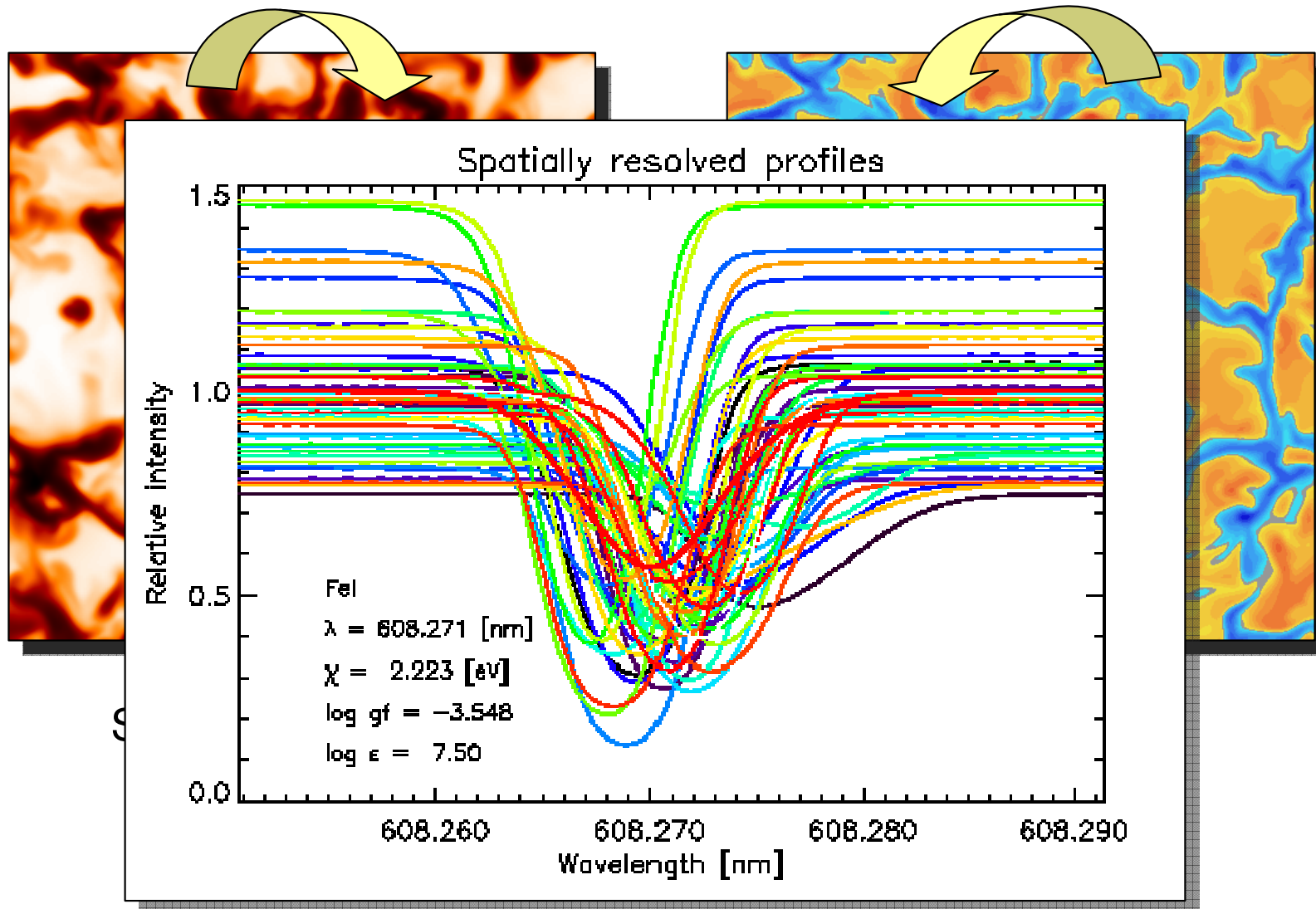
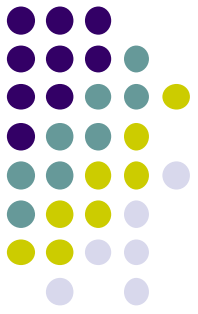


# Solar velocity spectrum



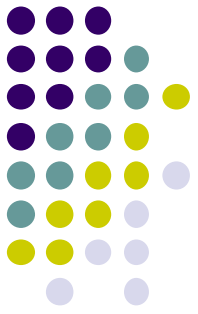


# Synthetic solar spectral lines – a crucial fingerprint!

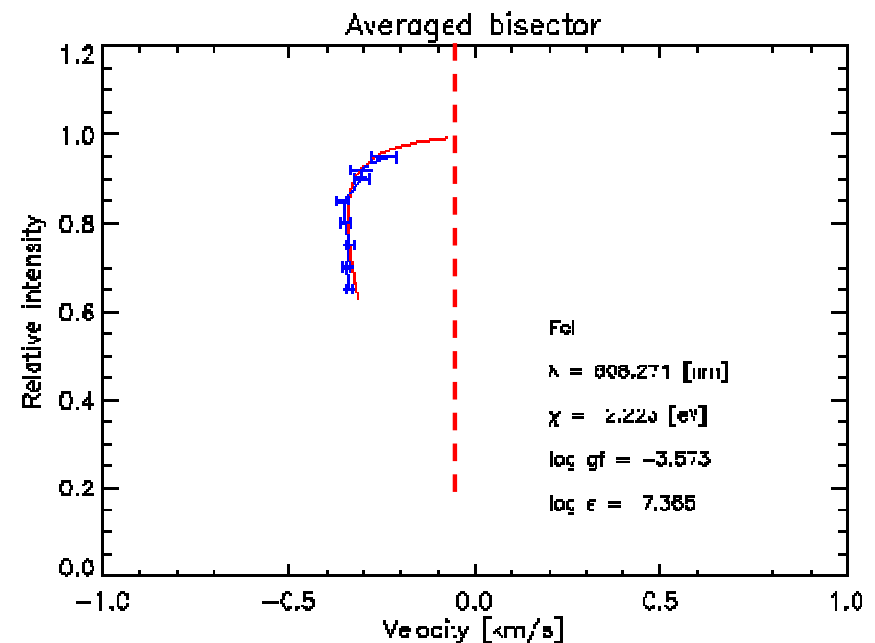
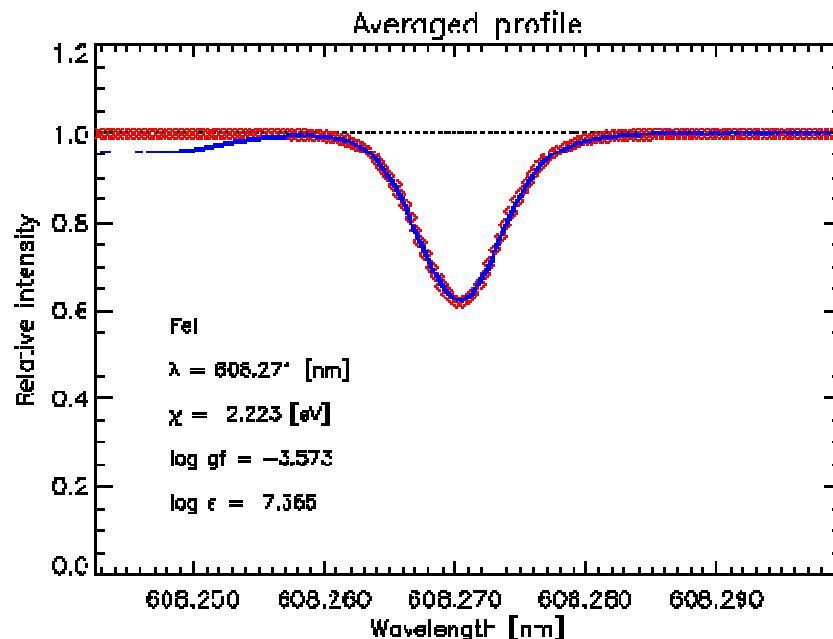


Spatially resolved spectral line profiles

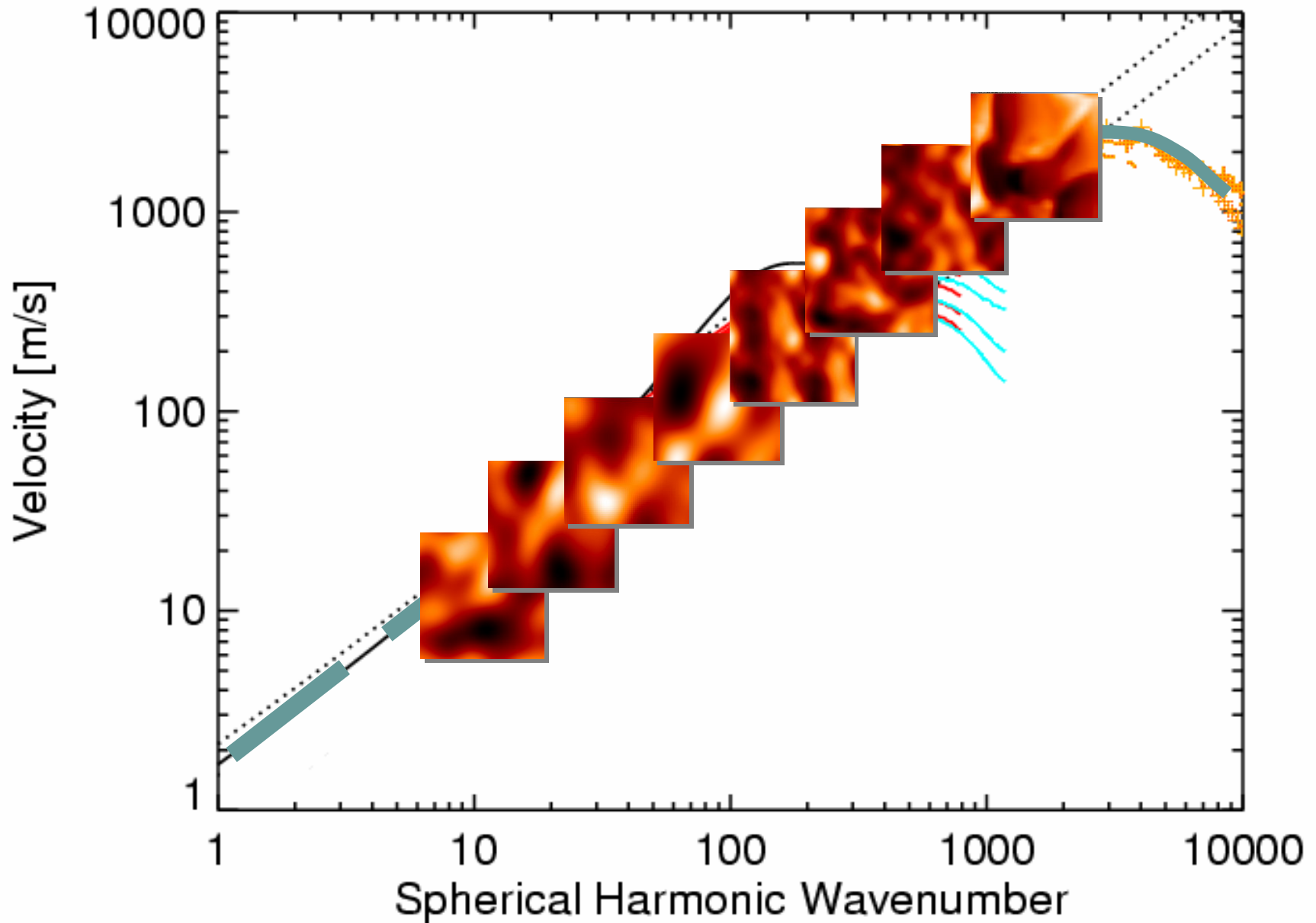
# Accurate match; widths, shapes *and* shifts!



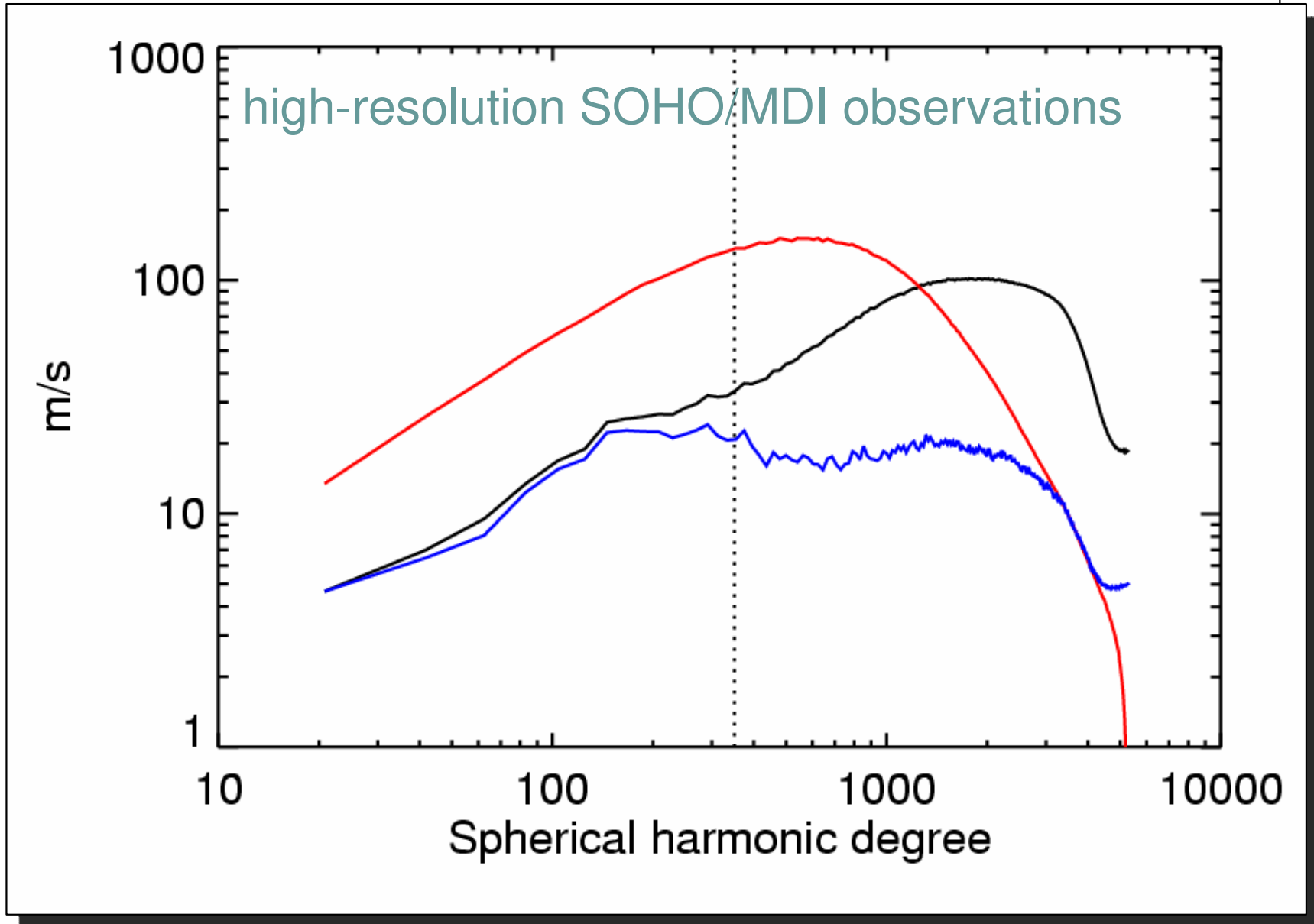
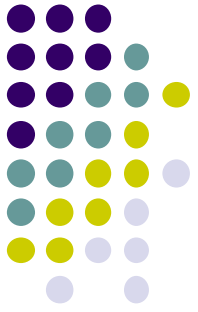
- **Requires** that both *temperature and velocity amplitudes are accurate!*
- **Proves** that dissipation is practically *identical at model and solar Reynolds numbers!*



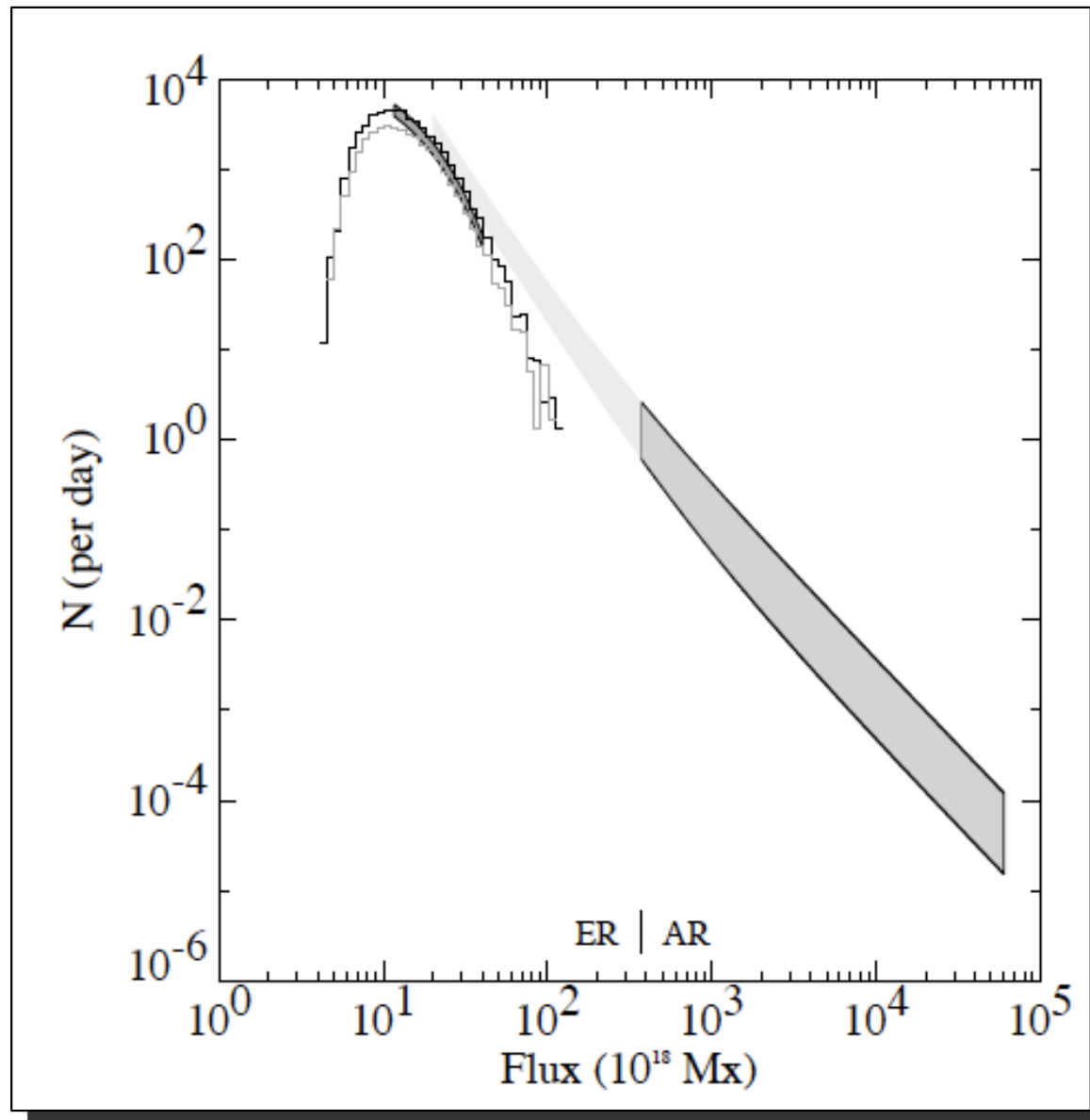
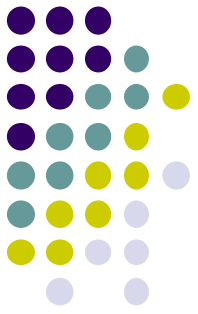
# Solar velocity spectrum – observations and simulations



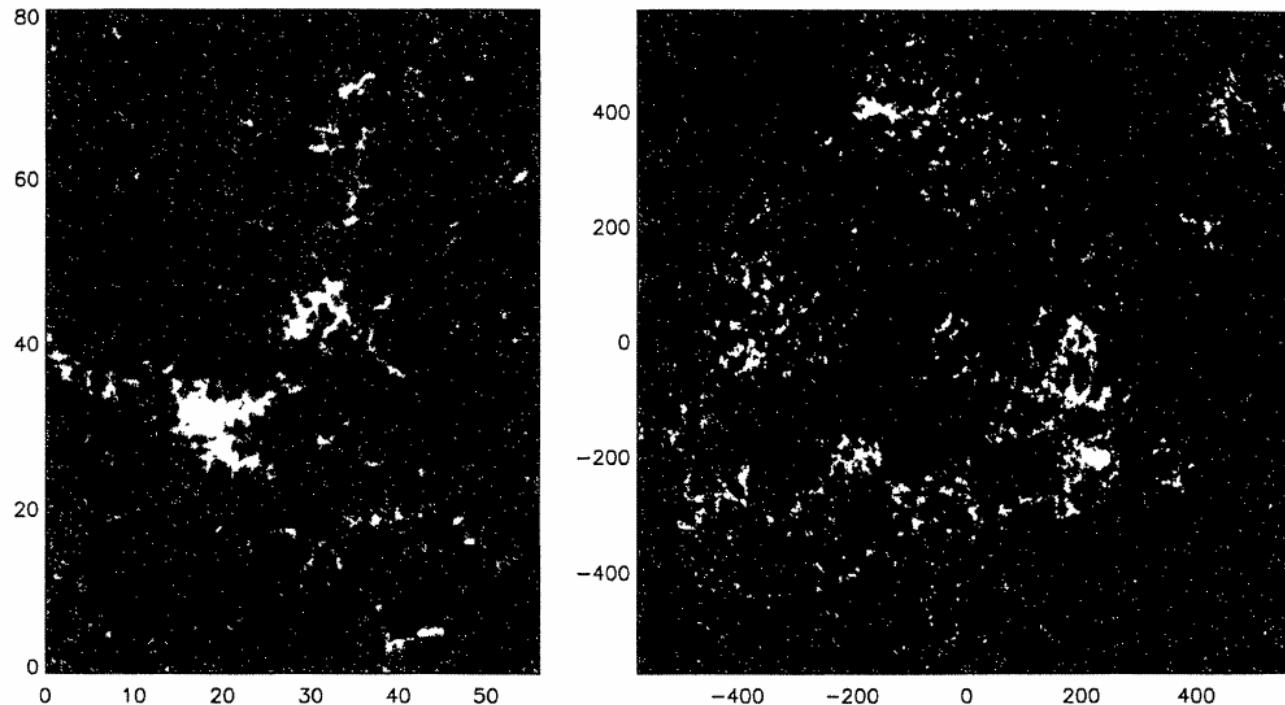
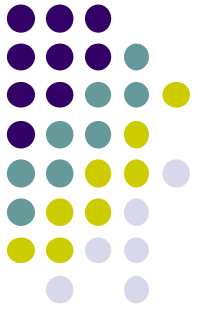
# oscillation power (red), convective power (black) – time average (blue)



# Near-scale free surface magnetic flux distribution



# Magnetic field patterns and distributions also show self-similarity



*Figure 1. Illustration of pattern self-similarity over a large dynamic range. The La Palma high-resolution magnetogram (left panel), obtained on 9 February 1996, covers an area at the center of the quiet Sun that is only 0.35% of the area covered by the MDI magnetogram in the right panel, obtained on 20 March 2002. The spatial scale is given in arcsec. The grey scale cuts are identical for the two magnetograms: white represents +100 G, dark -100 G. Although the MDI magnetogram contains many active regions with sunspots, both the morphology and field-strength distribution are similar in the two magnetograms.*

# Magnetic field patterns and distributions also show self-similarity

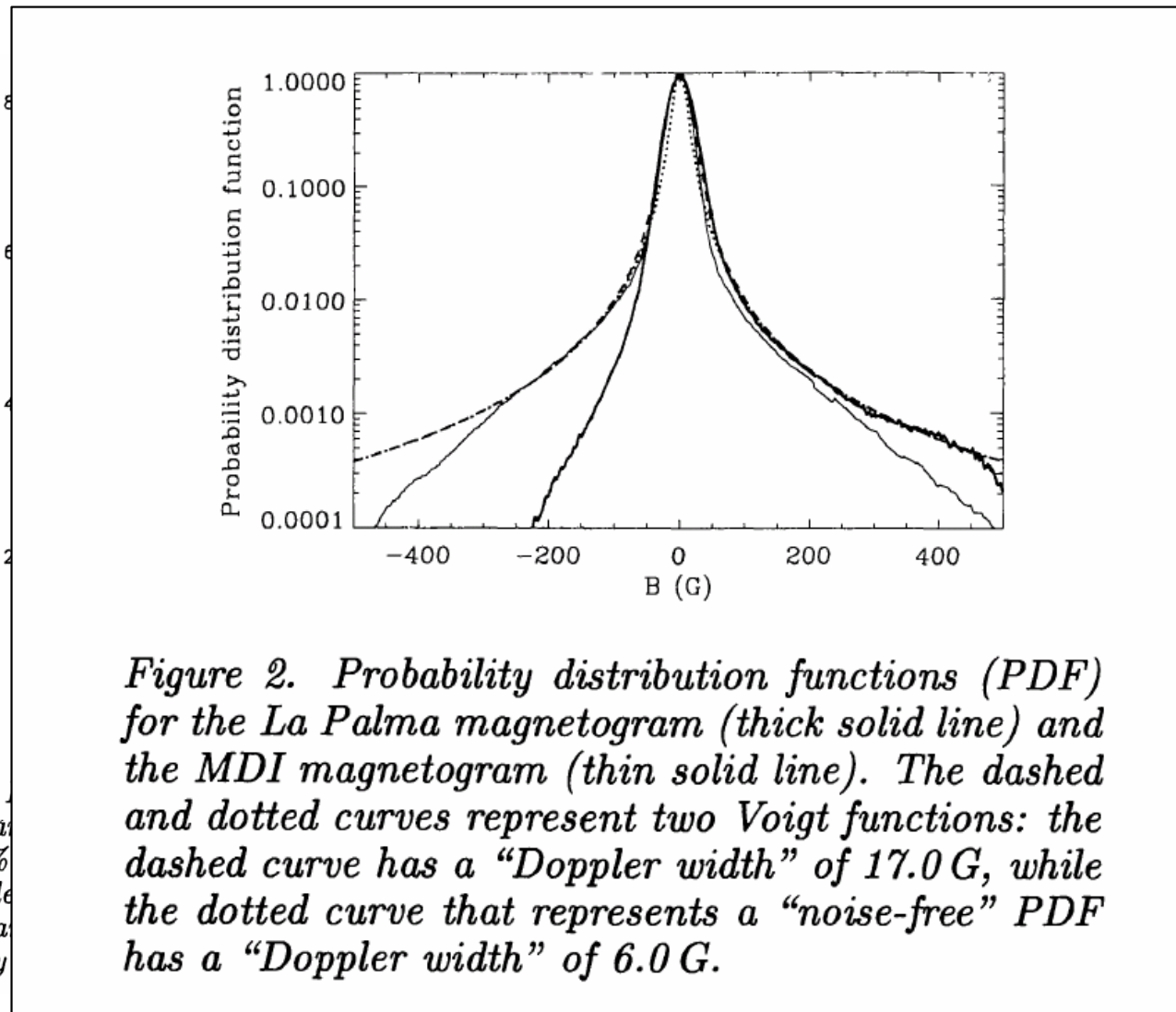
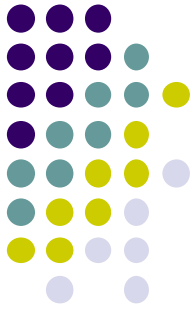
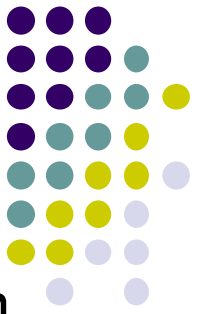


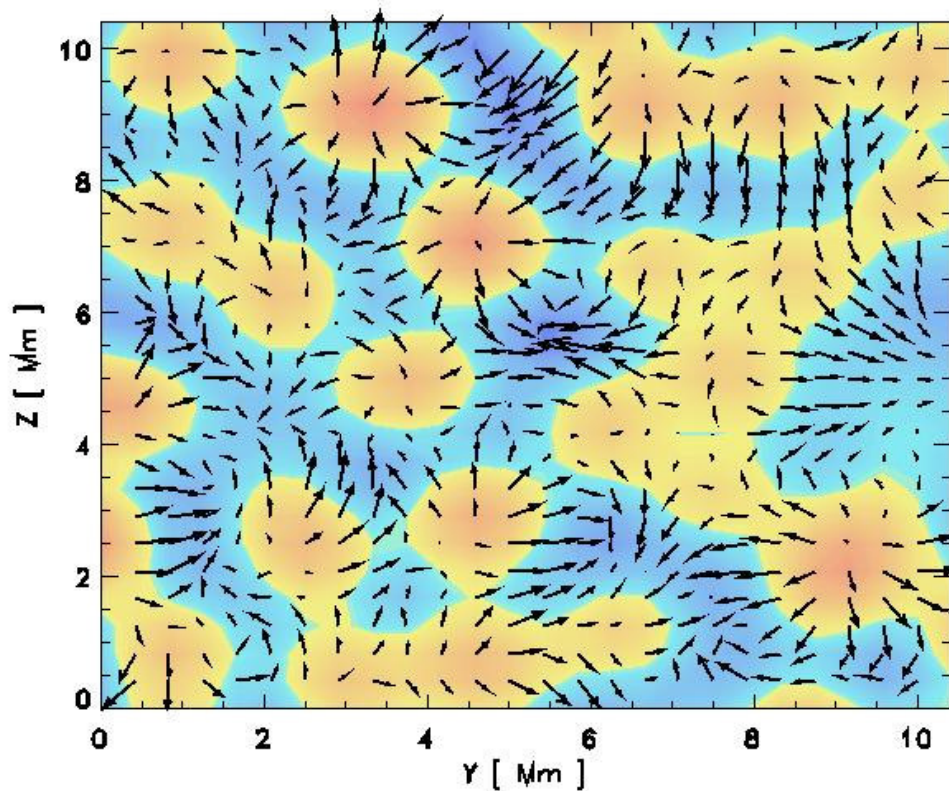
Figure 1. Magnetogram showing only 0.35% spatial scale +100 G, data morphology

High-resolution Sun that is 2002. The represents both the

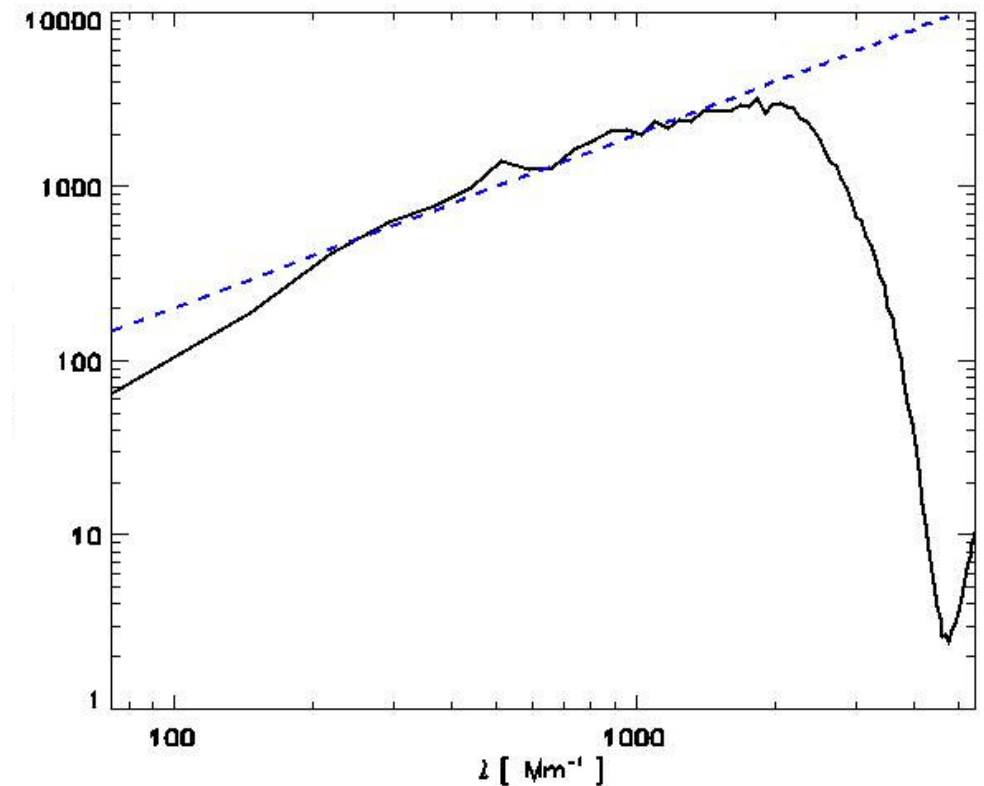
# Velocity driving for the corona



Voronoi tessellation  
ensemble

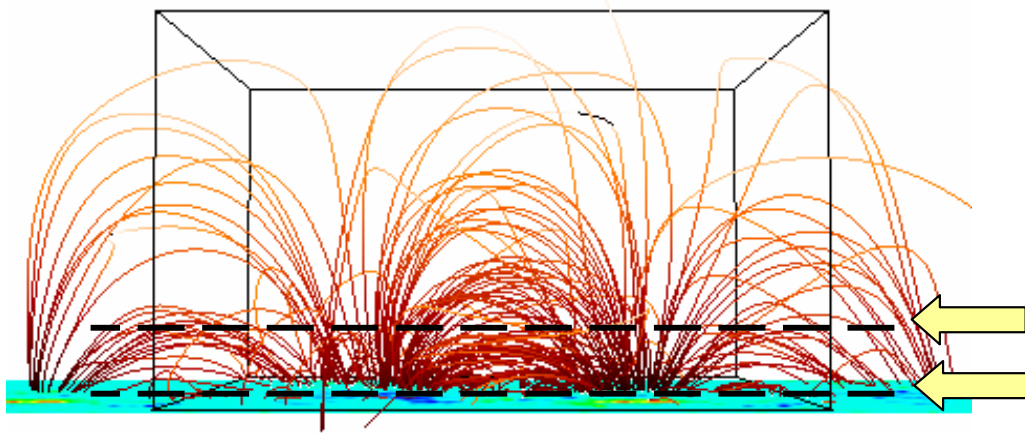
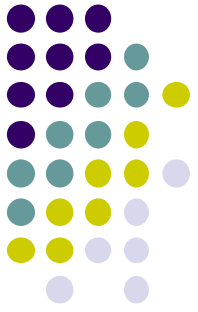


Velocity spectrum from  
three superposed ensembles





# Coronal heating



B: 4.5 Mm

A: 0.3 Mm

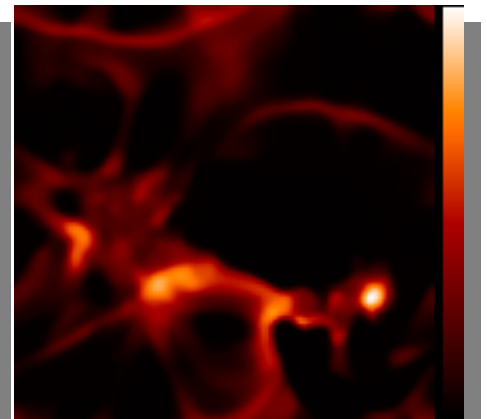
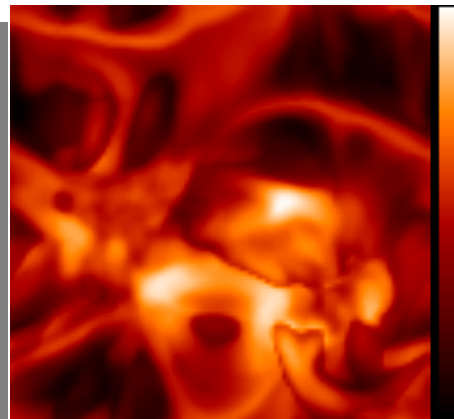
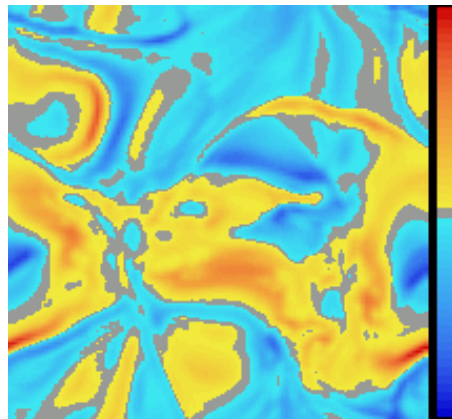
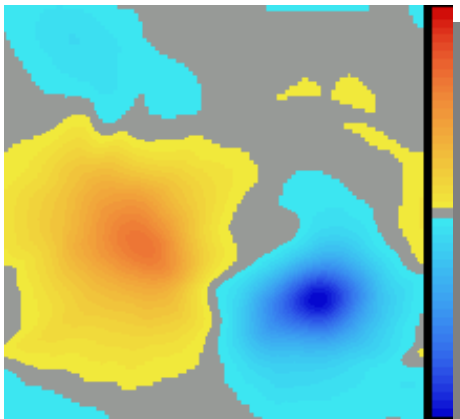
$B_{\text{vertical}}$

$\alpha$

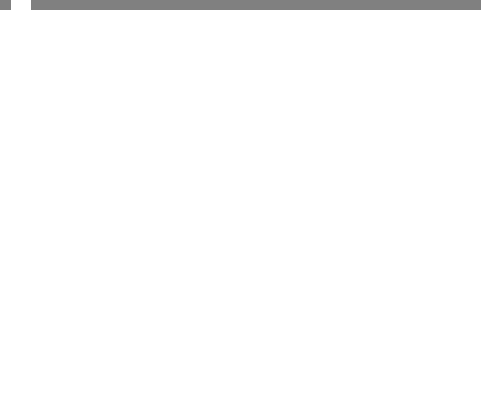
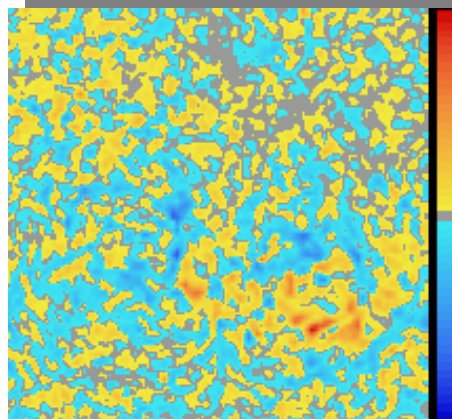
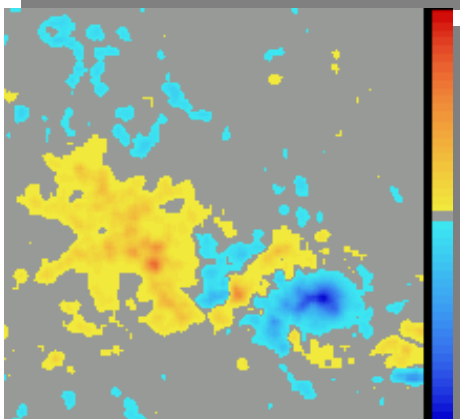
$\log(P_g)$

Temperature

B

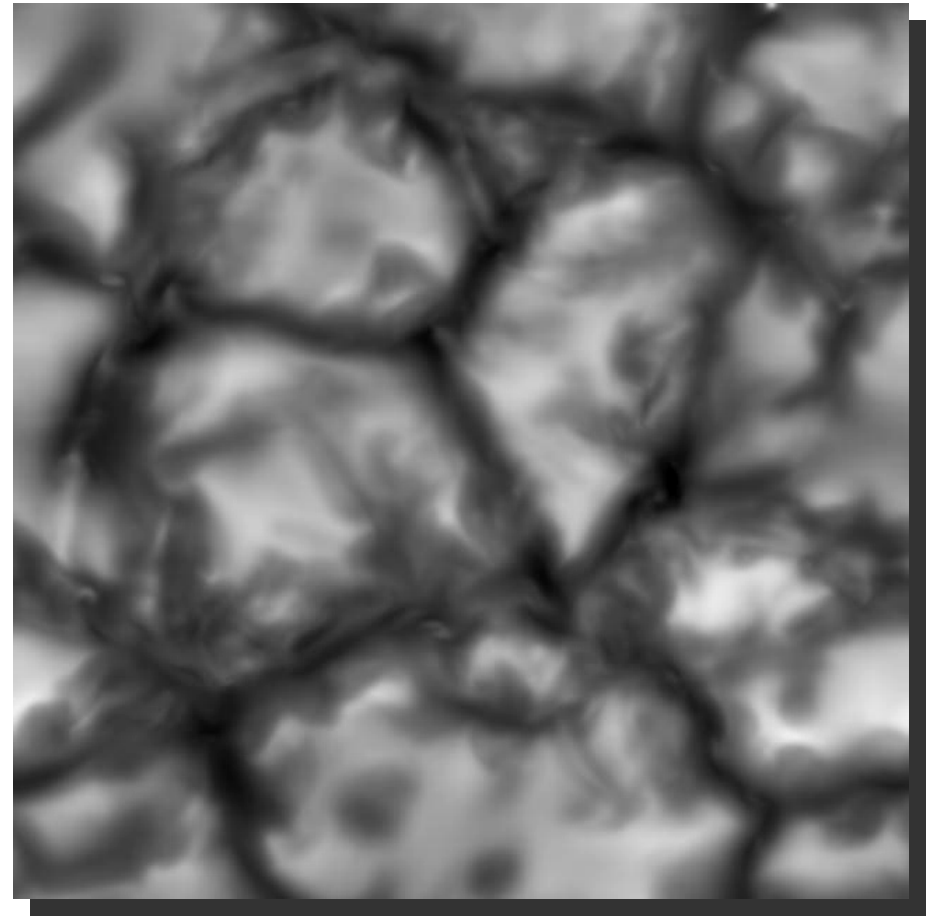
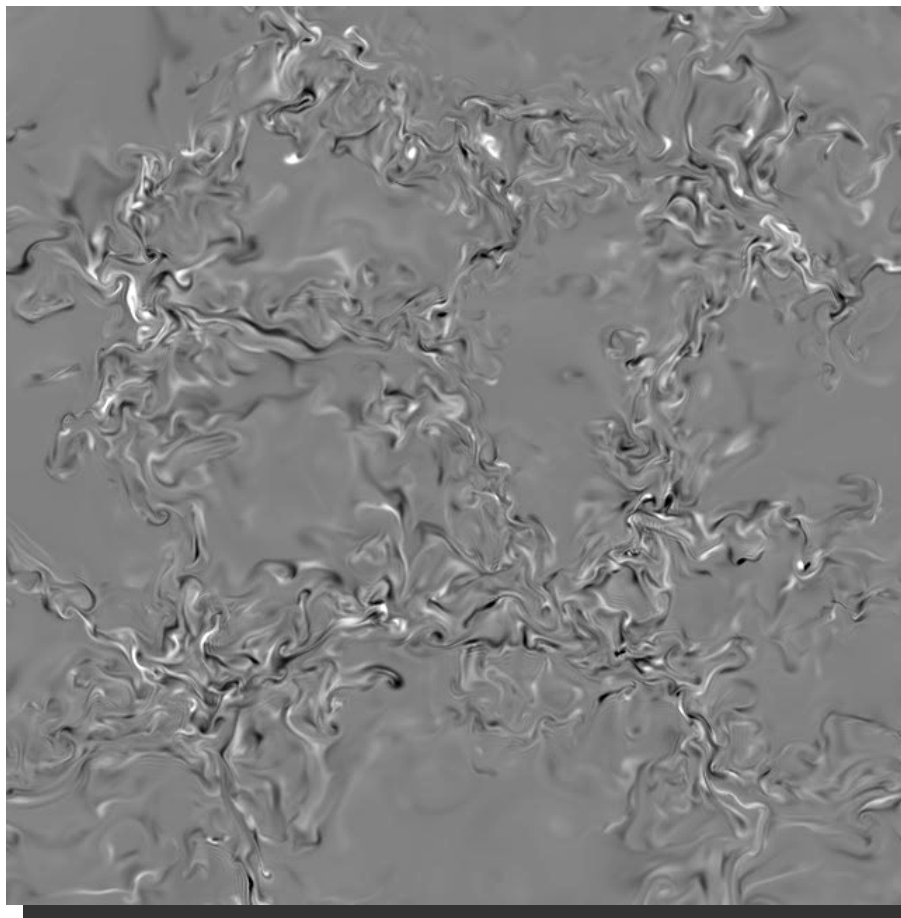
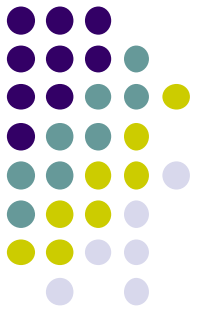


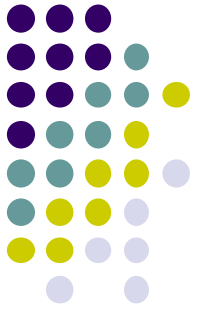
A



# Local dynamo action in surface convection

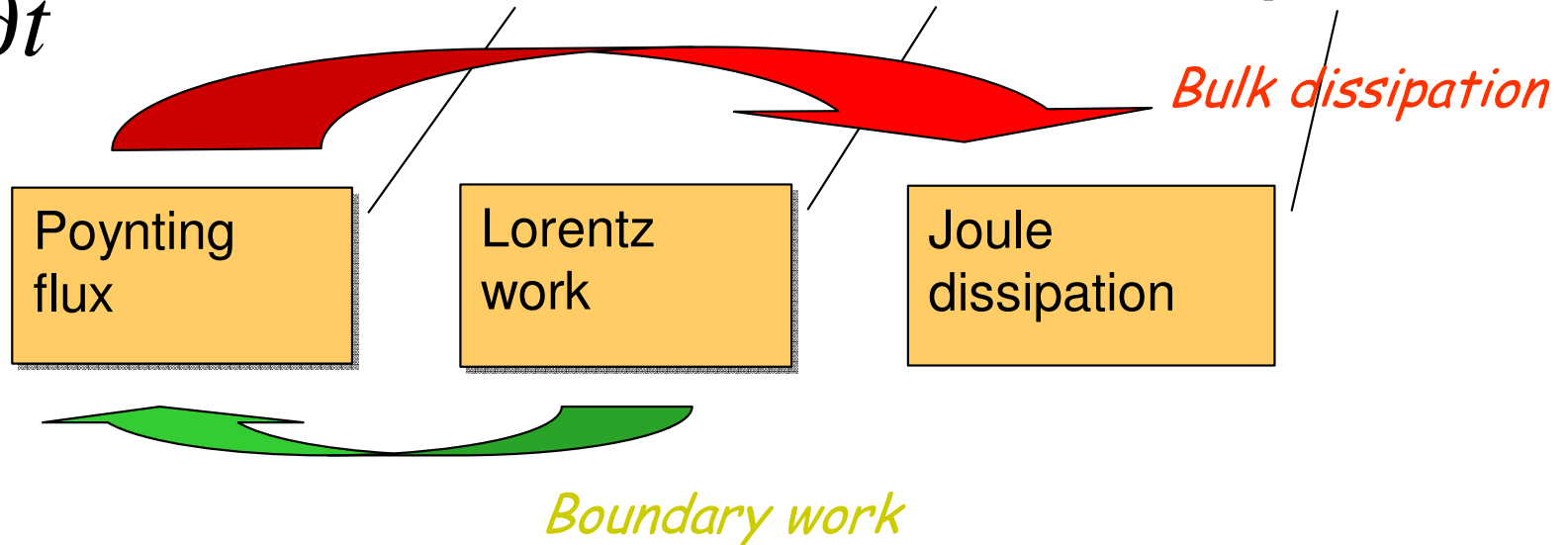
*(Vögler & Schüssler, 2007)*





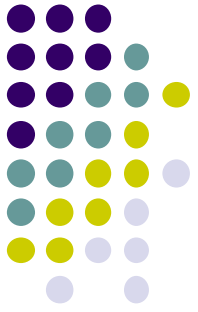
# Magnetic energy equation

$$\frac{\partial E_B}{\partial t} = -\nabla \cdot (\mathbf{E} \times \mathbf{B}) - \mathbf{u} \cdot (\mathbf{J} \times \mathbf{B}) - \eta J^2$$

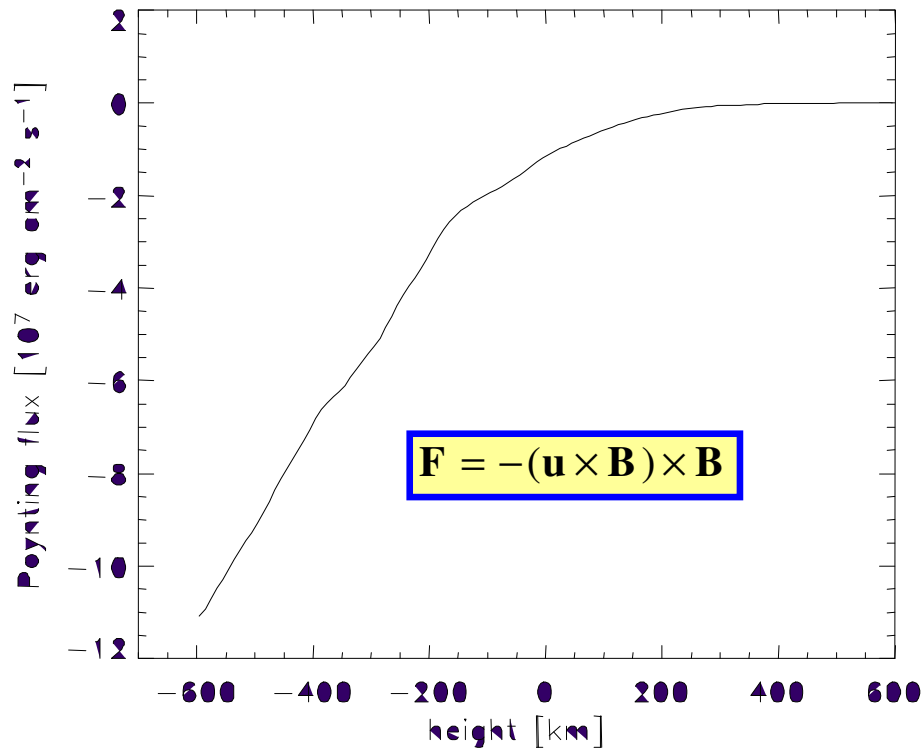


- Poynting flux: energy input; e.g. boundary work
- Lorentz work: drives, supports energy dissipation
- Joule dissipation: supports radiative losses

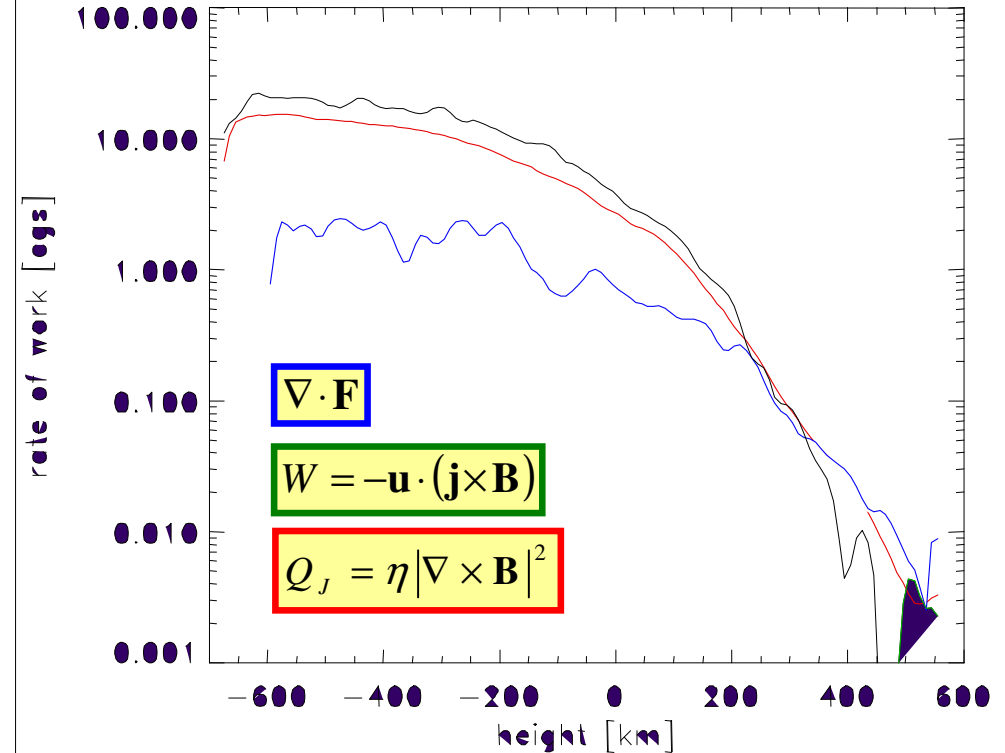
# Distributed dynamo action



Poynting Flux



Energy Balance



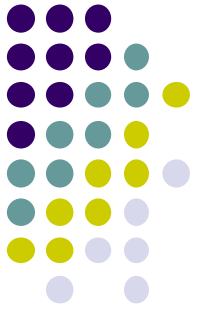
Negative Poynting flux

$$\nabla \cdot \mathbf{F} / (W - Q_J) \approx 0.8$$

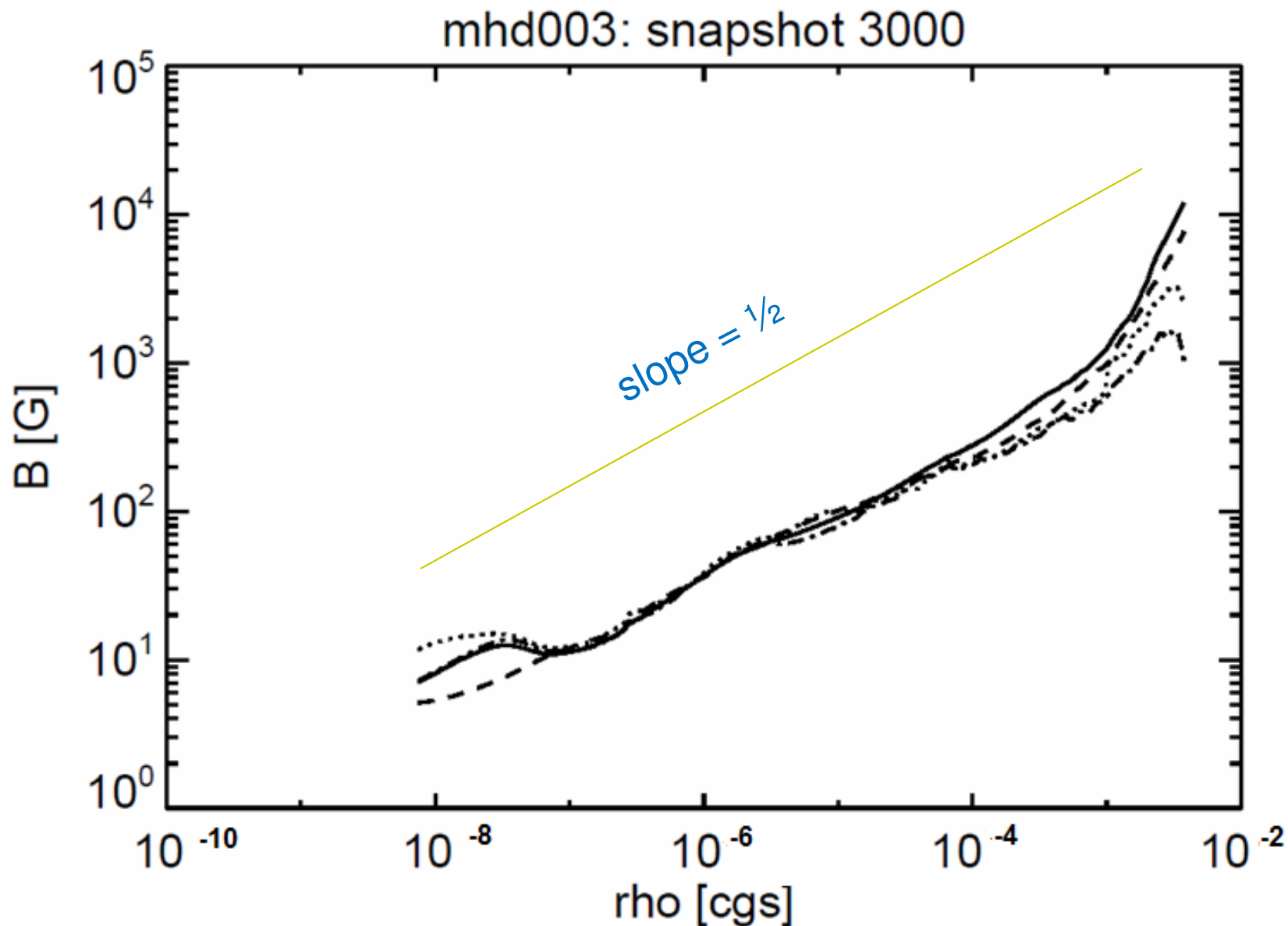
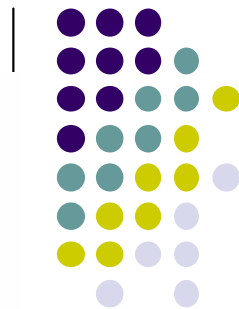
→ Convective pumping into deeper layers

→ large part of net energy input lost due to downward pumping

# Generalize this!

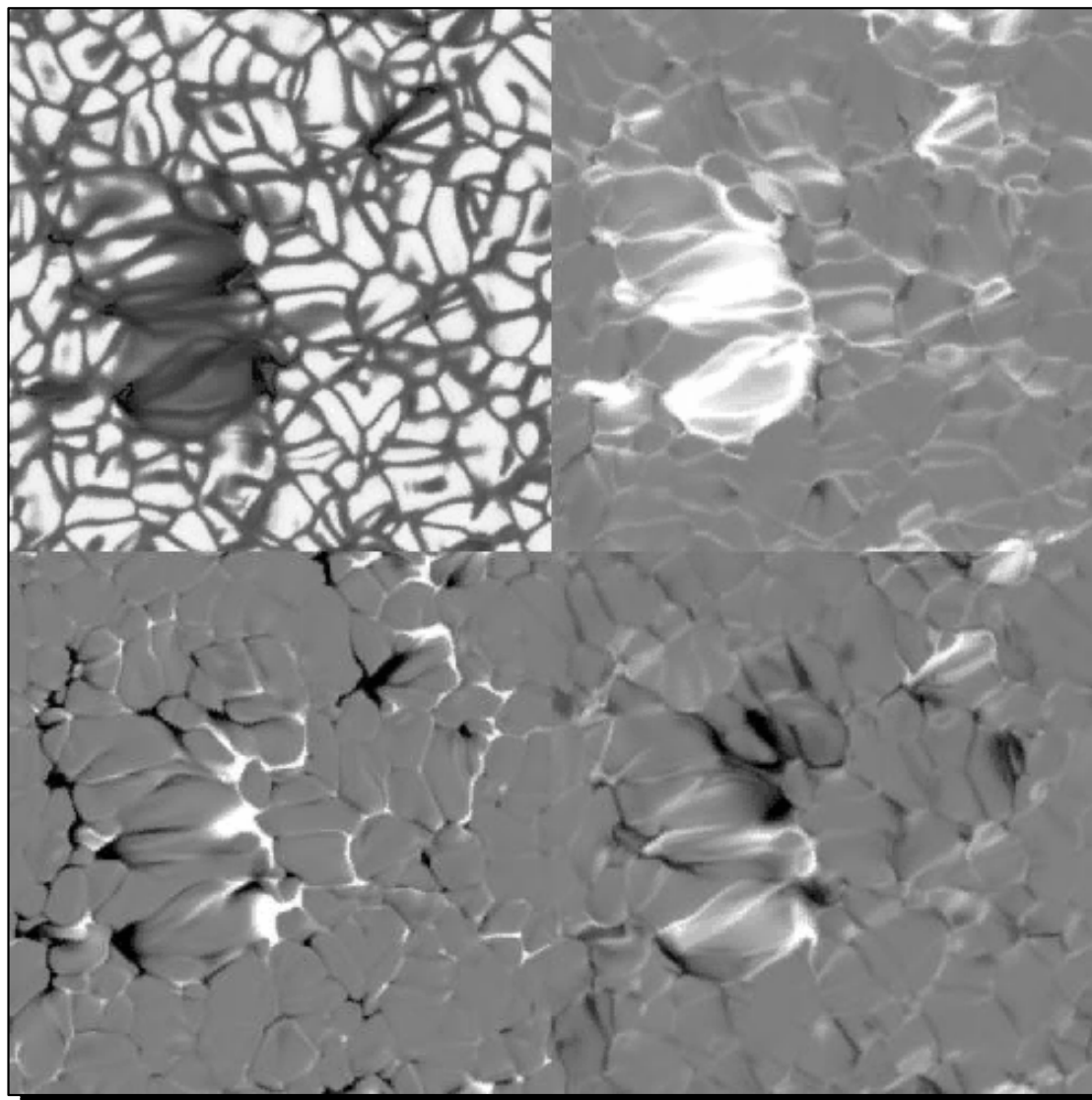


- Likely that there is net small scale dynamo action at each depth in the CZ!
  - Net magnetic energy delivered to the next layer
- On the largest scale = largest depths (and only there) differential rotation enables a large scale – global – dynamo action
  - With buoyancy eventually pushing the field back up



The scaling of average (full drawn) and fluctuating magnetic field components (x:dotted, y:dashed, z:dot-dashed) after 25 solar hours.

# 24x24x20 Mm magnetoconvection Horizontal boundary field



**Slide 31**

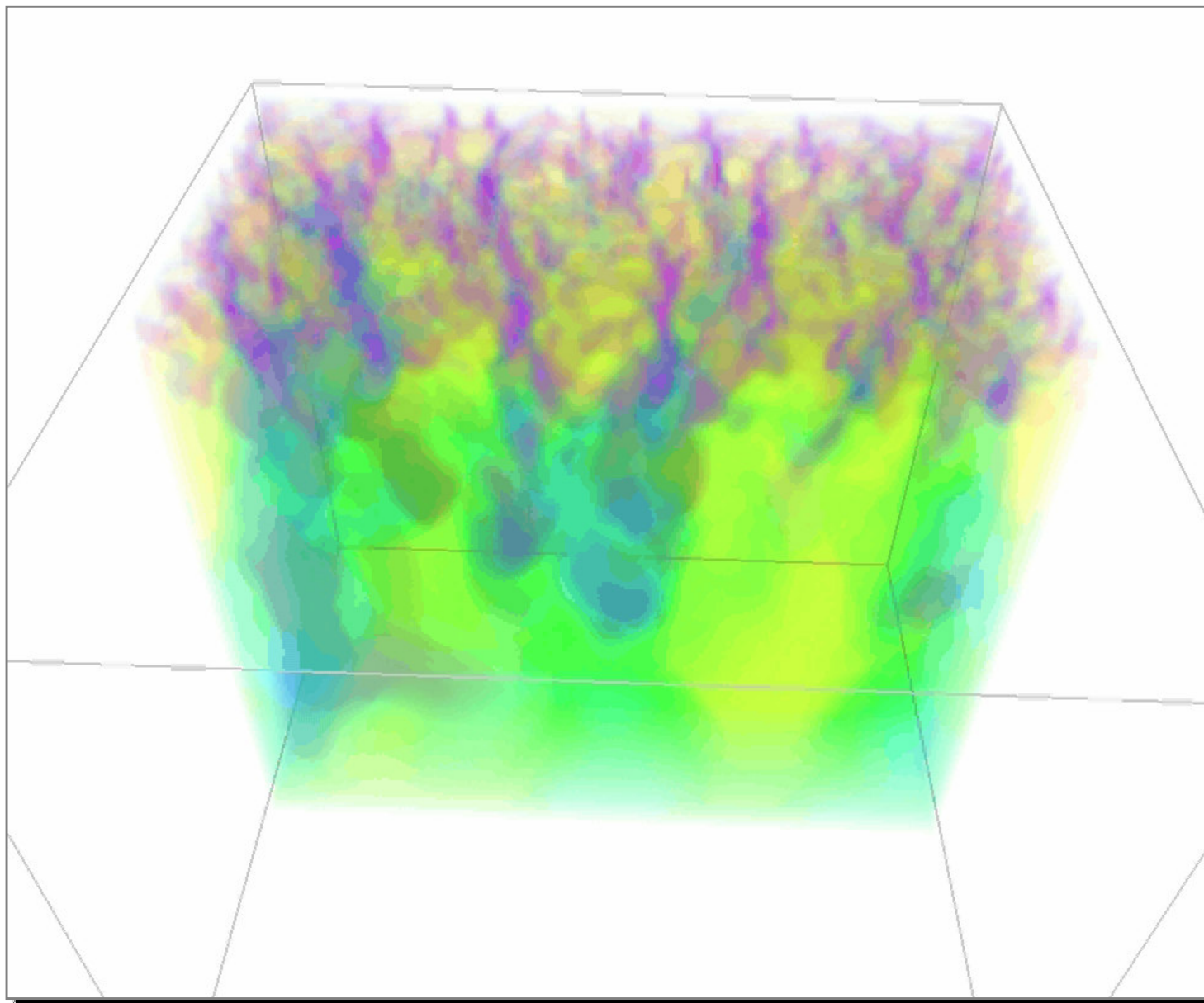
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**A2**

Aake, 6/22/2008



# Multi-scale convection; 24x24x20 Mm (cut-out)



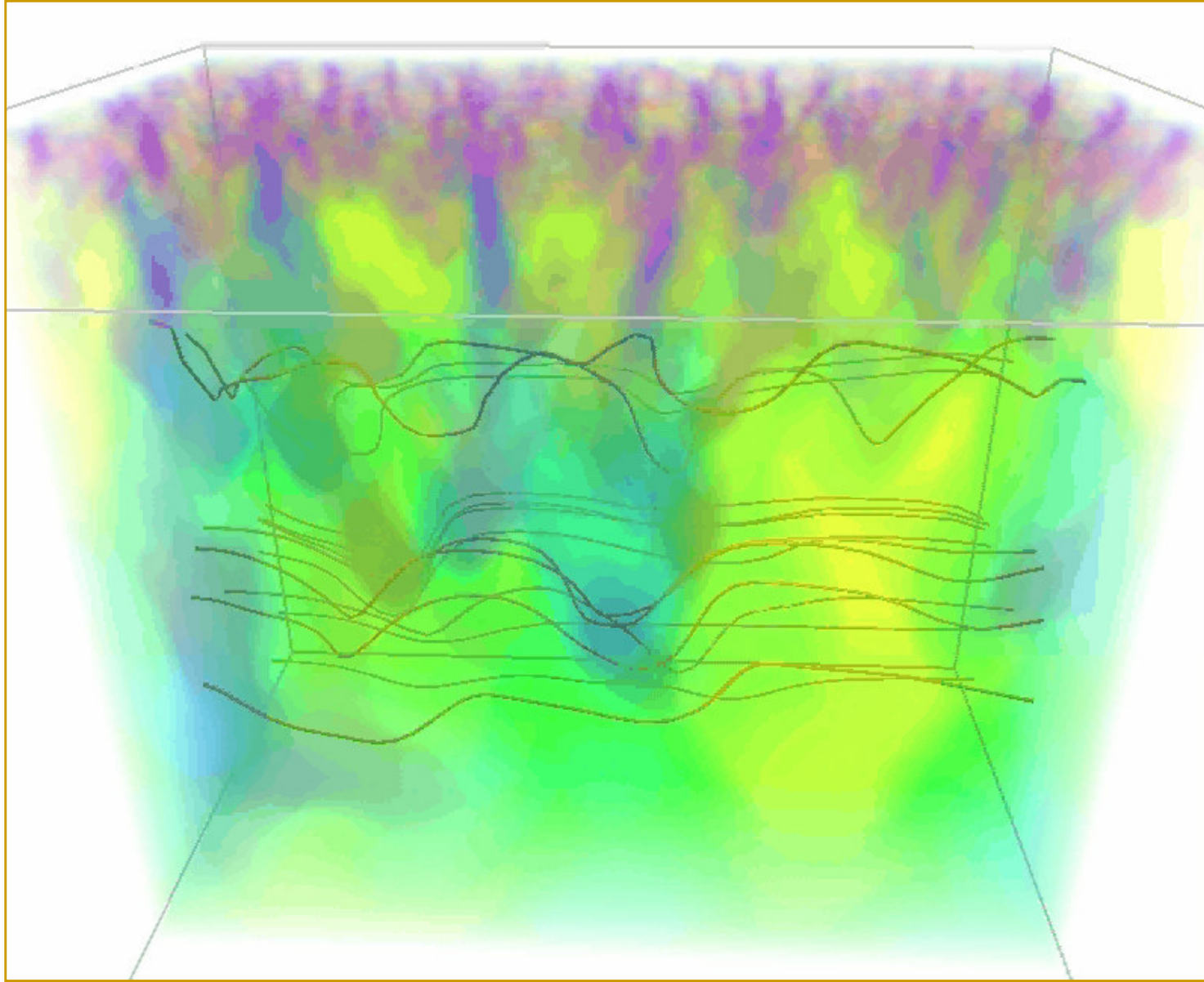
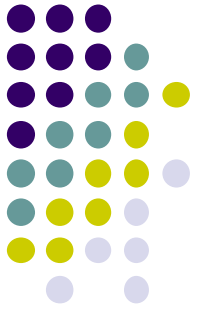
**Slide 32**

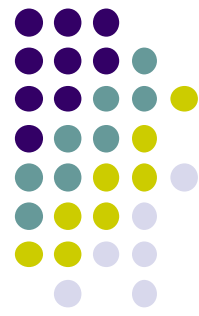
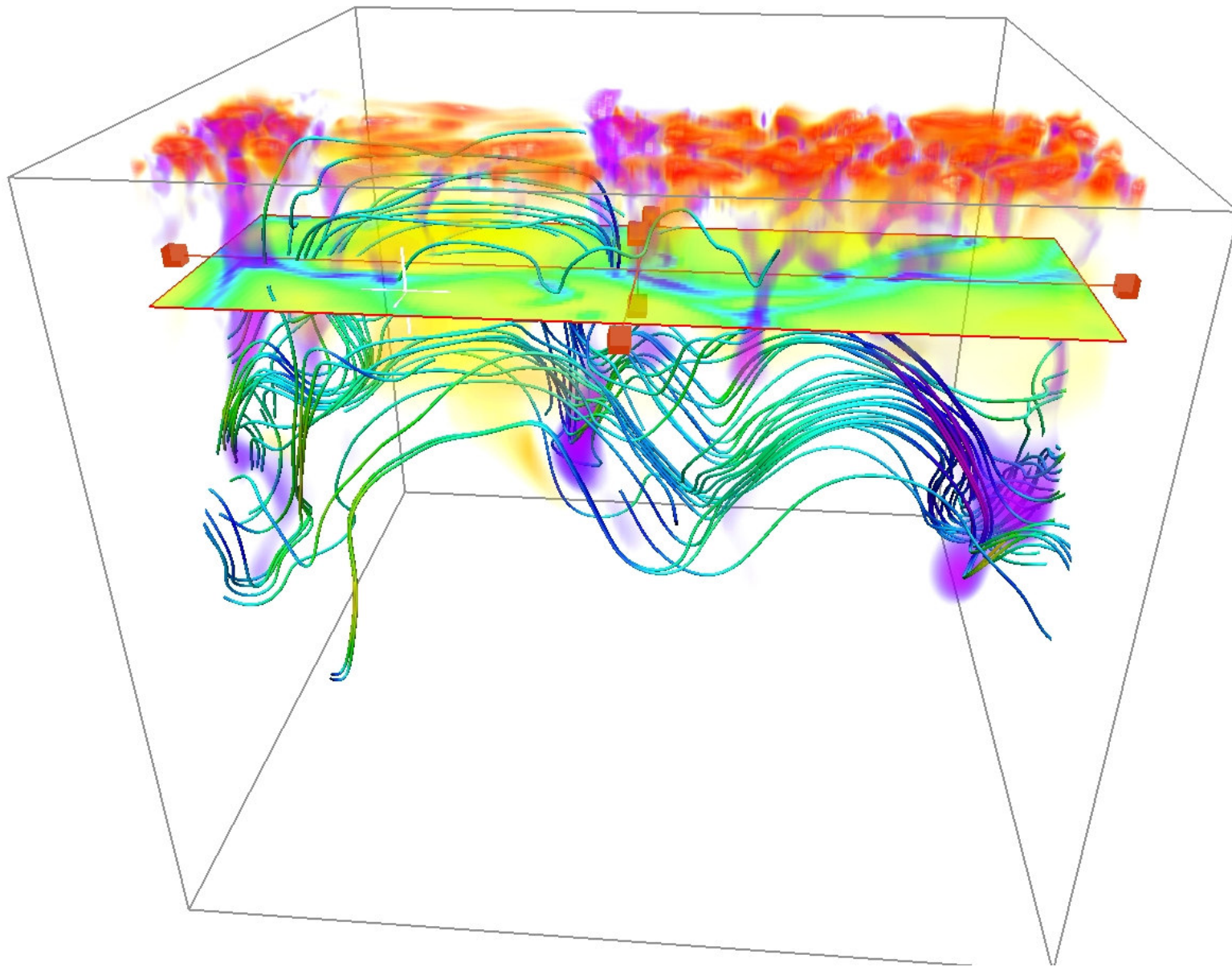
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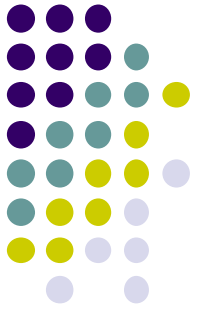
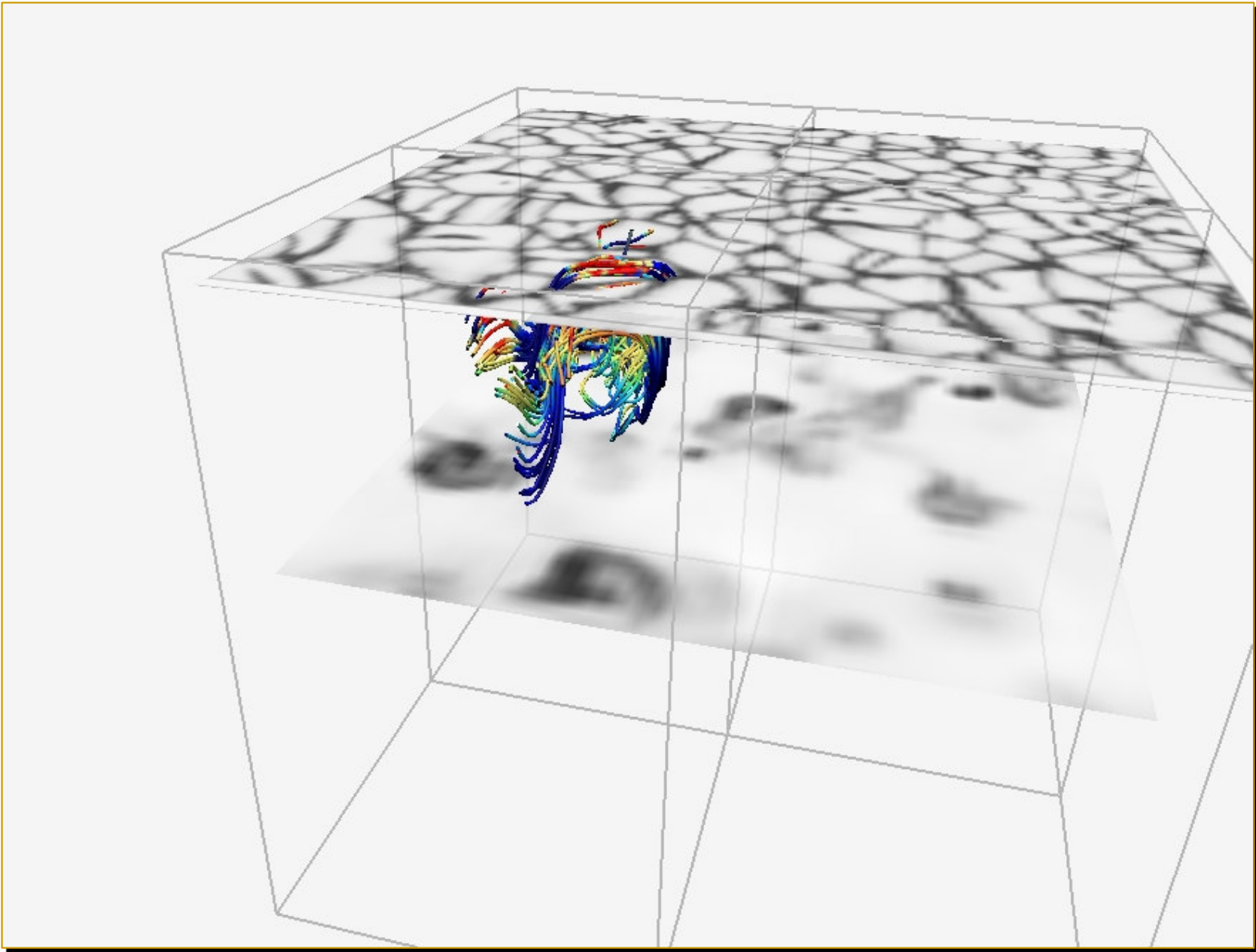
**A1**

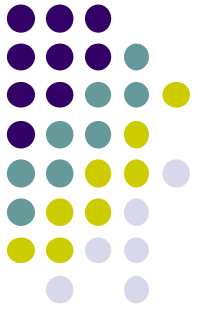
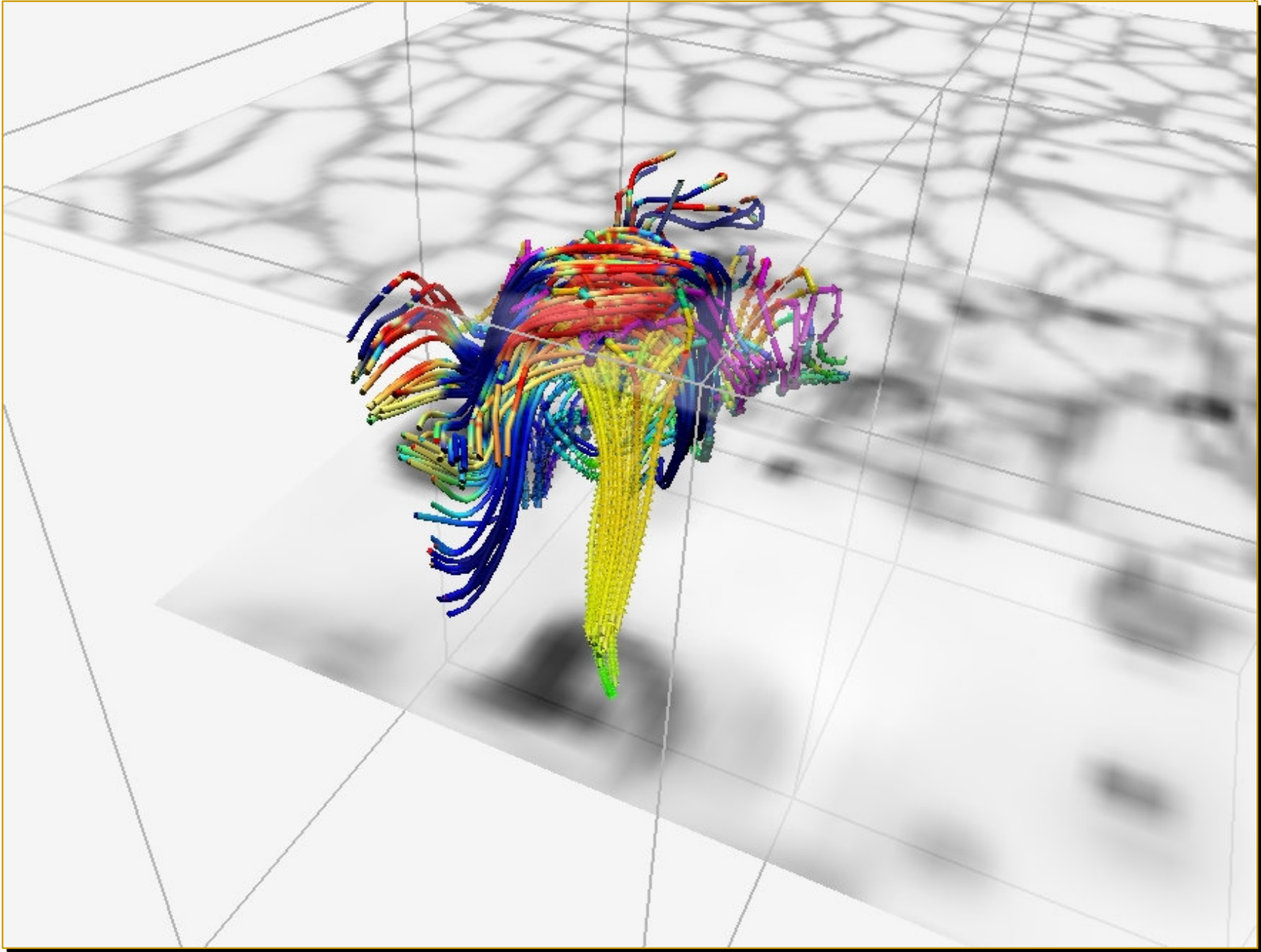
Aake, 6/22/2008

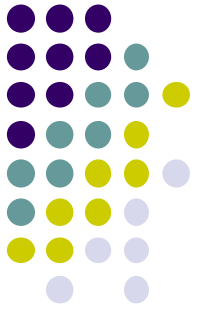
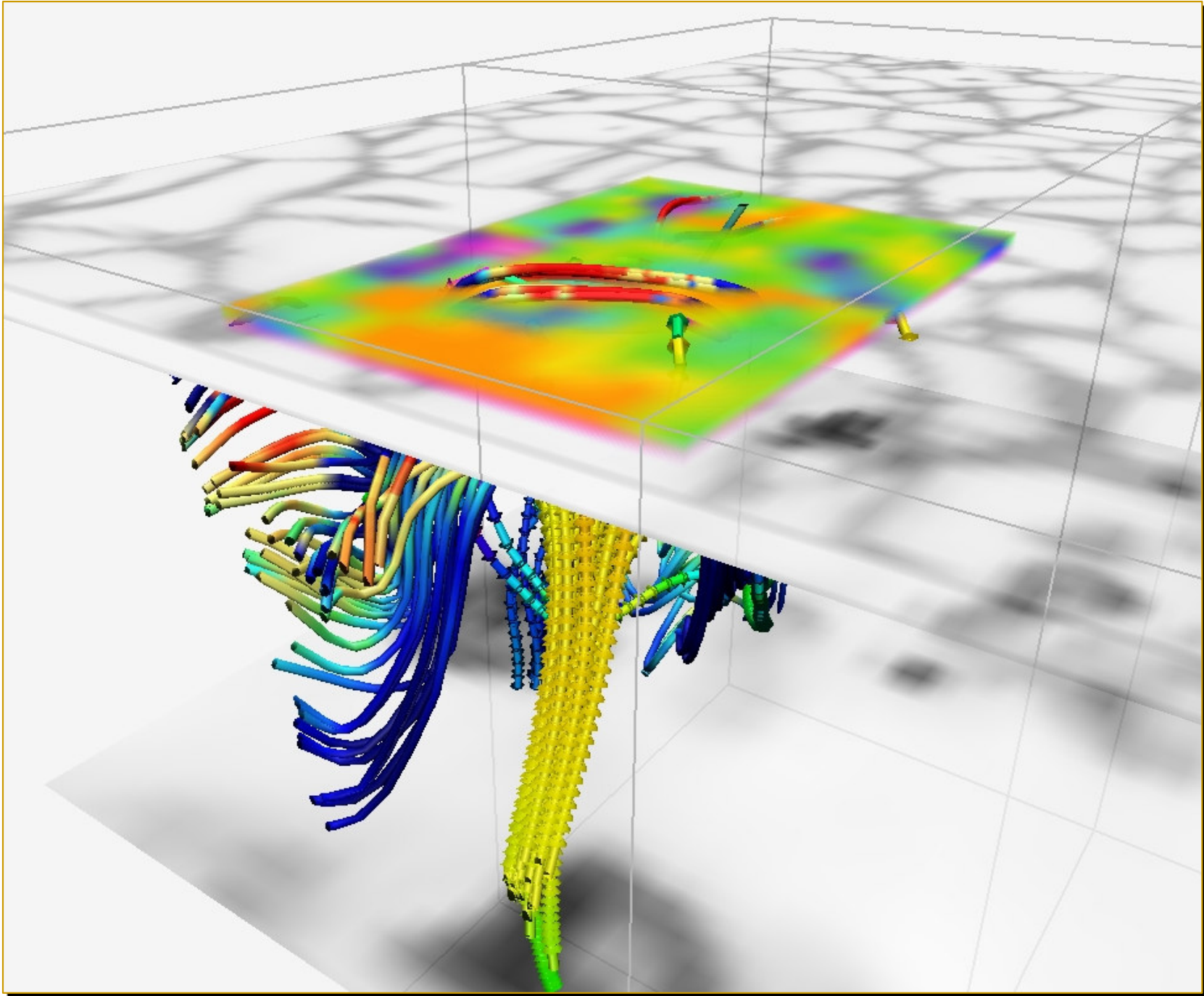
# Multi-scale magneto-convection; initially horizontal field

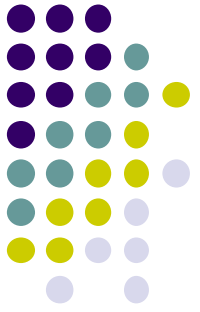
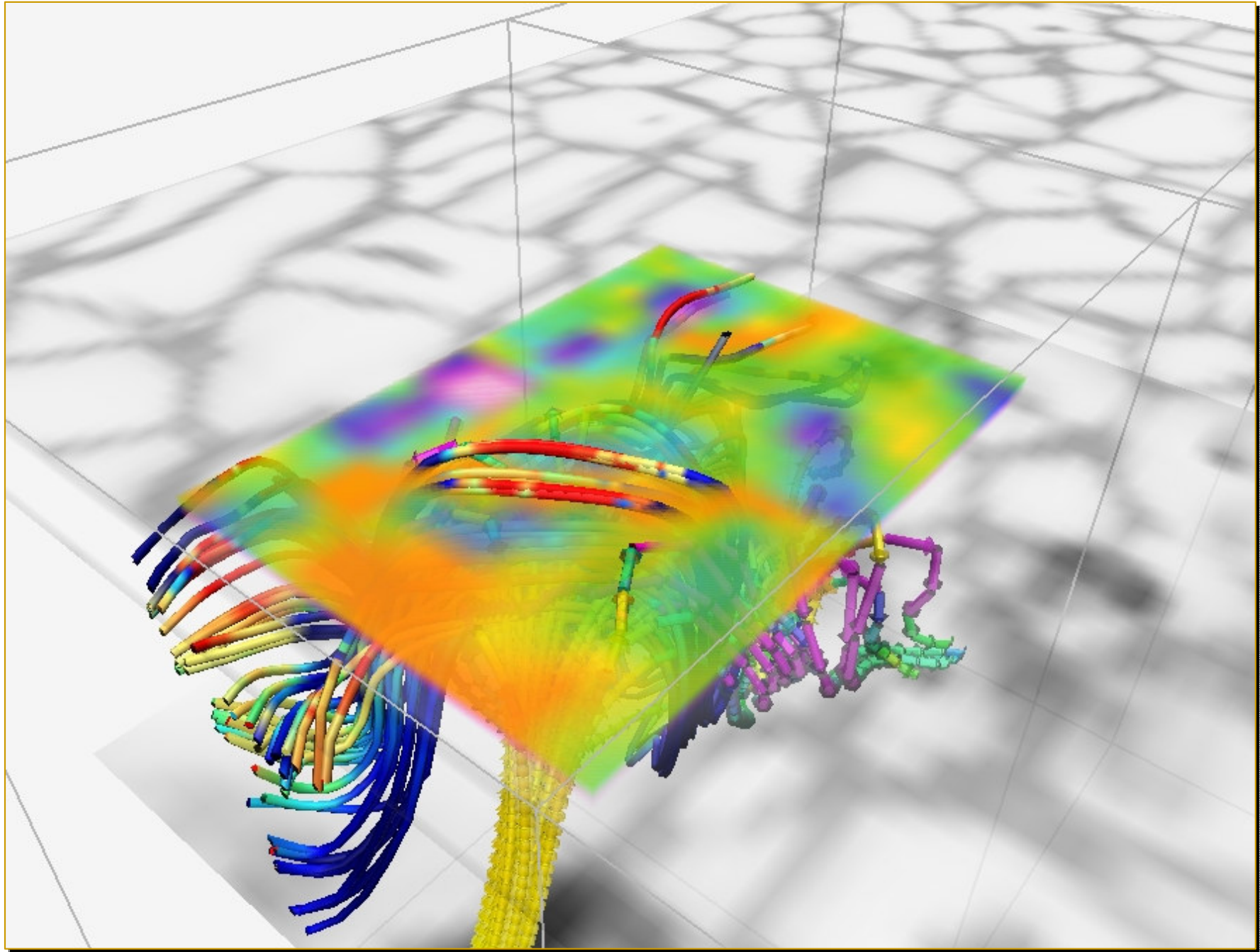




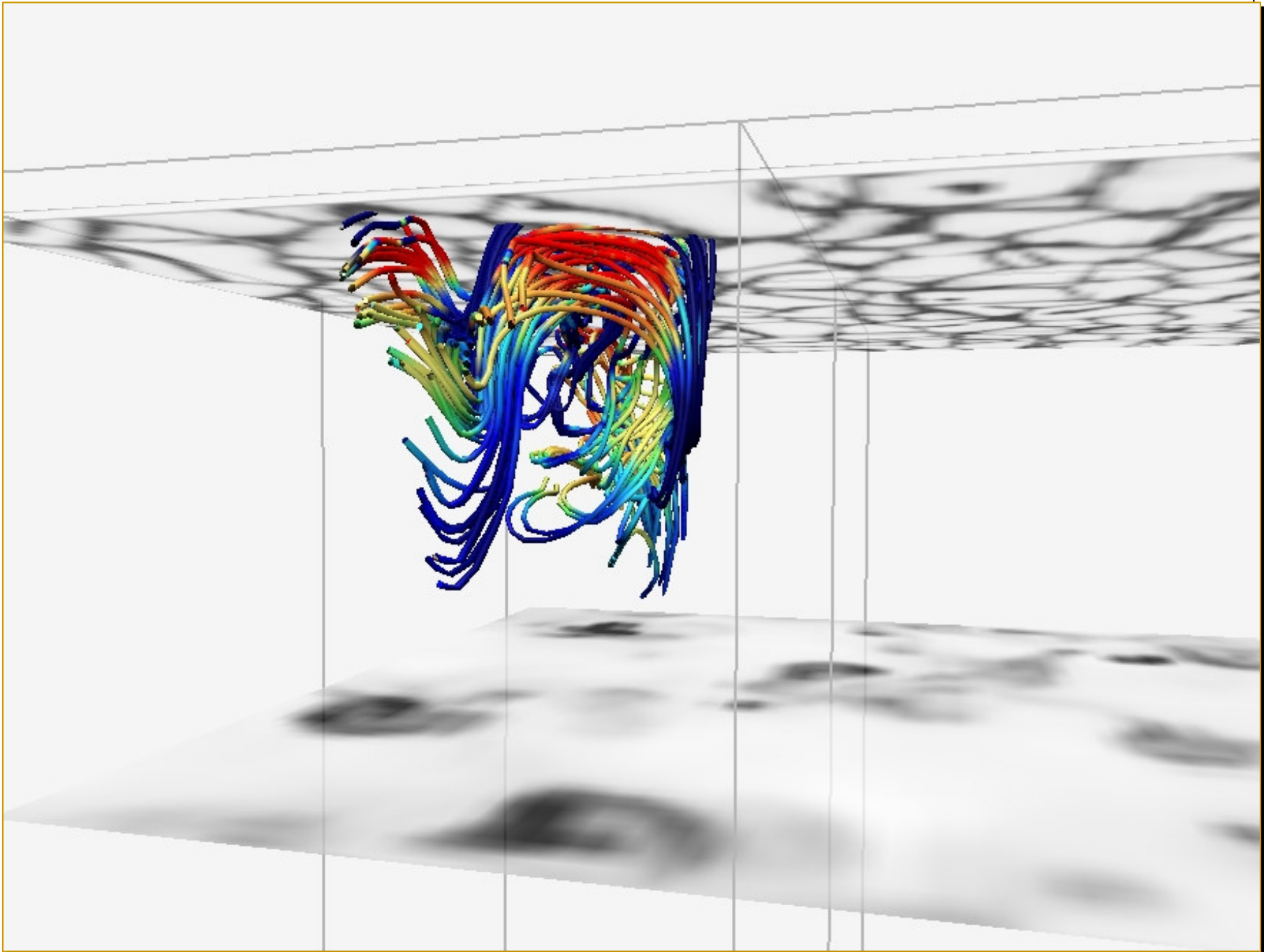
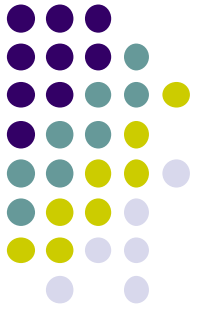




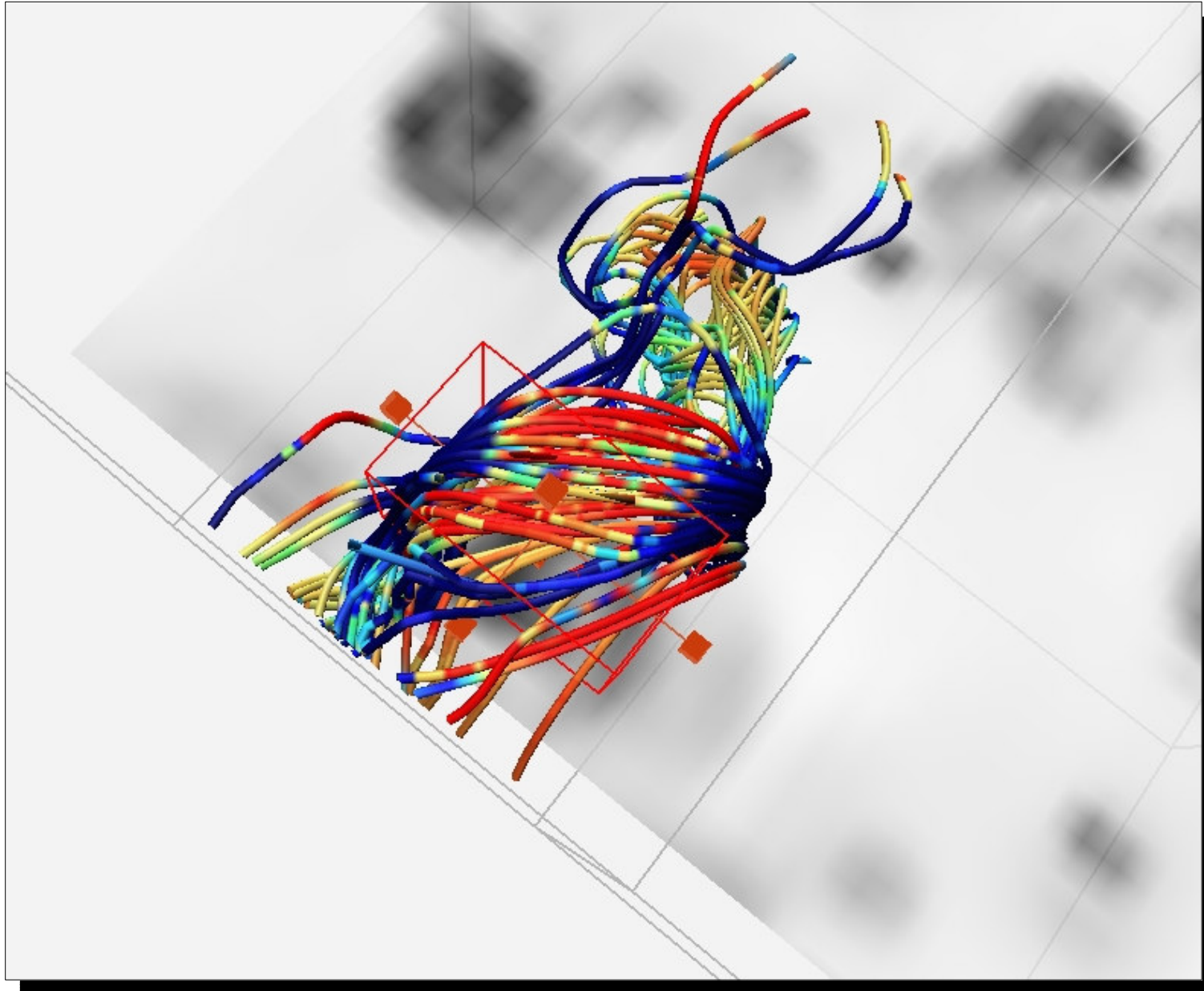
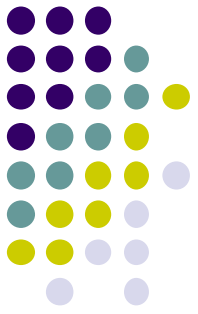




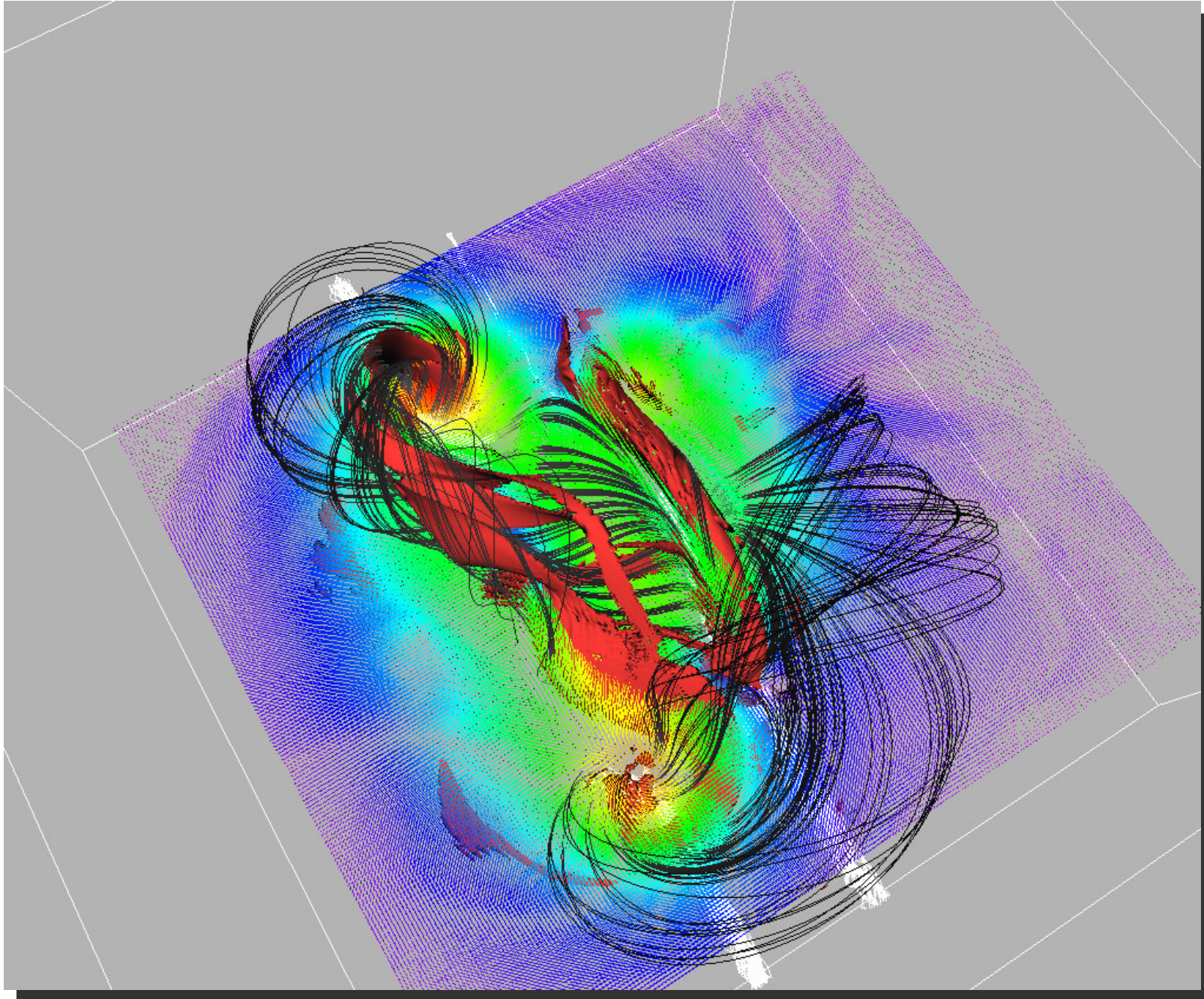
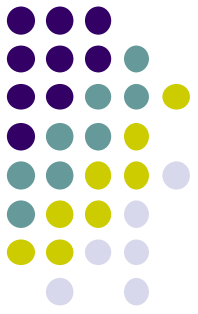




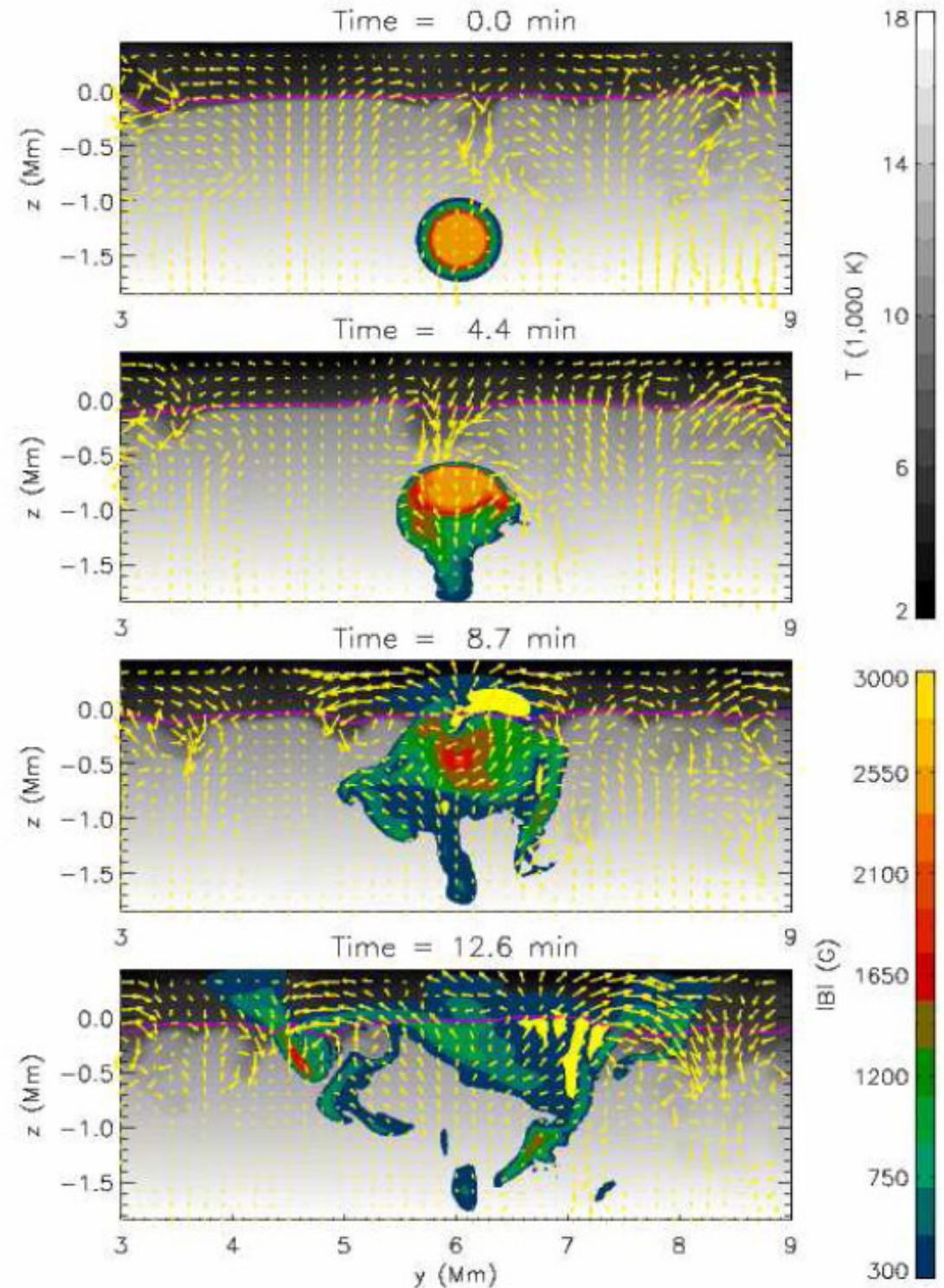
# View from above; sheared field lines



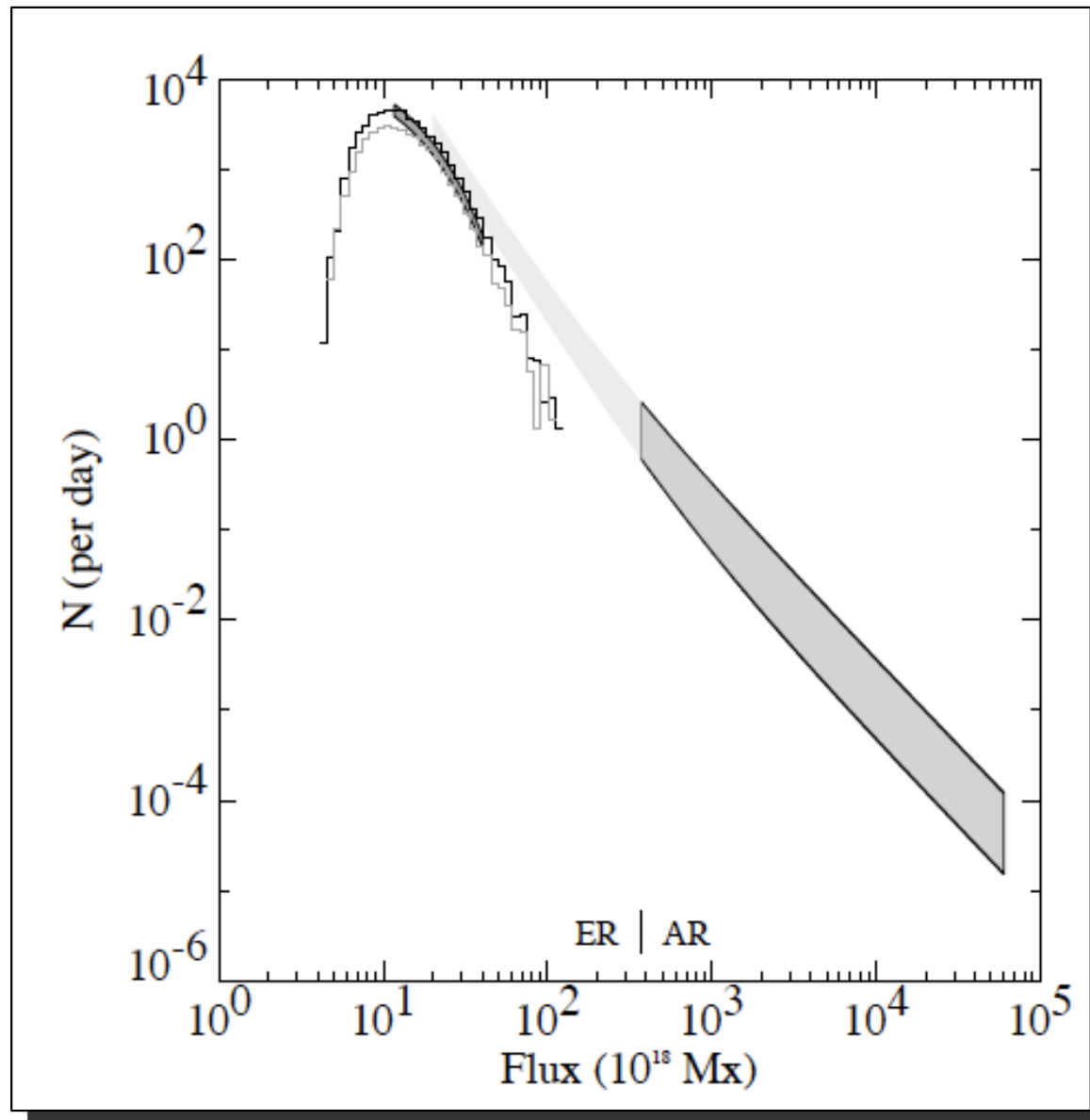
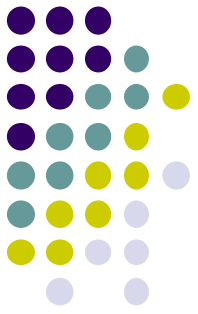
# St. Andrews' team; Archontis ..



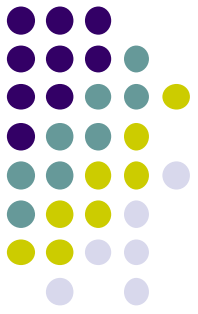
# ”Classical” emerging flux studies



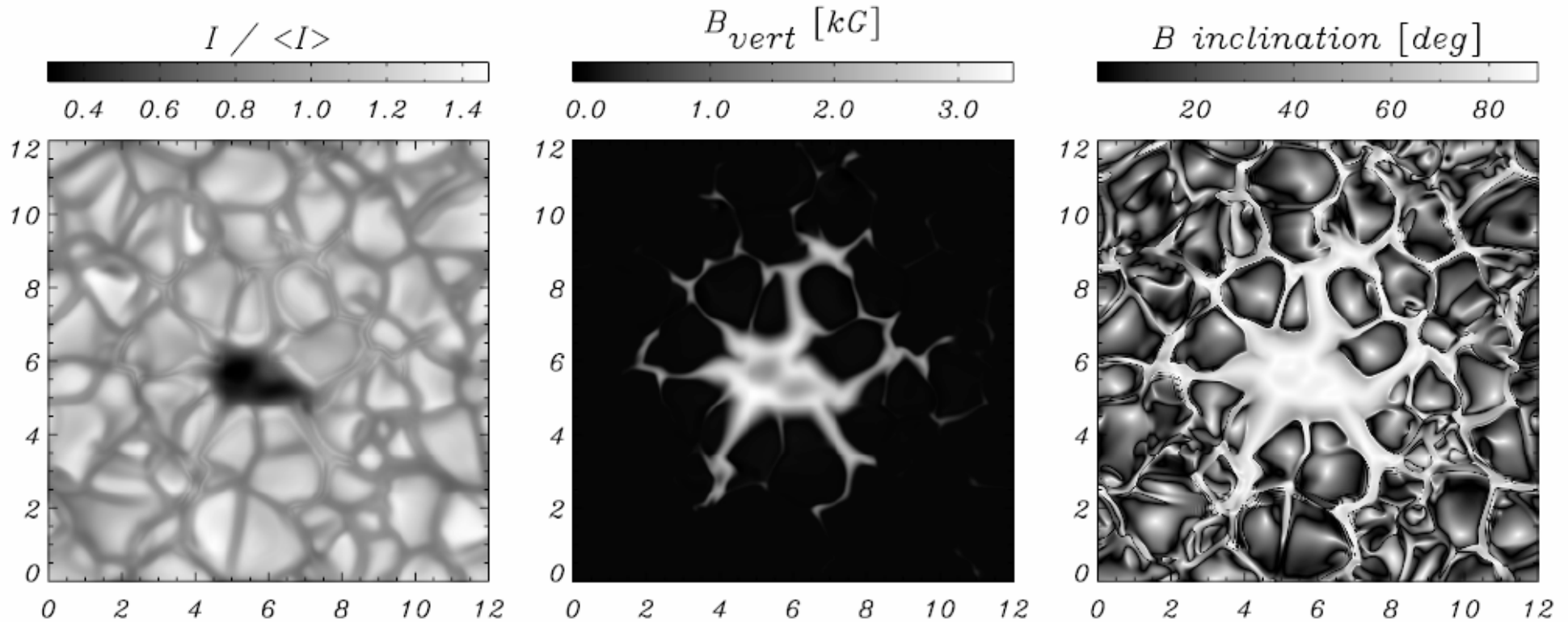
# Near-scale free surface magnetic flux distribution



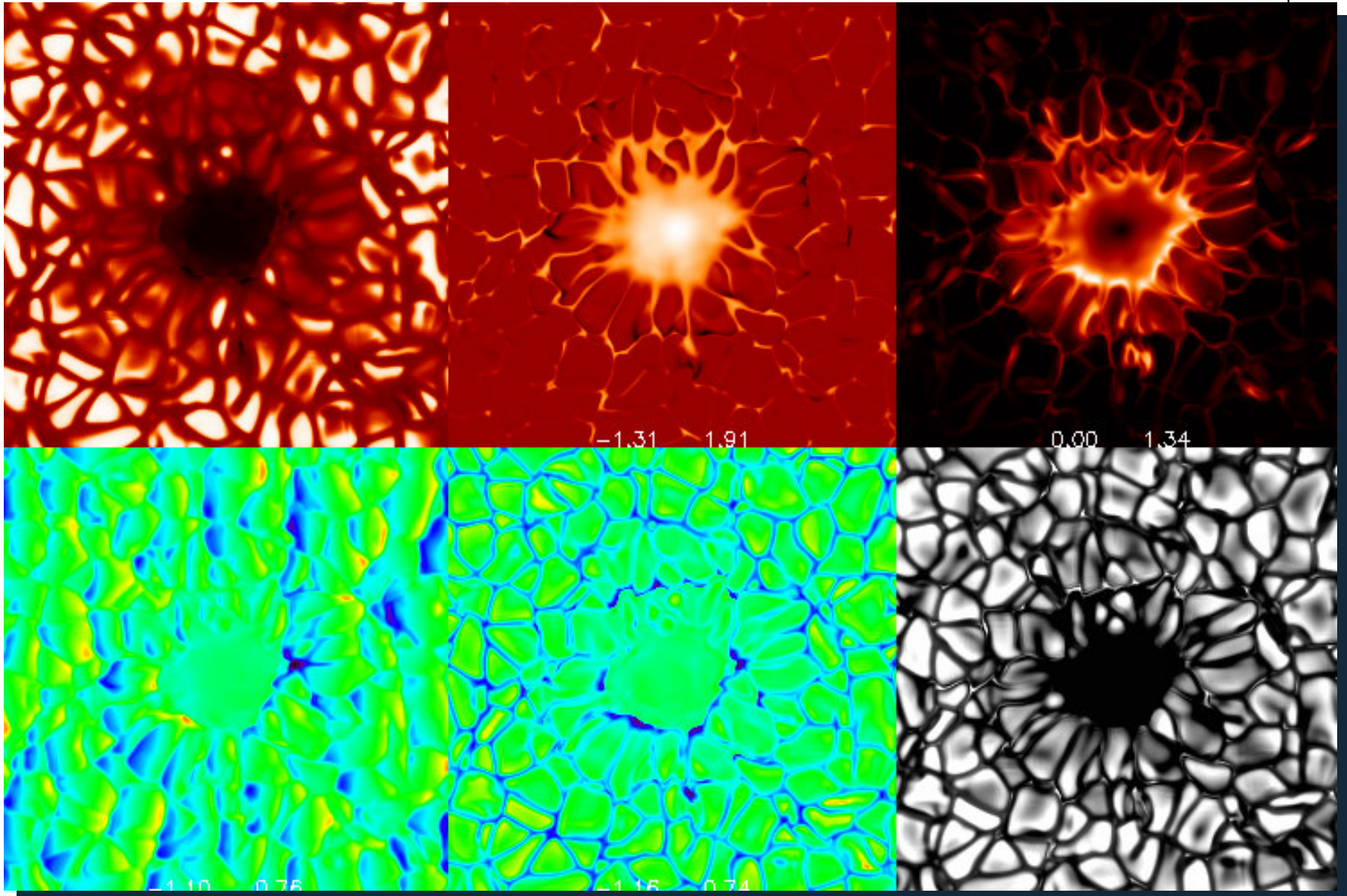
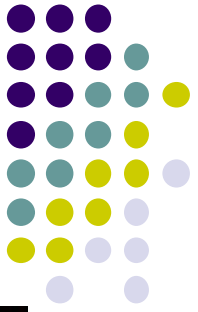
# Magneto-convection: Pores and sunspots



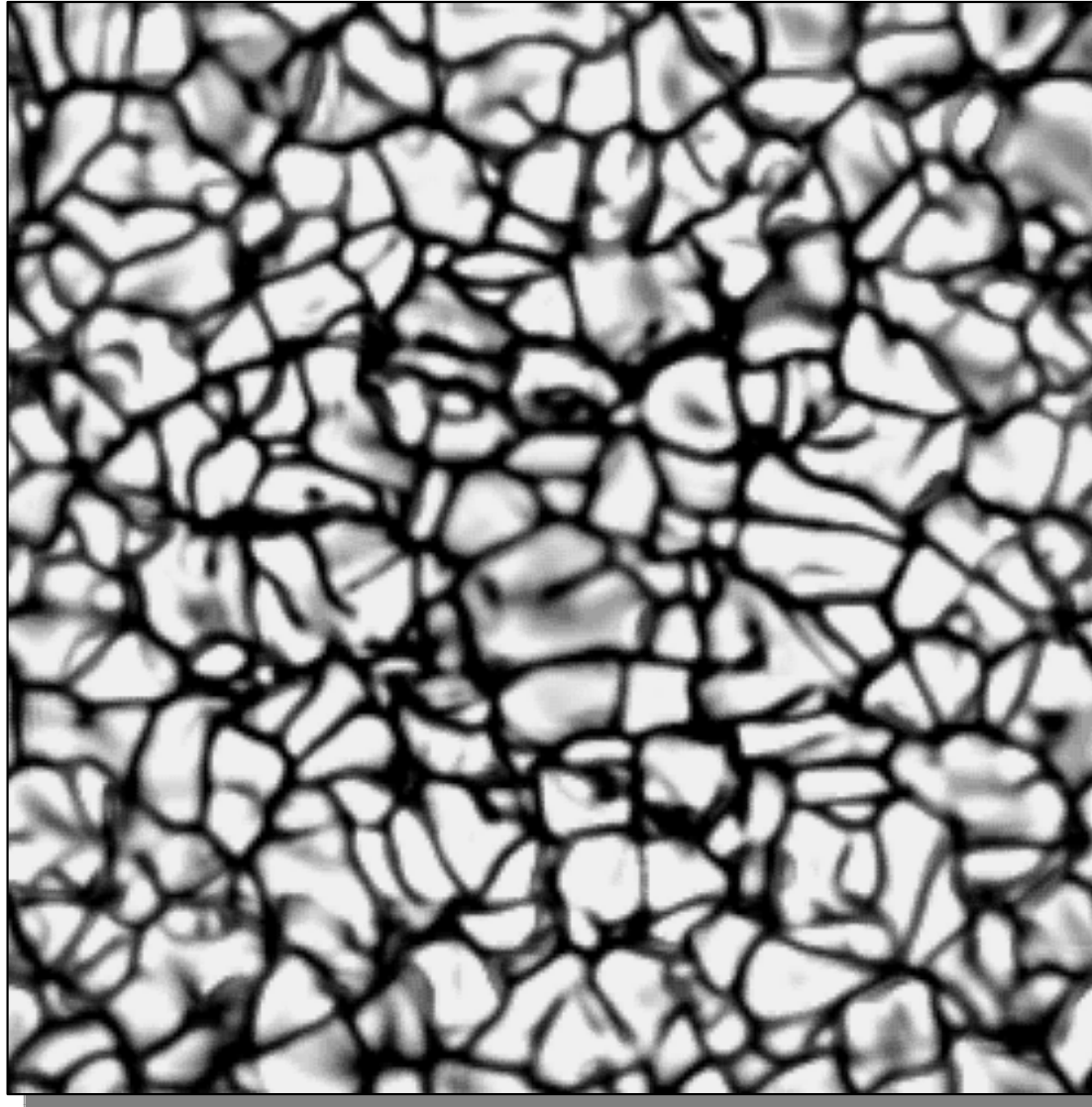
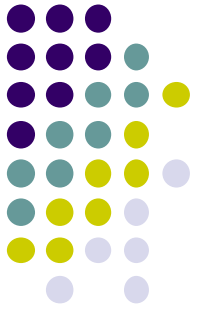
R. Cameron et al.: Radiative magnetohydrodynamic simulations of solar pores



# Temperature, hor. & vert. magn. field, hor. & vert. velocity, surface intensity

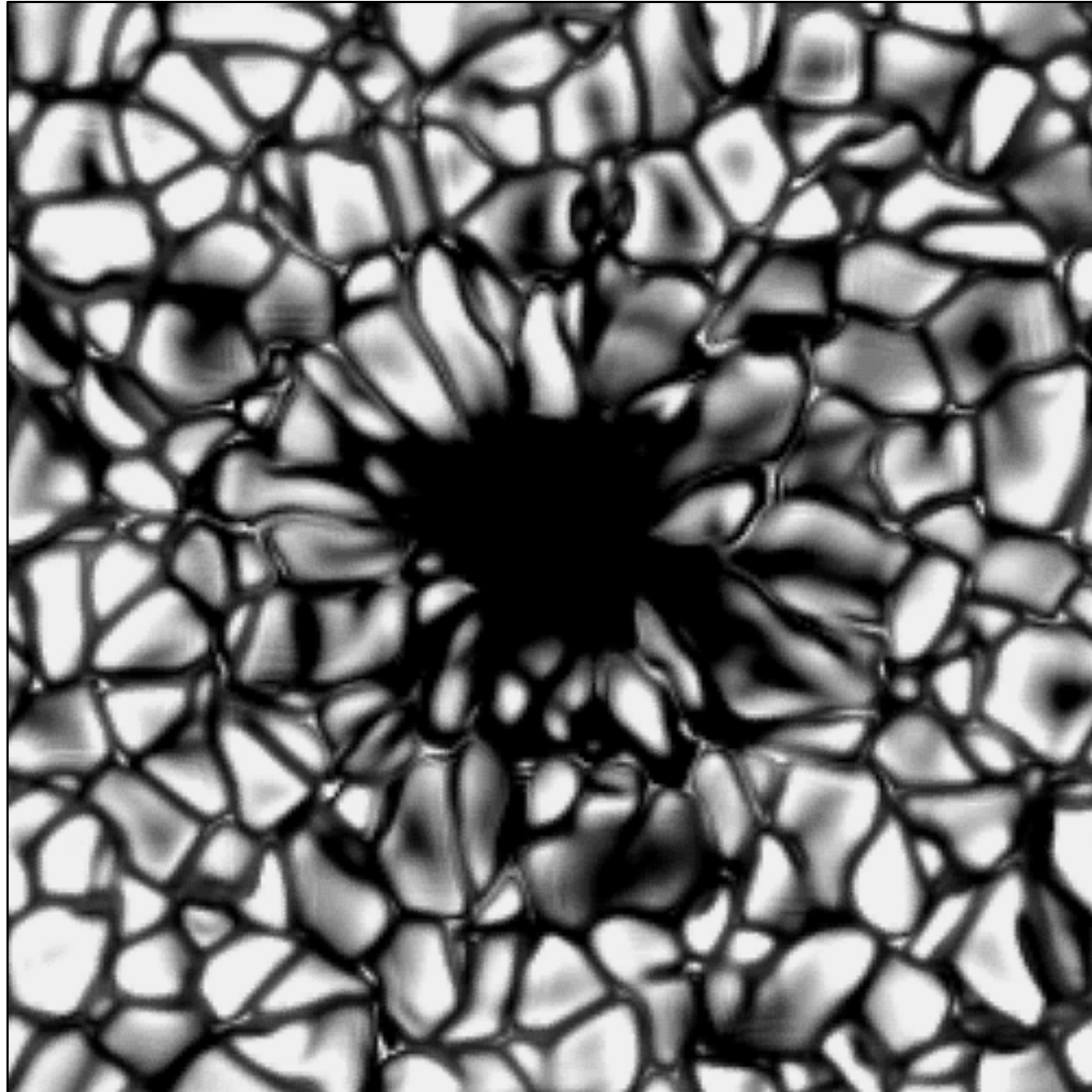
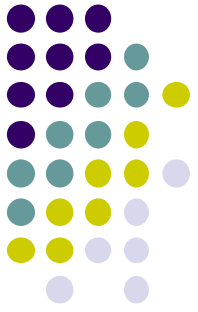


# Sunspot, initial time evolution

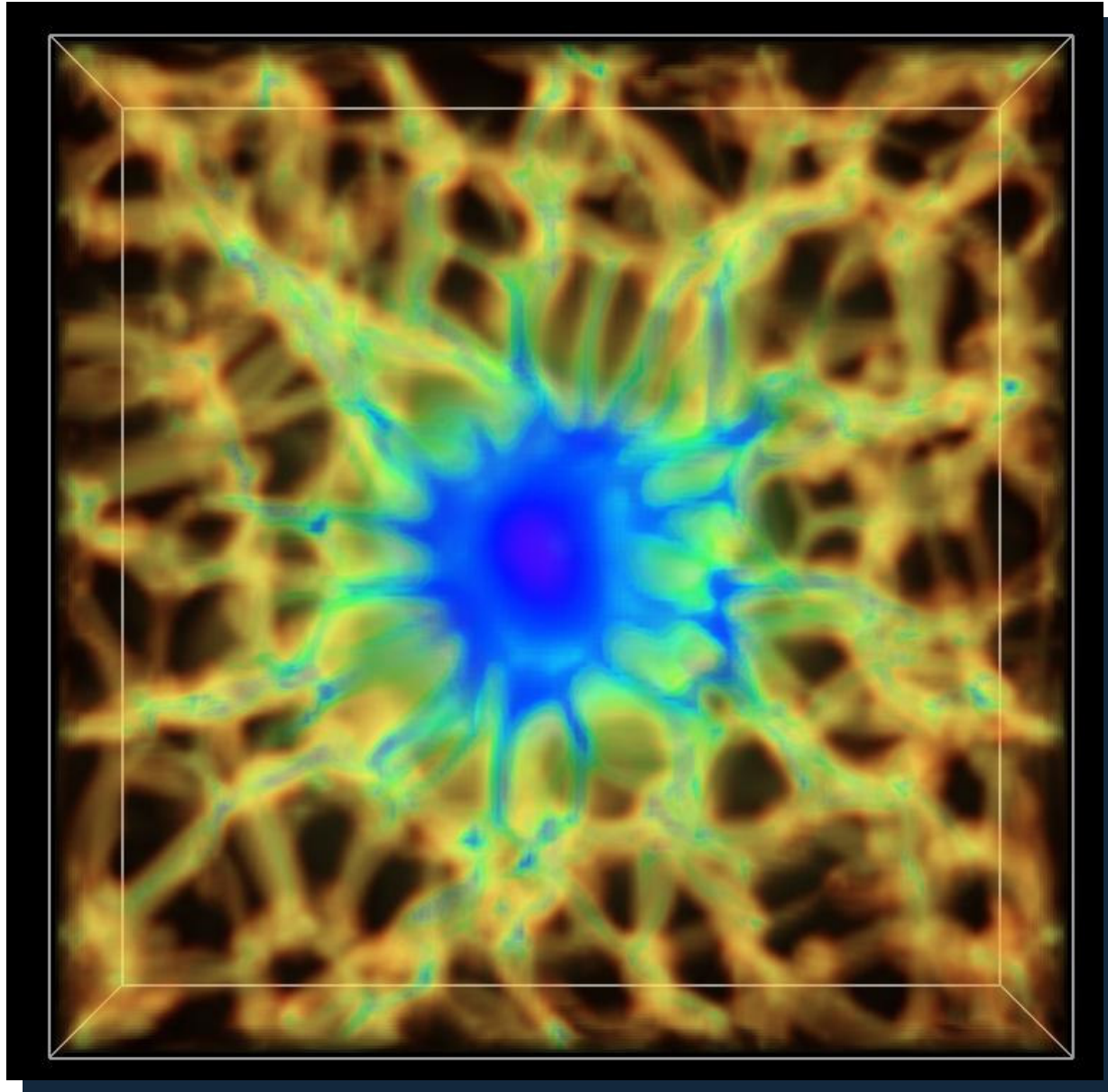
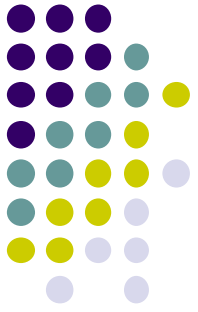




# Sunspot, time evolution (rep.)

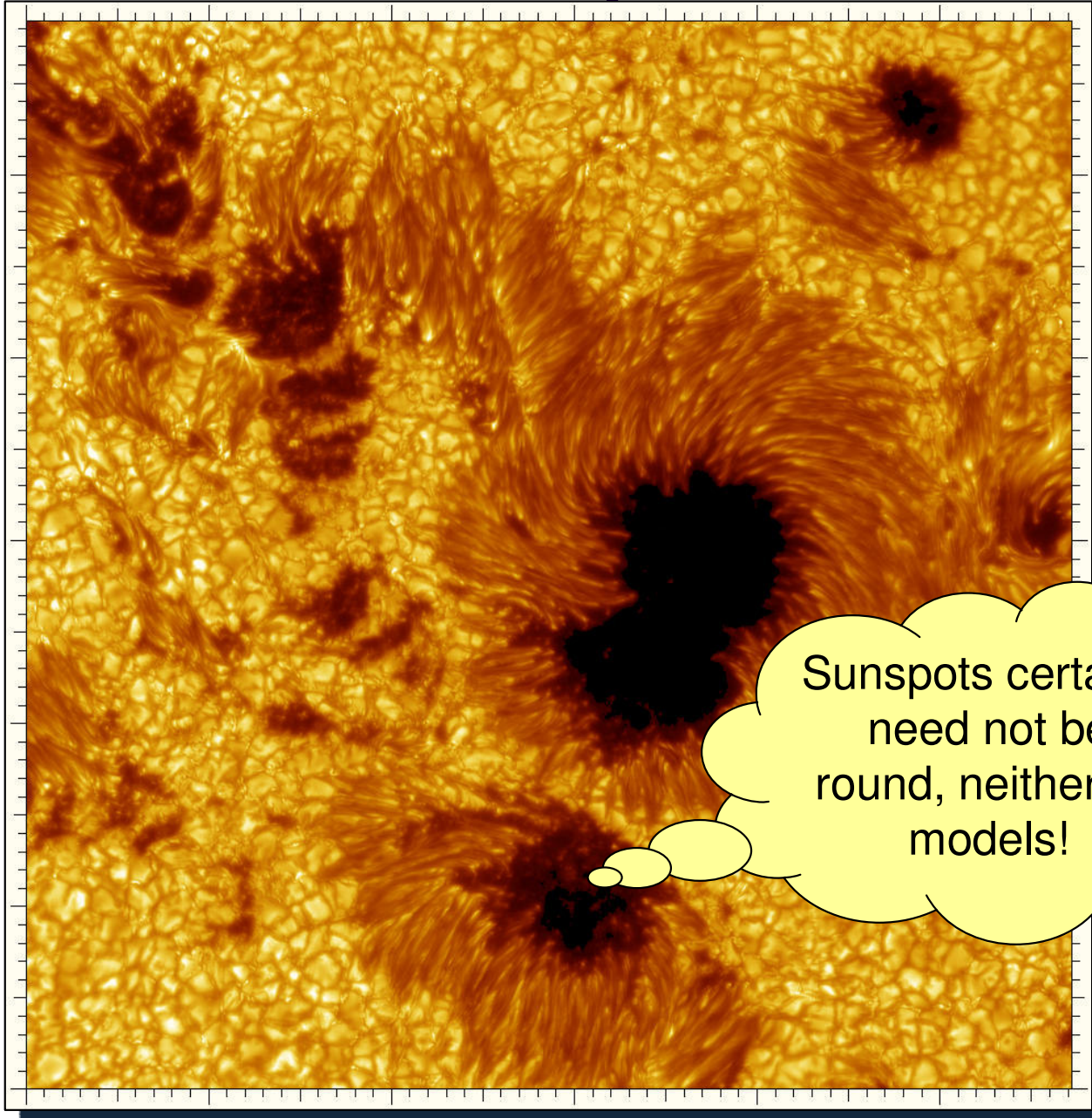
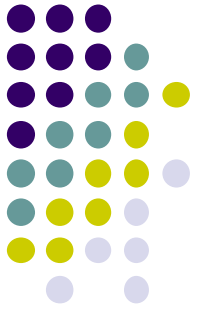


# Sunspot, log magnetic pressure



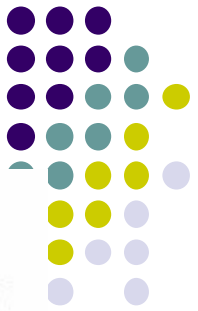
# Sunspots w/o Penumbrae

# Penumbrae w/o Sunspots

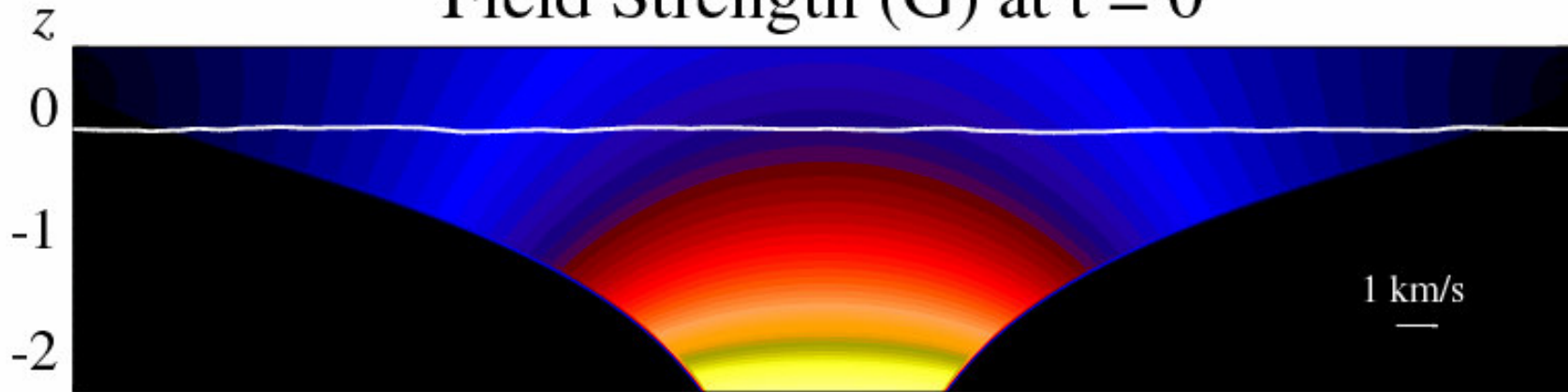


Sunspots certainly  
need not be  
round, neither do  
models!

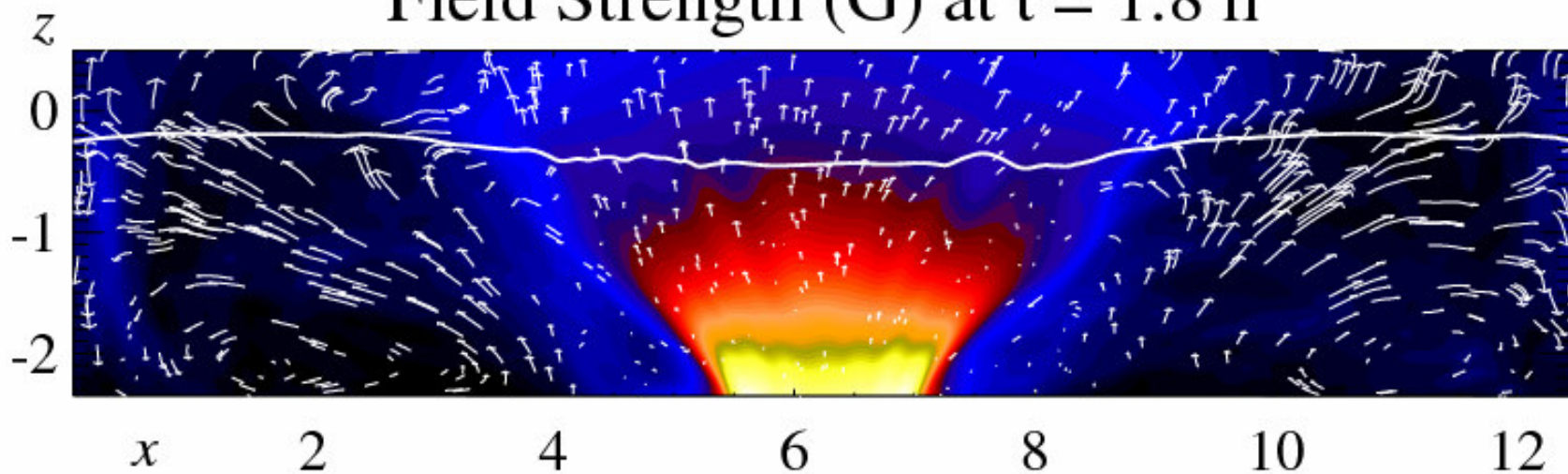
# Cross section of model



Field Strength (G) at  $t = 0$



Field Strength (G) at  $t = 1.8$  h

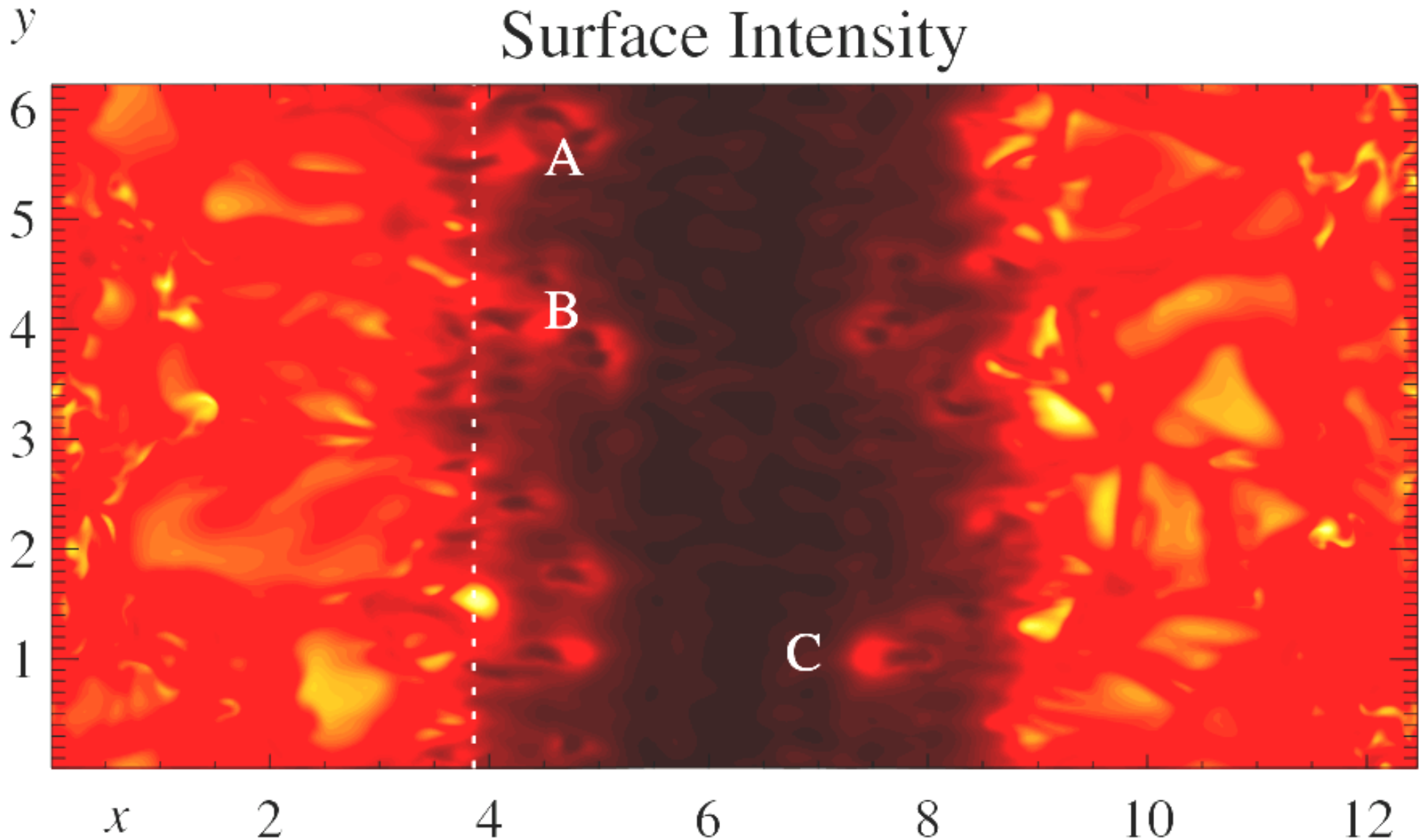


2000

4000

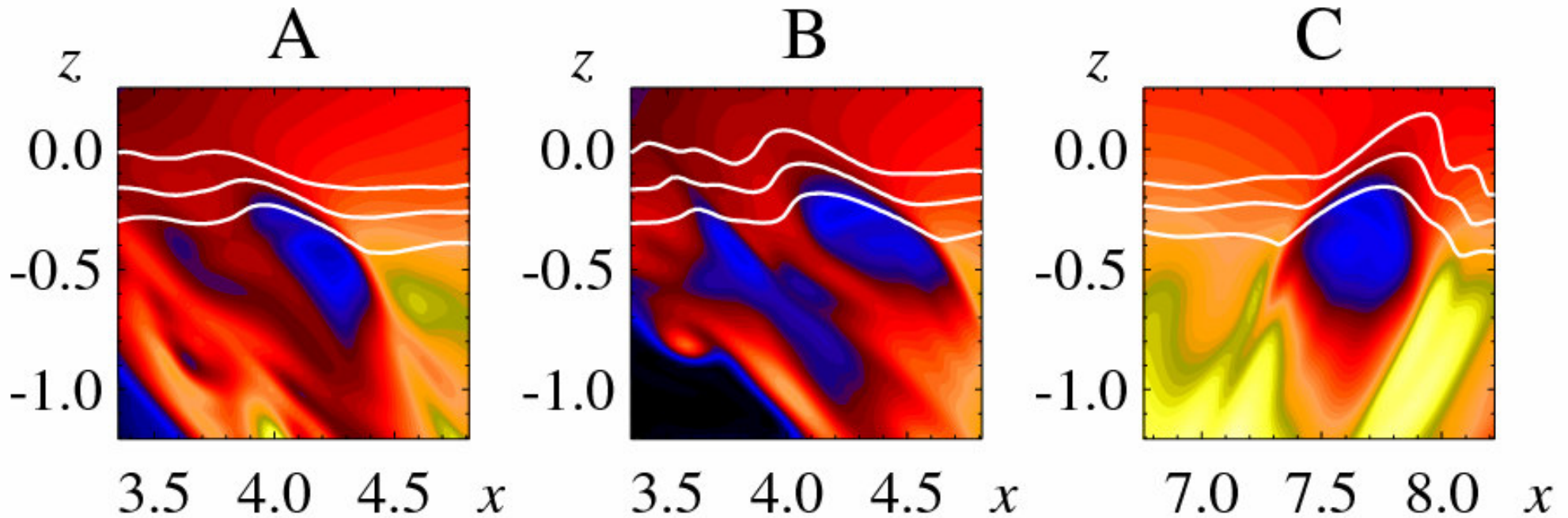
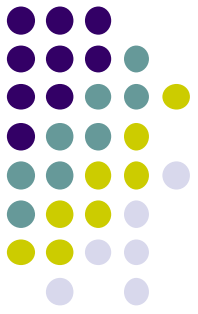
6000

# Snapshot, with dark filaments

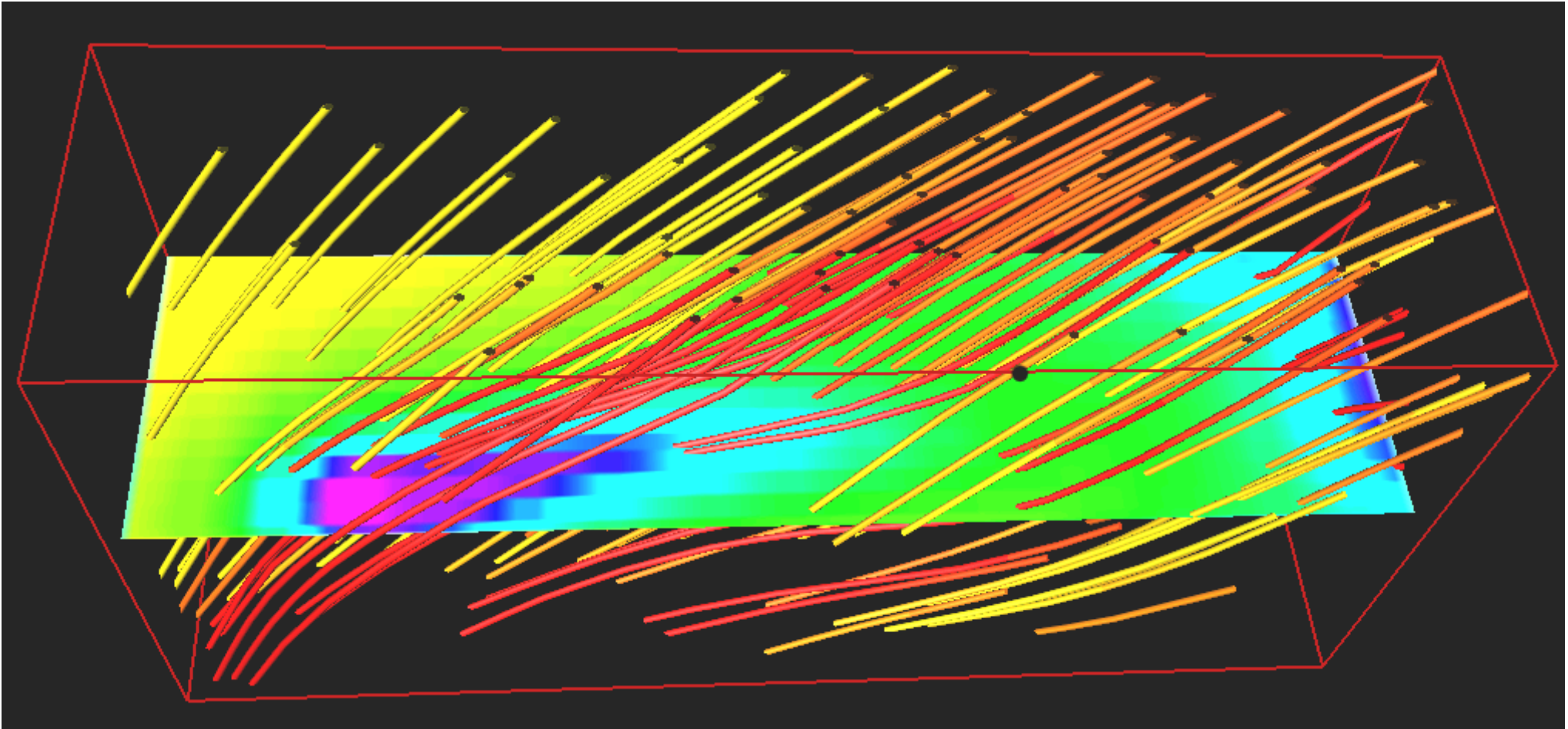
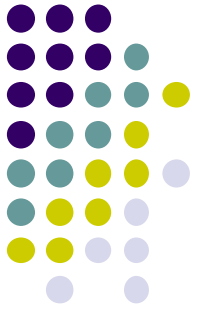


Heinemann, Nordlund, Scharmer & Spruit 2007  
Scharmer, Nordlund & Heinemann 2008

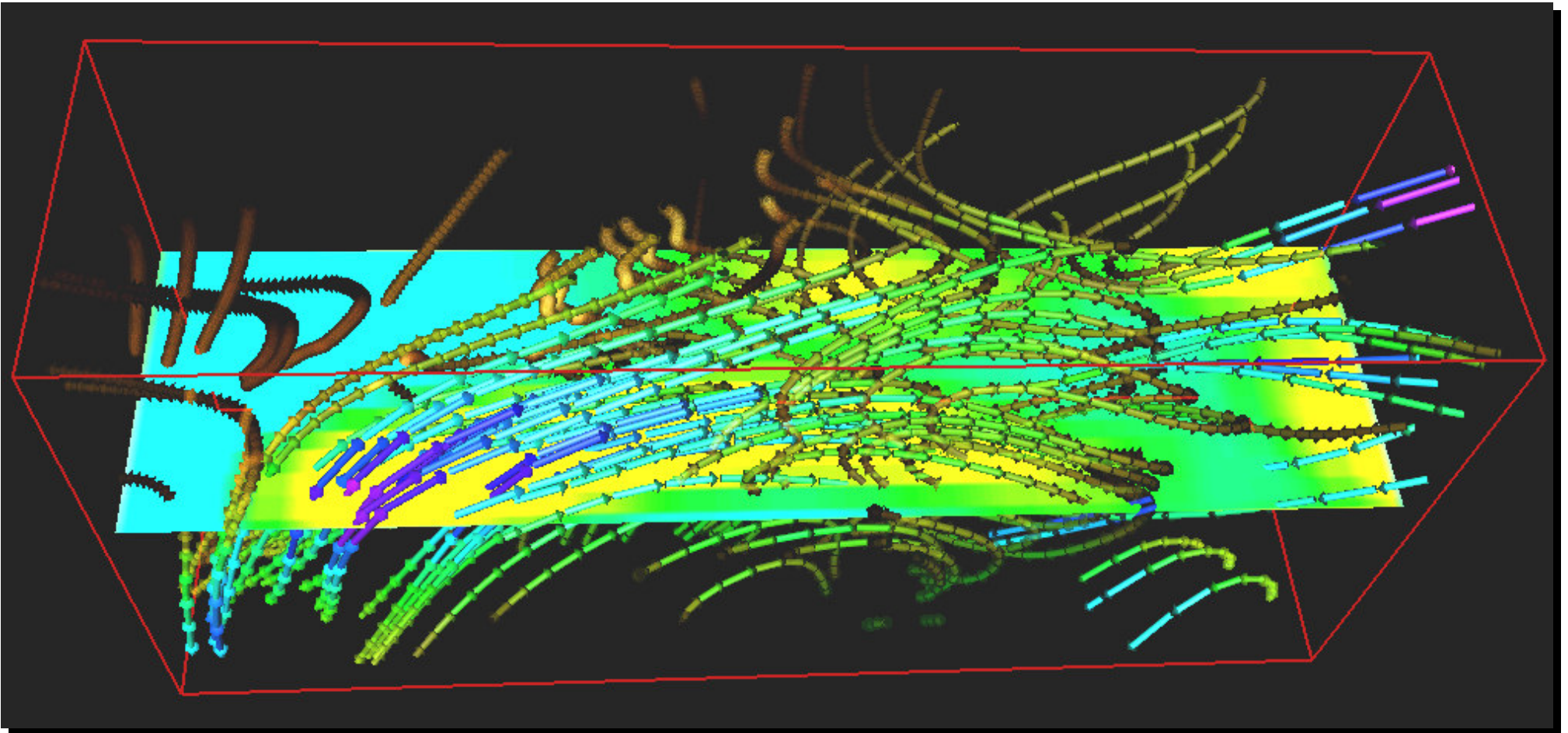
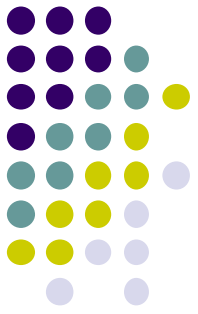
# Zoom in on dark filaments, from the side



# Magnetic field lines and vertical velocity (image plane)

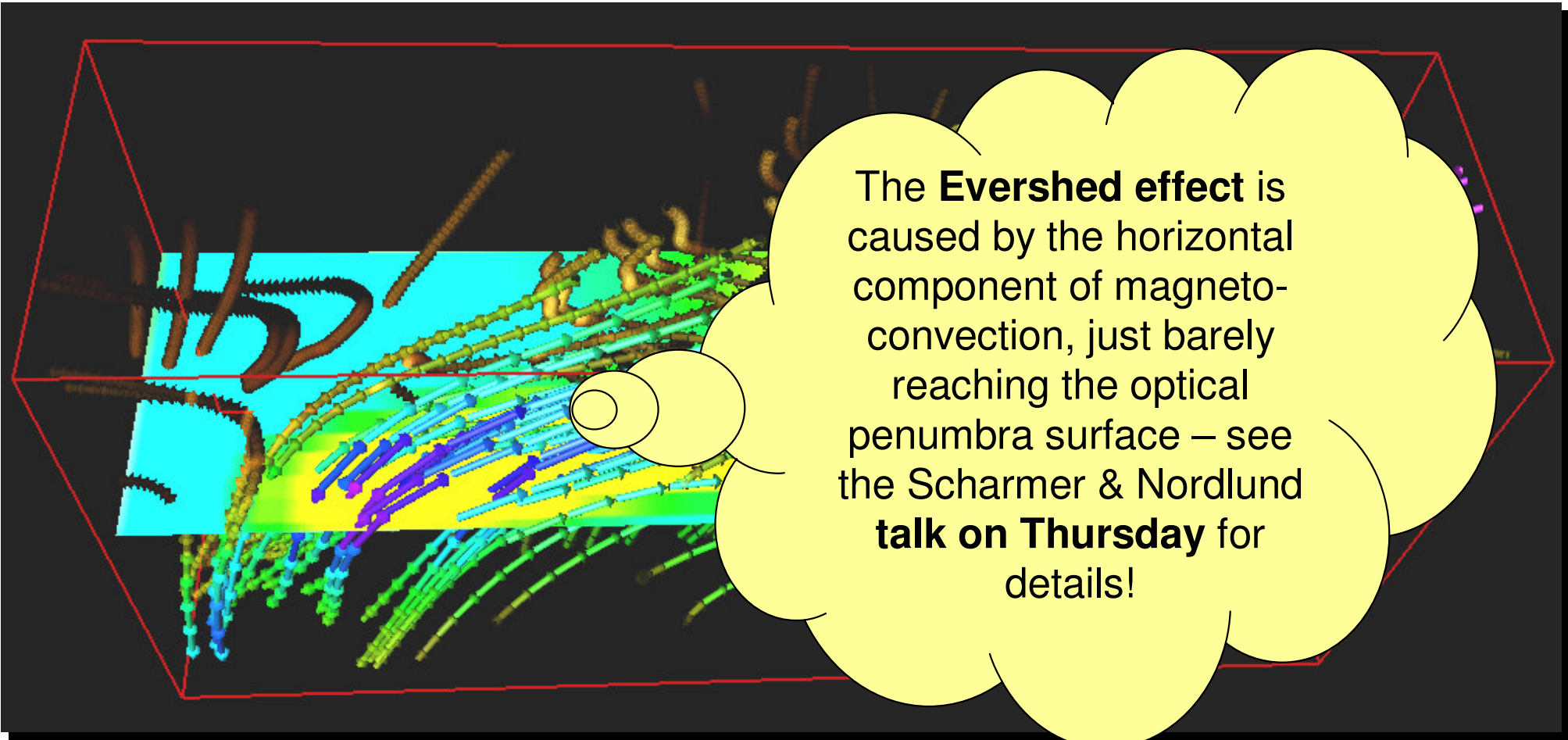
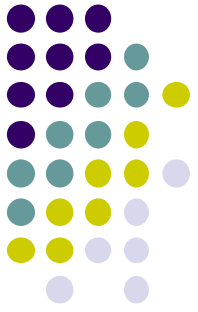


# Velocity field and magnetic field strength (image plane)



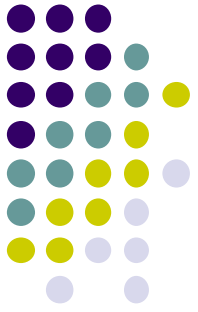


# Velocity field and magnetic field strength (image plane)

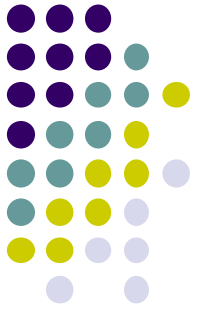


The **Evershed effect** is caused by the horizontal component of magnetoconvection, just barely reaching the optical penumbra surface – see the Scharmer & Nordlund talk on Thursday for details!

# Summary

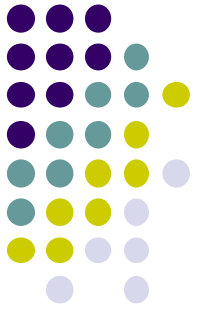


- Stellar magneto-convection is fundamentally ***multi-scale***
  - Major difficulty for modeling and understanding!
- But also has  $\sim$  ***scale invariance***
  - That helps a lot!
- Two asymptotic regimes; ***small and large***
  - Approx. self-similarity also in B, flare event size,...
- The Sun + simulations provide ***proof*** that ***dissipation converges*** at relatively low Re
  - Similar behavior expected for magnetic dissipation



**Thanks for your attention!**

# Acknowledgments



The results presented here were made possible by hardware grants to ÅN from the Danish Center for Scientific Computing, and by Columbia computing resource grants to Bob Stein from NASA / NAS.

Visualizations partly done with VAPOR from NCAR.