Measurements

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Some Resources

- http://ipag.osug.fr/~philybla/teaching/phy553b.html
- http://www.astro.princeton.edu/~draine/book/index.html
- http://www.physics.sfsu.edu/~lea/
- http://spiff.rit.edu/classes/
- http://home.strw.leidenuniv.nl/~emr/stralingsprocessen/

Cox ARAA 2005, 43, 337

• The interstellar medium (ISM) is a fascinating place to spend one's life. There is ample beauty in the images, abundant challenge in the observations, good company in the fellow travelers, and a high sense of importance attached to the work as a foundation for understanding how galaxies work, along with the ways they may have influenced one another and the intergalactic medium. There is also sufficient uncertainty about what is happening that it presents a huge canvas for the joyous exercise of imagination.

Magnitude Scale

- Greeks classified stars by brightness to eye.
 - Eye responds in a logarithmic scale.
- Brightest stars classified as 0th magnitude.
 - Each magnitude corresponds to a factor of 2.5 in brightness.
- Faintest observable stars about 6th magnitude.



Magnitude Scale

Modern magnitude scale:

- Defined by Vega zeroth magnitude A0 star.
- $m = -2.5 \log(f_{obs}/f_0)$
- Breaks down for UV.
 - A0 stars have no flux below 2000 Å.

Zombeck:

http://ads.harvard.edu/cgi-bin/bbrowse?book=hsaa&page=100

Standard photometric systems

Standard U, B, V, R, I and long wavelength systems

Filter band	λο ^(a) (μm)	$\Delta \lambda_0$ (FWHM) (μ m)	Absolute spectral irradiance for $mag = 0.0$			
			$f_{\lambda}(0)$ (erg cm ⁻² s ⁻¹ Å ⁻¹)	$f_v(0)$ (W m ⁻² Hz ⁻¹)		
U	0.365	0.068	4.27×10^{-9}	1.90×10^{-23}		
В	0.44	0.098	6.61×10^{-9}	$4.27(4.64)^{(b)} \times 10^{-23}$		
V_{-}	0.55	0.089	3.64×10^{-9}	3.67×10^{-23}		
R	0.70	0.22	1.74×10^{-9}	2.84×10^{-23}		
I	0.90	0.24	8.32×10^{-10}	2.25×10^{-23}		
J	1.25	0.3	3.18×10^{-10}	1.65×10^{-23}		
H	1.65	0.4	1.18×10^{-10}	1.07×10^{-23}		
K	2.2	0.6	4.17×10^{-11}	6.73×10^{-24}		
L	3.6	1.2	6.23×10^{-12}	2.69×10^{-24}		
Μ	4.8	0.8	2.07×10^{-12}	1.58×10^{-24}		
Ν	10.2		1.23×10^{-13}	4.26×10^{-25}		

^(a) $\lambda_0 = \int \lambda S(\lambda) d\lambda / \int S(\lambda) d\lambda$, where $S(\lambda)$ is the photometer response function. ^(b) From S. Kleinmann.

U, B, R, I, N values from Allen, C. W., Astrophysical Quantities. The Athlone Press (1973). V, J, H, K, L, M values from Wamsteker, W., Astron. Astrophys., 97, 329 (1981).

The spectral irradiance for a star of a given magnitude is given either by:

 $\log f_{\lambda}(m_x) = -0.4m_x + \log f_{\lambda}(0),$

where $f_{\lambda}(m_x)$ is the spectral irradiance in erg cm⁻² s⁻¹ Å⁻¹ of a star of magnitude (m_x) in the x filter band at the mean wavelength $\lambda_0(x)$, or

$$\log f_{\rm v}(m_{\rm x}) = -0.4m_{\rm x} + \log f_{\rm v}(0)$$

where $f_v(m_x)$ is the spectral irradiance in W m⁻² Hz⁻¹.

The relationships above are for the irradiance at the top of the Earth's atmosphere and are valid for B through M stars.

Photometer response curves for UBVRI and long wavelength systems. (Adapted from Webbink, R. F. & Jeffers, W. Q., *Space Sci. Rev.*, 10, 191 1969.)



Magnitude Scale

Better to use SI units:

• ergs cm⁻² s⁻¹
$$_{A}^{*}$$
 -1

- Apparent magnitude observed from Earth.
- Absolute magnitude intrinsic to the star.

Standard photometric systems

Standard U, B, V, R, I and long wavelength systems

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Apparent/Absolute Magnitude

- Absolute magnitude is brightness of star at 10 pc.
- Apparent magnitude is observed brightness.
- $F = L/4\pi d^2$
- $m_1 m_2 = -2.5 \log(F_1/F_2)$
- $m_1 m_2 =$ -2.5log(d₂/d₁)² = -5log(d₂/d₁)



Apparent/Absolute Magnitude

- Absolute magnitude is brightness of star at 10 pc.
- Apparent magnitude is observed brightness.
- $F = L/4\pi d^2$
- m M = 5 => F/f = 100.
 - d = 10D
- Distance Modulus:
 - $m M = 5 \log d 5$



Reddening

- Measure B and V magnitudes.
 - B: 4400 ± 500 Å.
 - V: 5500 ± 500 Å.
- Star has intrinsic (B-V)
 - $(B V)_I = 0$ for A0 stars.

- $E(B V) = (B V)_{O} (B V)_{I}$.
- $A_v = 3.1 E(B V) =$ 1.086 τ
- Distance Modulus: $(m_v - A_v) - M_v = 5 \log d - 5$

Spectrographs



$n\lambda = d (sin(i) + sin(I))$

Solar Spectrum



Solar Spectrum



Spectroscopy



Grotrian Diagram (Oxygen)



Atomic Basics

- H I is atomic hydrogen.
- H II is ionized hydrogen not to be confused with H_2 .
- O VI is O^{+5} five times ionized oxygen.
- Atomic energy levels: n, 1 where $0 \le l \le n$.
 - n: energy; l: angular momentum
 - s, p, d, f for l = 0, 1, 2, 3

Atomic Basics

- Atomic energy levels: n, 1 where $0 \le l < n$.
 - n: energy; l: angular momentum
 - s, p, d, f for l = 0, 1, 2, 3
- Degenerate quantum numbers
 - m_z : projection of angular momentum onto z axis.
 - spin of electron.
- Pauli Exclusion Principle.
 - Degeneracy: 2(21 + 1).
- C: $1s^22s^22p^2$.

Periodic Table

- 1A -									noble
H	Abridged Periodic Table of the Elements 4/17/96 ghw								He
1s ¹	2A			3A	4A	5A	6A	- 7 A -	1s ²
Li	Be		. 2	5 B 221	C	N	0	9 F 20	10 Ne
1s-2s	1s-2s-		15	Zs=2p	Zs-Zp-	Zs=Zp=	Zs-Zp	2s-2p-	Zs-Zp°
Na	Mg ¹²	1B	2B		Si ¹⁴	P 10	S		Ar
[Ne]3s ¹	[Ne] 3s ²		[Ne]	3s ² 3p ¹	$3s^2 3p^2$	3s² 3p ³	$3s^2 3p^4$	$3s^2 3p^5$	$3s^2 3p^6$
K ¹⁹		Cu ²⁹	Zn ³⁰	Ga ³¹	Ge ³²	As ³³	Se ³⁴	Br ³⁵	Kr ³⁶
[Ar] 4s ¹	[Ar]3d ¹⁰	4s ¹	4s ²	4s ² 4p ¹	$4s^2 4p^2$	$4s^24p^3$	$4s^2 4p^4$	$4s^2 4p^5$	$4s^24p^6$
Rb ³⁷		Ag ⁴⁷	Cd ⁴⁸	49 In	Sn ⁵⁰	Sb ⁵¹	Te ⁵²	53 	Xe ⁵⁴
[Kr] 5s ¹	[Kr]4d ¹⁰	5s ¹	5s ²	5s²5p ¹	5s²5p²	5s ² 5p ³	5s²5p ⁴	5s ² 5p ⁵	5s ² 5p ⁶
Cs ⁵⁵	[Xe]	79 Au	80 Hg	81 TI	82 Pb	83 Bi	84 Po	At ⁸⁵	Rn ⁸⁶
[Xe] 6s ¹	4f ¹⁴ 5d ¹⁰	6s ¹	6s ²	$6s^26p^1$	$6s^26p^2$	6s ² 6p ³	6s²6p ⁴	$6s^26p^5$	6s ² 6p ⁶

Selection rules

- The selection rules that apply to one-electron systems are:
 - orbital angular momentum: $\Delta l = \pm 1$
 - parity must change between states.
 - magnetic quantum number: $\Delta m = 0, \pm 1$
 - spin does not change: $\Delta s = 0$ (always true for the H atom)
 - total angular momentum: $\Delta j = 0, \pm 1$
- Forbidden transitions violate a selection rule.

Allowed HI Transitions



Line Broadening

- Uncertainty relationship between E and t.
 - Lorentzian: 2γ is Einstein A coefficient for spontaneous transition.
 - 1/A is the lifetime of the state.

$$I(v) = I_0 \gamma \frac{1}{(v - v_0)^2 + (\gamma/4\pi)^2}$$



Line Broadening

- Thermal broadening.
 - Gaussian.
- FWHM is 2.3548σ.
- σ is dependent on the Temperature and on turbulence.

$$\varphi_{mn}(\upsilon) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(\upsilon - \upsilon_{mn})^2}{2\sigma^2}\right)$$
$$2\sigma^2 = \frac{\nu_{mn}^2}{c^2} \left(\frac{2kT_k}{M} + V^2\right)$$



Line Broadening

- Uncertainty relationship between E and t.
 - Lorentzian.
- Thermal broadening.
 - Gaussian.
- Convolution.
 - Voigt function.

 $\varphi(v) = \frac{2\sqrt{\ln 2}}{\sqrt{\pi}\Delta v_D}H(a,b)$ $a = \sqrt{\ln 2}\Delta v_L/(2\Delta v_D)$ $b = 2\sqrt{\ln 2}(v - v_0)/\Delta v_D$ $H(a,b) = \frac{a}{\pi}\int \frac{\exp(-y^2)dy}{(b-y)^2 + a^2}$ $\Delta v_D \ FWHM - Doppler$ $\Delta v_L \ FWHM - Lorentzian$



Emission Lines



- Instrumental broadening.
- Typically gaussian.
- Limits information from lines.

http://www.thespectroscopynet.com/Index.html?/Lineshapes_1.html

Real Data



A new interest of mine is the search for molecular oxygen (O2) in the interstellar medium. The fractional abundance of O2 is an important, but as yet unknown, parameter for models of interstellar clouds. This species likely plays a central role in gas-phase interstellar chemistry. If present in significant abundance, O2 may also function as an important coolant of interstellar clouds and therefore play a role in cloud contraction and star formation.

Oxygen is the third-most abundant nucleon in the universe yet its form in much of the interstellar medium remains a mystery. The presence of ionized oxygen has long been known in HII regions, while [OI] lines have been observed in some photon-dominated regions. In the denser, better-shielded regions where molecules exist, O2 is predicted to be one of the most important

http://www.etsu.edu/physics/mwc/interest.htm#Molecular%20Oxygen%20in %20the%20Interstellar%20Medium

Spectral Resolution

- Resolution = $\lambda/\Delta\lambda$.
 - IUE: Resolution was 0.2 Å at 2000 Å \Rightarrow R = 10,000.
 - FUSE: R = 20,000.
- For small velocities: $\Delta \lambda = \Delta v/c \lambda$.
- IUE: $\Delta v = 30 \text{ km s}^{-1}$.
- Typical interstellar lines may be $< 10 \text{ km s}^{-1}$.

Equivalent Width

• Equivalent width.

$$W_{\lambda} = \int (1 - F_{\lambda}/F_0) d\lambda$$

- Same area as line.
- Independent of instrumental broadening.



Voigt Profiles



The equivalent width (equation 11.A.1) is the area above these curves, and it can be seen again that determining the upper limit for x' is a problem.

Curve of Growth

- Equivalent width more robust than modelfitting.
- Easier to measure.



Curve of Growth

- b is the velocity dispersion
- Dimensional check: (m² kg s⁻² K⁻¹ kg⁻¹ K + m²s⁻²)m⁻²s².

$$\varphi_{mn}(\upsilon) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left(-\frac{(\upsilon - \upsilon_{mn})^2}{2\sigma^2}\right)$$
$$2\sigma^2 = \frac{\nu_{mn}^2}{c^2} \left(\frac{2kT_k}{M} + V^2\right)$$



- Intensity defined such that:
- $dE = I_v dA dt d\Omega dv$ where dE is the energy crossing dA in time dt in the frequency range dv
- I_v units are ergs s⁻¹ cm⁻² sr⁻¹ Hz⁻¹



Definitions

• If LTE then
$$I_{\nu} = \frac{2h\nu^3}{c^2} \frac{1}{e^{\frac{h\nu}{kT}} - 1}$$

- Brightness temperature
 - $T_B(v)$ is temperature at which a blackbody would have the same specific intensity.

Definitions

- Antenna temperature:
 - Linear with intensity and $\sim T_B$ for $kT_A >> hv$
- Excitation temperature of u relative to 1.
 - where n is number, g is degeneracy and E is energy of upper and lower states.

 $T_A(
u) \equiv rac{c^2}{2kw^2} I_
u$

$$rac{n_u}{n_l} \equiv rac{g_u}{g_l} e^{-rac{E_u - E_l}{kT_{exc}}}$$

 $dE = I_v dA dt d\Omega dv =$ $I_{\lambda} dA dt d\Omega d\lambda$ $I_{v} dv = I_{\lambda} d\lambda$ $v = c/\lambda \Longrightarrow dv = c/\lambda^2 d\lambda$ $c/\lambda^2 I_{\nu} = I_{\lambda}$ dimensional check: $(m s^{-1})(m^{-2})(ergs s^{-1} m^{-2} sr^{-1} Hz^{-1}) =$ ergs s⁻¹ m⁻² sr⁻¹ m⁻¹



- Spontaneous emission coefficient *j*.
 - *j* is *energy* emitted per unit *time* per unit *solid angle* per unit *volume*.
- $dE = j dV d\Omega dt$
- $dI_v = j_v ds$



- Absorption coefficient: $\alpha_v = n\sigma_v$
- $dI_v = -\alpha_v I_v ds$



- Equation of radiative transfer: $dI_v/ds = -\alpha_v I_v + j_v$
- Define: optical depth: $d\tau_v = \alpha_v$ source function: $S_v = j_v / \alpha_v$
- $dI_v/d\tau_v = -I_v + S_v$



$$I_{\nu} = I_{\nu(0)} e^{-\tau_{\nu}} + \int_{0}^{\tau_{\nu}} e^{-(\tau_{\nu} - \tau_{\nu}')} S_{\nu}(\tau_{\nu}') d\tau_{\nu}'$$

Kirchoff's Law

- Infinite uniform slab: $I_v = B_v(T)$
- $dI_v = 0 = -B_v d\tau_v + S_v d\tau_v$.
- Kirchoff's Law: $S_v = j_v / \alpha_v = B_v(T)$

$$I_{\nu} = I_{\nu(0)} e^{-\tau_{\nu}} + \int_{0}^{\tau_{\nu}} e^{-(\tau_{\nu} - \tau_{\nu}')} S_{\nu}(\tau_{\nu}') d\tau_{\nu}'$$

Limiting Cases

- Optical/UV
- All atoms in ground state so spontaneous emission may be neglected.
 - In ground state because no collisional excitation.

- Radio
- Upper levels are populated and spontaneous emission important.
 - If population inversion, maser occurs.

Transitions

- Spontaneous emission: Energy drops from upper state to lower state.
 - Einstein A coefficient A₂₁: transition probability per unit time.
 - Random process independent of radiation field.

Transitions

- Absorption dependent on the number of absorbers and the strength of the radiation field: $\frac{dn_2}{dt} = n_1 B_{12} u_{\nu}$
- where n_2 is the number in upper state; u_v is the radiation density and B_{12} is the Einstein B coefficient.
- For stimulated emission replace B_{12} with B_{21} .

Relation between Einstein coefficients

- In thermodynamic equilibrium:
- $n_1 B_{12} B(T) = n_2 A_{21} + n_2 B_{21} B(T)$
- but $n_1/n_2 = g_1/g_2$ e(hv/kT) where g is the degeneracy factor. A_{21}/B_{21}
- After algebra: $B(T) = \frac{A_{21}/B_{21}}{(g_1 B_{12}/g_2 B_{21})exp(h\nu/kT) 1}$
- *But* for this to be true for all T:
 - $g_1 B_{12} = g_2 B_{21}$
 - $A_{21} = 2hv^3/c^2 B_{21}$

Einstein Coefficients

- $\alpha_v = (hv/4\pi) (n_1 B_{12} n_2 B_{21}) \phi(v)$ where $\phi(v)$ is the absorption profile
- $j_v = (hv/4\pi) n_2 A_{21}$ with the assumption that the emission profile is the same as the absorption profile.
- oscillator strength: $B_{12} = (4\pi^2 e^2)/(hv_{21}m_e c)f_{12}$
- $\mathbf{g}_1 \mathbf{f}_{12} = -\mathbf{g}_2 \mathbf{f}_{21}$

Curve of Growth



FIG. 5.—Empirical curve of growth for the dominant ion states expected in H I clouds. The solid lines were drawn for a Maxwellian velocity distribution with b = 6.5 km s⁻¹ and the damping constants appropriate for the lines labeled in the upper right corner. The horizontal scale was labeled to give log $N(\text{cm}^{-2})$ for Fe II $\lambda 2382$.

Absorption Line Data

 Two components in Fe II line of α Tri.



FIG. 4.—Fe II $\lambda 2599$ region of α Tri showing the observed spectra, the st-fit model ater convolution, and the residuals of the best fit. Two nponents are seen in the opacity profile. The continuum is normalized unity, and the rest wavelength for Fe II is shown by the labeled tick rk.

Absorption Line Data

- Two components in Fe II line of α Tri.
- Fit Ly α line with two components.
- D I next to H I line.



Absorption Line Data

- Two components in Fe II line of α Tri.
- Fit Ly α line with two components.
- D I next to H I line.
- Stellar confusion.





the resolution of the FUSE spectrographs. Therefore, in 65% of these stars the interstellar and photospheric contributions could be separated and the nature of the O VI component unambiguously determined. Furthermore, in other examples, where the spectra were of a high signal-to-noise, no photospheric material was found and any O VI detected was assumed to be interstellar. Building on the earlier work of Oegerle et al. and Savage & Lehner, we have increased the number of detections of interstellar O vI and, for the first time, compared their locations with both the soft X-ray background emission and new detailed maps of the distribution of neutral gas within the local interstellar medium. We find no strong evidence to support a spatial correlation between O VI and SXRB emission. In all but a few cases, the interstellar O vI was located at or beyond the boundaries of the local cavity. Hence, any $T \sim 300,000$ K gas responsible for the O vI absorption may reside at the interface between the cavity and surrounding medium or in that medium itself. Consequently, it appears that there is much less O vi-bearing gas than previously stated within the inner rarefied regions of the local interstellar cavity.

Key words: ISM: clouds - ISM: general - ISM: structure - ultraviolet: ISM - ultraviolet: stars - white dwarfs

Online-only material: color figures

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Θ

1. INTRODUCTION

The existence of the diffuse soft X-ray background (SXRB; Bowyer et al. 1968) implies that a substantial fraction of the Galactic disk, at least near the Sun, is filled with low-density hot gas (McCammon et al. 1983). This discovery has important implications for our understanding of the structure and ionization of the interstellar medium (ISM) and in subsequent decades further studies have been made of the diffuse background, with a full sky survey being conducted by the ROSAT mission (Snowden et al. 1995, 1998). The total soft X-ray emission has

ergy input of 114 eV. Since the local interstellar radiation field declines steeply at energies above this value (Vallerga 1998), it is very difficult to account for the presence of O vI with a photoionization model. Therefore, the best explanation is that the O VI arises from collisional ionization in gas at a temperature in excess of 2×10^5 K. This proposition is supported by the relative breadth of the O vI absorption line profiles, compared to those of lower ionization potential, which are consistent with thermal broadening at this temperature. In this paper, we refer to the $T \sim 300,000$ K material which may be responsible for O VI absorption as "transition temperature" gas to differentiate it from the "hot" a 1 000 000 K V row emitting an

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